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NUCLEOSYNTHESIS OF RARE NUCLEI FROM SEED NUCLEI IN EXPLOSIVE CARBON BURNING*

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ABSTRACT

We demonstrate that a Population I concentration of primordial heavy seed nuclei, when present in the carbon- and oxygen-rich core of the presupernova star and exposed to the temperature and free nucleon densities of explosive carbon burning, is efficiently transmuted into the rare species 36 S, 40 K, 40 Ar, 43 Ca, 46 Ca, 48 Ca, 46 Sc, 47 Ti, 49 Ti, 50 Ti, 50 Vi, 62 Ni, 64 Ni, 68 Zn, 70 Zn, and 76 Ge in approximately their solar-system abundance ratios. If the temperature is high enough ($T_9 \simeq 2.1$) that at least 10 percent of the Fe and Ni seed nuclei undergo (p, n) reactions during the explosion, the nuclei 65 Cu, 67 Zn, 71 Ga, 73 Ge, and perhaps 76 As can also be synthesized. These nuclei comprise virtually all of the relatively rare neutron-rich nuclei in the range $36 \le A \le 76$ except 54 Cr and 58 Fe. We emphasize the dependence of the results upon the rates of important nuclear reactions, most of which are unknown. The temperature, density, and timescale of the carbon explosion all have a strong influence on the results as well. We therefore regard this paper as an exploratory survey of a very difficult problem that will give increasing information about nucleosynthesis as nuclear facts and models of nuclear explosions become more secure.

I. INTRODUCTION

The features of the solar-system abundance distribution (including isotopic abundance ratios) of the elements can be produced with a remarkable degree of success by calculating the nucleosynthesis that takes place when massive stars burn their evolved cores and outer layers violently and quickly on a hydrodynamic timescale (see the recent review by Arnett and Clayton 1970). In particular, the explosive burning of ¹²C (Arnett 1969) in zones that have undergone hydrostatic helium burning seems to synthesize the solar-system abundance distribution of ²⁰Ne, ²³Na, ^{24,25,26}Mg, ²⁷Al, ^{29,30}Si, and ³¹P. At higher temperatures the explosive burning of ¹⁶O (Truran and Arnett 1970; Woosley, Arnett, and Clayton 1972) in zones that have completed hydrostatic carbon burning may account for the solar-system abundance of ²⁸Si and for abundances of major nuclei in the mass range $32 \le A \le 42$. The abundances of ⁴⁶Ti and ⁵⁰Cr are also produced in this calculation. Recent calculations (Arnett, Truran, and Woosley 1971; Woosley et al. 1972) show that explosive burning at even higher temperatures merges into quasi-equilibrium abundances (Bodansky, Clayton, and Fowler 1968) slightly altered by the cooling of the gas and by electron-capture to produce nuclei in the mass range of the iron group $(48 \le A \le 62)$.

In spite of this overwhelming success, many rare nuclei in the designated mass ranges are not produced by the explosive fuels. In particular, the relatively rare neutron-rich nuclei ³⁶S, ⁴⁰Ar, ⁴⁰K, ⁴³Ca, ⁴⁶Ca, ⁴⁸Ca, ⁴⁵Sc, ⁴⁷Ti, ⁴⁹Ti, ⁵⁰Ti, ⁵⁰V, ⁵⁴Cr, ⁵⁸Fe, ⁶³Cu, ⁶⁵Cu, ⁶⁴Ni, ⁶⁶Zn, ⁶⁸Zn, and ⁷⁰Zn are not, with possible exceptions of ⁴⁵Sc and ⁴⁹Ti, synthesized in the above-mentioned calculations. To have a consistent and viable understanding of the thermonuclear origin of the elements we must account for all nuclear species in the

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applicable mass range. Although almost all of the above-mentioned nuclei are rare, it seems important to us to account for their existence. We will report in this paper on a possible source of these nuclei that is a direct result of the explosive burning of carbon.

We assume that the presupernova star formed from material of solar-system composition, taking with minor modifications the abundances of Cameron (1968). The abundances of ³⁶Ar and ³⁸Ar have been reduced a factor of 2 from Cameron's value to account for recent results from lunar samples analyzed by Eberhardt et al. (1970), and the numerical abundance ⁴⁰K = 4.3 per 10⁶ silicon atoms is taken as the abundance when the Sun formed. The star is then initially composed of approximately 0.27 percent by mass of nuclei heavier than Mg. This mass is primarily in the form of 58 Ni, 60 Ni, 54 Fe, 56 Fe, 57 Fe, 52 Cr, 40 Ca, 36 Ar, 38 Ar, 32 S, 34 S, 31 P, 28 Si, 29 Si, and 30 Si, which are those nuclei having mass fractions $X > 10^{-5}$ g g⁻¹. We assume that these nuclei remain unaltered during the hydrostatic evolution of the star and act as "seed" for the free protons, neutrons, and α -particles liberated in the explosive carbon-burning shell. Although the concentration of these seed nuclei is small compared to that of the ¹²C and ¹⁶O in the shell, the solar mass fractions of the rare neutron-rich nuclei are even smaller (typically 10^{-7} < $X < 10^{-8}$). The seed abundances are sufficiently small that they consume only a small fraction of the liberated free particles during the explosive carbon burning. We have performed the explosive calculation with and without the seed nuclei as neutron absorbers, for example, and have found a negligibly small change in the free neutron density. We have therefore taken the free-particle densities as a function of time directly from explosive-carbon-burning calculations. This is a great simplification which allows us to decouple the fate of the seed nuclei from the small perturbation they make in the carbon burning.

II. METHOD OF CALCULATION

A computer code follows the abundance changes of the seed nuclei due to nuclear interactions when it is given the free-particle densities and the temperature as a function of time. The system of equations is linear in the sense that if each initial seed nucleus is multiplied by a factor α , the final abundances are multiplied by the same factor α. The dependence on the free-nucleon densities is more complicated. Interactions with α -particles can be ignored. As in previous explosive nucleosynthesis calculations, the density is taken to decrease one e-fold on a hydrodynamic timescale taken to be $\tau_{\rho} = (24\pi G \rho_0)^{-1/2}$, and the expansion is taken to be adiabatic so that $\rho \propto T^3$ is a good approximation. The network for calculating the fate of the seed nuclei in the charge region $12 \le Z \le 24$ involves as many as 91 species, including the isotopes ²⁸Si through ³⁵Si, ³⁰P through ³⁶P, ³²S through ³⁷S, ³⁵Cl through ⁴⁶Cl, ³⁶Ar through ⁴⁷Ar, ³⁹K through ⁵⁰K, ⁴⁰Ca through ⁵¹Ca, ⁴³Sc through ⁵⁰Sc, ⁴⁵Ti through ⁵¹Ti, ⁴⁷V through ⁵¹V, and ⁴⁸Cr through 51Cr. The limits on the size of the network were chosen from considerations of neutron separation energies for neutron-rich nuclei and of the rates for the chargeincreasing (p, γ) and (p, n) reactions for the neutron-rich nuclei. The calculations of reactions on Fe and Ni seed nuclei were performed considering only (n, γ) and (γ, n) reactions. At the temperatures we are considering (1.8 $\leq T_9 \leq$ 2.15), we can ignore proton-induced reactions for Z > 26 with an important exception to be mentioned later, and (n, p) and (n, α) reactions are energetically highly unfavorable. The Cr seed nuclei are not significant sources for any product.

A differential equation for the rate of change of the number density of each nuclear species is written involving the participating reaction rates. The set of linear differential equations are then solved by a method of backward differencing at each time, as described by Arnett and Truran (1969). Experimental rates for charged-particle-induced reactions, when available, were taken from Fowler, Caughlan, and Zimmerman (1971). The rates of Allen, Gibbons, and Macklin (1971) served as guides to these reactions and were extrapolated to the required temperature. Estimated rates were provided by Truran (1971); experimental binding energies were used when possible, but unmeasured

values were taken from estimates by Garvey et al. (1969). Beta-decay rates from the ground state of radioactive nuclei were found to play no role in the nuclear processing and were not included.

In table 1 we list the important reactions and the values of their rates for two values of the temperature. For particle-induced reactions, we list the product $N_A \langle \sigma v \rangle$ in cgs units, where N_A is Avogadro's number. For (γ, n) reactions the entry is the inverse mean lifetime in seconds of the species. The mean lifetime in seconds of the target species against a specific proton-induced reaction, for example, is given by

$$\tau_p = [\rho X_p N_{\mathbf{A}} \langle \sigma v \rangle]^{-1},$$

where ρ is the total mass density (near 10⁵ g cm⁻³ in these calculations) and X_p is the fraction of the mass in the form of free protons (near 10⁻⁹ in these calculations). This long list of rates should be very helpful not only in understanding what we have done but also in providing a quick estimate of lifetimes near $T_9 = 2$ for other workers. Examination of this table will in itself show the discerning reader how the flows go in this problem. We do not, however, wish to suggest that these entries are well-established numbers. The footnotes to the table reveal the sources of these numbers, and there the reader will see that many numbers were almost arbitrary choices on our part, especially where we believed the value of the rate to have little influence on the answers. For every reaction listed, the inverse reaction was also in the network. Reactions not listed in table 1 are believed to be unimportant for this problem. An exception to this principle lies in repeated values of cross-sections, which are indicated by the reference notes to the table; for example, the (p, n) reactions on all unstable neutron-rich isotopics of Cl were taken to have the same cross-section, as indicated by reference note (7) to table 1. Because the event is r-process-like above Fe, we have not listed the values of $N_A \langle \sigma v \rangle$ for the (n, γ) reactions on isotopes of Fe, Co, Ni, Cu, and Zn. We actually used the values 1.9×10^6 , 4.3×10^6 , and 1.0×10^7 for their even-even, even-odd, and odd-odd nuclear isotopes, but the final yields are rather insensitive to the values chosen. Much more important are their (γ, n) rates, which we do list and which are primarily determined by the unknown values of neutron separation energies. Such a rudimentary representation of the nuclear rates is not adequate for accurate solution of this problem; however, it will suffice for these exploratory calculations of what must be an important system of reactions if, in fact, explosive carbon burning actually occurs in nature as a major source of ²⁴Mg nuclei. Nonetheless, none of the yields we calculate can be regarded as correct to better than a factor of 2 or 3 at best except for specific fortuitous cases. What we will provide is a reliable overview of the general possibilities, and the very encouraging nature of our results more than warrants this approach. It will take many hard years of research into nuclear facts to secure the detailed numerical accuracy.

III. RESULTS

a) Choice of Peak Burning Temperature

The temperature of the carbon burning largely determines the magnitude of the fluxes of free particles. Our basic assumption in this paper will be that the Mg isotopes owe their thermonuclear origin to explosive carbon-burning shells. Recent calculations by one of us (W. D. A.) seem to indicate that the carbon-oxygen-rich shell of a massive ($M>10~M_{\odot}$) star will have a density $\rho\approx 10^5~{\rm g~cm^{-3}}$ just prior to its violent disruption. At this density, the peak temperature of the explosive burning must be near $2\times 10^9~{\rm K}$ for a significant amount of the $^{12}{\rm C}$ to be transmuted into $^{20}{\rm Ne}$, $^{23}{\rm Na}$, $^{24}{\rm Mg}$, $^{25}{\rm Mg}$, $^{26}{\rm Mg}$, $^{27}{\rm Al}$, $^{29}{\rm Si}$, $^{30}{\rm Si}$, and $^{31}{\rm P}$ in amounts very similar to their solar-system abundance ratios. For $T_9<2$, less than 10 percent of the carbon burns; and for $T_9>2.2$ the yields of $^{23}{\rm Na}$ and $^{25,26}{\rm Mg}$ become discouragingly small relative to that of $^{24}{\rm Mg}$. Following this reasoning, we will assume a density $\rho=10^5~{\rm g~cm^{-3}}$ and calculate the nuclear interac-

TABLE 1 DESCRION DATES

	$N_A < \sigma v >$					$N_A < \sigma v >$					
Target	Reaction	$T_9 = 2.00$	T ₉ = 2.15	Ref ⁽¹⁾	Target	Reaction	$T_9 = 2.00$	$T_9 = 2.15$	Ref ⁽¹⁾		
³² s	(n,γ)* (n,α)	4.8 (5) 3.5 (4)	4.9(5) 5.0(4)		⁴⁸ к	(γ,n)*	5.5(3)	6.7(4)	(8)		
³³ s	(n,γ)*!	3.8(5)	3.8(5)		50 _K	(Y,n)*	2.1(8)	1.3(9)	(8)		
³⁴ s	(n,α)*!	7.9(6)	8.6(6)		⁴⁰ Св	(n,γ)* (n,p)	1.1(6) 2.7(3)	1.1(6) 5.3(3)	(2)		
³⁵ s	(n,γ)*! (n,γ) (p,n)	1.1(5) 3.8(5) 6.3(4)	1.1(5) 3.8(5) 9.7(4)	(2) (3)	⁴¹ Ca	(n,γ)*! (n,p)*! (n,α)*!	4.2(6) 2.1(6) 8.1(6)	4.2(6) 2.4(6) 8.8(6)	(2)		
³⁶ s	(π,γ) (p,γ)*!	5.2(4) 9.7(3) 1.2(3)	5.7(4) 1.3(4) 2.8(3)	(2)	⁴² Ca	(n, y) (p, y)	1.2(6) 7.7(2)	1.2(6) 1.1(3)	(2)		
³⁷ s	(p,n) (γ,n)	2.6(3)	1.9(4)		⁴³ Ca	(n,γ) (p,γ)	1.2(6) 3.1(3)	1.2(6)	(2)		
³⁵ c1	(n,γ) (n,p)	3.6(6) 2.2(6)	3.7(6) 2.7(6)	(4)	⁴⁴ Са	(n, y) (p, y)	2.4(6) 3.0(3)	2.4(6) 4.4(3)	(2)		
36 _{C1}	(p,α) (n,γ)	9.6(3)	1.4(4) 2.3(6)	(5) (6)	45 _{Ca}	(n,γ) (p,n)	3.2(6) 1.6(4)	3.2(6) 2.6(4)	(2)		
-	(p,n) (n,p)* (n,α)	3.7 (4) 1.7 (7) 1.3 (5)	5.7 (4) 1.8 (7) 1.6 (5)	(9)	⁴⁶ Ca	(n, y) * (p, y)	2.4(6) 6.5(3)	2.4(6) 1.0(4)	(2)		
³⁷ Cl	(n,γ)* (p,n)	4.5(5) 3.6(3)	4.8(5) 7.4(3)	(2)	47 _{Ca}	(n,γ) (p,n)*	1.8(6) 1.3(4)	1.8(6) 2.1(4)	(2)		
20	(p, n) (p, x) *	3.7(3) 1.9(4)	5.1(3) 2.6(4)	(5) (5)	⁴⁸ Ca	(p, n) * (n, y) * (p, y) *	1.2(5) 6.6(3)	1.2(5) 1.0(4)	(2)		
³⁸ C1	(p, n) (p,α)	3.8 (4) 8.9 (3)	5.8(4) 1.5(4)	(7)	49 _{Ca}	(n,γ)	6.0(5) 1.8(2)	6.0(5) 1.6(3)	(2)		
^{‡2} C1	(Y, n)	1.8(3)	1.9(4)	(8)		(Y,n) (p,n)	1.3(4)	2.2(4)			
¹⁴ C1 ¹⁶ C1	(Y,n)*	1.8(3)	1.9(4)	(8)	50 _{Ca}	(n,γ)	6.0(5)	6.0(5)	(2)		
GC1 B6 _{Ar}	(γ,n)*	1.4(7)	7.8(7)	(8)	51 _{Ca}	(Y, n)	9.5(6)	4.5(7)	(2)		
	(n,γ)* (n,p)*! (n,α)	2.5 (5) 2.8 (5) 5.3 (4)	2.7 (5) 4.2 (5) 7.2 (4)	(2)	⁴³ Se	(n,γ) (n,p) (n,α)	1.3(6) 1.3(8) 3.6(4)	1.4(6) 1.4(8) 4.6(4)			
³⁷ Ar	(n,γ) (n,ρ)*! (n,α)*!	2.0(5) 3.8(7) 1.9(7)	2.1(5) 4.1(7) 2.0(7)	(2)	⁴⁴ Se	(n,γ) (n,p) (n,α)	5.8(6) 9.5(7) 2.2(5)	6.2(6) 1.0(8) 2.6(5)	,		
³⁸ Ar	(n,γ) (p,γ)*	7.8(5) 1.5(3)	8.5(5) 2.0(3)	(5)	⁴⁵ Sc	(p,Y) (n,Y)	1.2(3)	1.8(3)			
³⁹ Ar	(n,γ) (p,n) (n,α)	2.0(6) 2.3(4) 1.8(5)	2.1(6) 3.6(4) 2.2(5)	(9)	⁴⁶ Sc	(n,p) (p,Y)	2.6(5) 7.0(3) 9.4(6)	3.5(5) 9.6(3) 9.5(6)	(5)		
10 _{Ar}	(n, y) (p, n)	6.7 (5) 4.6(1)	7.2 (5) 1.3 (2)	(10)		(n,γ) (n,p) (p,n) (p,γ)	1.4(6) 4.3(3) 1.6(3)	1.5(6) 7.1(3) 2.6(3)			
l Ar	(p,q)*	5.1(3) 2.9(4)	7.0(3) 4.6(4)	(11)	47 _{Se}	(n,γ) (p,n)	5.6(6) 7.7(3)	6.1(6) 1.3(4)			
13 _{Ar}	(Y,n)*	9.5(1)	1.1(3)	(8)	⁴⁸ Sc	(n, y)	1.4(6)	1.5(6)			
¹⁵ Ar	(Y,n)*	1.3(3)	1.3(4)	(8)		(p,n) (p,Y)	1.2(3)	2.0(3)			
¹⁷ Ar ¹⁹ K	(Y, n) * (n, Y) *!	9.1(5) 3.5(6)	5.8(6) 3.5(6)	(8) (2)	⁴⁹ Se	(n,γ) (p,n)*	3.5(5) 8.3(3)	3.7(5) 1.4(4)			
10 _K	(n,p) (p,Y)	1.6(5) 3.8(2)	2.3(5) 5.4(2)	(5)	⁵⁰ Se	(γ, n) (ρ, n) (ρ, γ)	2.9(0) 5.8(4) 2.0(4)	4.4(1) 9.6(4) 3.3(4)			
ĸ	(n,γ) (n,p) (p,n) (n,α)	1.1(6) 3.1(6) 6.8(3) 2.6(6)	1.1(6) 3.4(6) 1.1(4) 3.0(6)	(2)	45 _{Ti}	(π, γ) (π, p) (π, α)	8.6(6) 1.7(8) 1.5(8)	8.8(6) 1.8(8) 1.6(8)			
1 _K	(n, γ) (p, n)	2.8(6) 4.0(3)	3.8(6) 7.5(3)		46 _{Ti}	(π,γ) (p,γ)	2.0(6) 8.1(2)	2.2(6) 1.2(3)			
	(p, γ) (p, α)	1.5(3)	2.0(3) 6.4(3)		47 _{Ti}	(n, Y)	7.4(6)	7.5(6)			
2 _K	(n,γ) (n,p)	1.1(7) 8.6(4)	1.1(7) 1.3(5)	(12) (11)		(n,p) (p,y)	2.9(4) 2.8(3)	4.5 (4) 4.3 (3)			
.3 _K	(p,n)	2.9(4)	3.0(4)	(13)	48 _{Ti}	(n, y) (p, y)	1.2(6) 1.7(3)	1.3(6) 2.7.(3)			
	(p, n) (p, y)	1.5(4) 5.1(2)	2.4(4) 8.2(2)	(14)	49 _{Ti}	(n, y) (p, n) *	1.5(6) 2.1(3)	1.5(6) 4.1(3)			
6 _K	(Y, n)	6.0(-1)	1.4(1)	(8)		(p, Y) *	6.3(2)	9.3(2)			

TABLE 1-Continued

N _A < σ v <							$N_A < \sigma v$	<	
Target	Reaction	$T_9 = 2.00$	$T_9 = 2.15$	Ref ⁽¹⁾	Target	Reaction	$T_9 = 2.00$	T ₉ = 2.15	Ref ⁽¹⁾
50 _{Ti}	(n, y)	3.0(5)	3.3(5)		71,73 _{Cu}	(p,n)*	5.0(2)	1.0(3)	(2)
	(p, y)	1.8(4)	2.9(4)		⁶¹ Fe	(Y,n)*	2.0(0)	2.3(1)	(8)
⁵¹ Ti	(p,n)	2.7(3)	4.6(3)		63 _{Fe}				(8)
47 _V	(n, y)	1.2(5)	1.8(5)		Fe	(Y,n)*!	3.9(2)	3.1(3)	
•	(n,p)	5.9(8)	5.7(8)		65 _{Fe}	(γ,n)*!	8.7(3)	4.6(5)	(8)
48 _V	(n, y)	1.3(7)	1.3(7)		⁶⁴ Со	(γ,n)	4.9(0)	6.3(1)	(8)
	(n,p) (p,Y)	2.1(7)	2.3(7) 2.1(3)		66 _{Co}	(Y,n)*	1.7(3)	1.4(4)	(8)
110		, ,			68			` '	
49 _V	(n, y)	8.3(6)	8.4(6)		68 _{Co}	(Y,n)*	4.5(4)	2.9(5)	(8)
	(n,p) (p,Y)	6.9(6) 1.6(3)	7.6(6) 2.6(3)		67 _{Ni}	(Y,n)*	3.0(1)	2.8(2)	(8)
50 _V	(n,γ)	1.6(6)	2.5(6)		69 _{Ni}	(Y,n)*!	6.0(2)	4.4(3)	(8)
	(p,n)	9.9(3)	1.8(4)		71 _{Ni}	(Y,n)*	1.9(4)	1.1(5)	(8)
	(p,y) (n,p)*	1.2(5) 3.9(7)	1.9(5) 4.1(7)			(Y, IL) *	1.9(4)	1.1(3)	
		, ,	. ,	(3.53	70 _{Cu}	(Y,n)*	3.1(1)	3.6(2)	(8)
Fe-Zn	(n, γ)	-	-	(15)	72 _{Cu}	(y,n)*	1.3(3)	1.1(4)	(8)
62,64 _{Fe}		1.1(3)	2.0(3)	(2)	74 _{Cu}	(Y,n)*	6.1(2)	5.6(3)	(8)
65,67 _{Co}	(p,n)*	1.1(3)	2.0(3)	(2)					
68,70 _{Ni}		5 0(2)	1.0(3)	(2)	⁷⁵ Zn	(γ,n)*	3.9(1)	3.5(2)	(8)
. NI	(p,n)*!	5.0(2)	1.0(3)	(2)	77 Zn	(γ,n)*	1.0(3)	7.4(3)	(8)

NOTES TO TABLE 1

- Important reaction rate.
- *! Very important reaction rate.
- (1) Rates for which no reference number is given are due to a private communication from James Truran (1971), who has made an extensive study, largely unpublished, of thermonuclear reaction rates.
- (2) Our estimate.
- (3) Chosen equal to ${}^{83}S(n, \gamma){}^{34}S$.
- (4) Our estimate. Same value is chosen for (n, γ) rate on 39,41,43,45 Cl. (5) Fowler *et al.* (1971).
- (6) Our estimate. Same value is chosen for (n, γ) rate on 38,40,42,44,46Cl.

- (0) Our estimate. Same value is chosen for (n, γ) rate on ^{35,40,42,44,46}Cl.
 (7) Truran (1971). Same value is chosen for (p, n) on ^{39,40,41,42,43,44,45,46}Cl. Reverse rates depend on semiempirical masses of Garvey et al. (1969).
 (8) Rates based on semiempirical (γ, n) thresholds of Garvey et al. (1969).
 (9) Our estimate. Same value is chosen for (n, γ) rates on ^{41,43,45,47}Ar.
 (10) Our estimate. Same value is chosen for (n, γ) rates on ^{42,44,46}Ar.
 (11) Truran (1971) Same value is chosen for (p, n) rates on ^{42,43,44,45,46,47}Ar. Reverse rates depend on semiempirical masses of Garvey et al. (1969).
 (12) Our estimate Same value is chosen for (n, γ) rates on ^{42,44,46,48}K
- (12) Our estimate. Same value is chosen for (n, γ) rates on ^{42,44,46,48}K.
 (13) Truran (1971). Same value is chosen for (p, n) rates on ^{44,46,48,50}K. Reverse rates depend on semiempirical masses of Garvey et al. (1969).

 (14) Truran (1971). Same value is chosen for (p, n) rates on 45,47,49 K. Reverse rate of 49 K $(p, n)^{49}$ Ca
- depends on semiempirical masses of Garvey et al. (1969).
- (15) These rates unimportant. See text.

tions at the three characteristic peak temperatures $T_9 = 2.00$, 2.05, and 2.15. These three temperatures provide a sufficiently wide variation of free-particle densities that we are able to ascertain the characteristics of the seed nucleosynthesis. Because we regard the hydrodynamic timescale as being related to the density, it will have the same value—i.e., $\tau_{\rho} = 1.4$ seconds—for each of the three calculations reported here. We will not defend this simplification except by noting that the nature of the burning depends much more strongly on temperature than on timescale. Nonetheless we acknowledge that the calculations we report here are only a sketchy survey of carbon burning.

b) Source of Free Particles

Figure 1.shows the free-proton and free-neutron mass fractions as a function of time for three temperatures. At t = 0.1 s the density has decreased by only 7 percent and the temperature by only 2 percent. A general feature of the profiles is that the neutrons dominate for the first 10^{-1} s, which for convenience we will call the "neutron-dominated phase," after which the protons dominate for the final second, which we will call the "proton-dominated phase." It is when these two phases overlap that the most complicated alteration of the seed nuclei take place. All of the features of figure 1 are determined by the basic carbon-burning reactions.

Approximately 2 percent by mass of the shell is assumed to be initially in the form of an ¹⁸O residue from the previous CNO cycle and helium burning. The ¹⁸O provides the major free-neutron source by (α, n) reactions. If the ¹⁸O were transmuted on to ²²Ne during helium burning, the nucleon densities would differ somewhat from those we will use, but the basic systematics will be similar. The neutron densities encountered during explosive carbon burning (typically $n_n = 10^{18}-10^{21}$ cm⁻³) are lower than the neutron densities usually required for r-process calculations $(n_n \simeq 10^{24} \text{ cm}^{-3})$ but much higher than neutron densities assumed for the s-process $(n_n \approx 10^{10} \text{ cm}^{-3})$. We therefore expect the capture process to be somewhat intermediate to the conventional s- and r-process pictures, and indeed that turns out to be the case. The temperatures are high enough that the photodisintegration rates of some nuclei of low neutron separation energy become important and the neutron-capture flow is stopped by (γ, n) reactions. Unlike the traditional r-process, however, the increase in Z is accomplished by (p, n) reactions rather than by β -decays.

To the extent that the capture is like the r-process, the resulting abundances depend more upon neutron separation energies (that are unmeasured) than on the rates of (n, γ) reactions. Proton-induced reactions, though slower than neutron-induced reactions, perform the role of increasing the nuclear charge and in modifying abundances when the neutron source is nearly exhausted.

At $T_9 = 2.15$, the source of free protons is the proton channel of carbon burning and, in the later stages of the burning, (α, p) reactions primarily on ²³Na. The primary importance of this proton density is due to the (p, n) reactions it causes on neutron-rich isotopes. We have not examined the extent to which the proton density is altered by

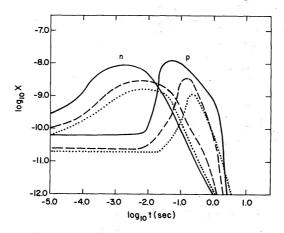


Fig. 1.—The mass fractions of free protons and neutrons are shown as a function of time during explosive carbon burning from initial density $\rho_0 = 10^6$ g cm⁻³. Solid curve, densities at $T_9 = 2.15$; dashed curve, those at $T_9 = 2.05$; dotted curve, those at $T_9 = 2.00$. The most complicated nuclear flows at $T_9 = 2.15$ take place between 10^{-2} and 10^{-1} s when both the proton and neutron fluxes are relatively high. Notice that the integrated proton flux is much larger at $T_9 = 2.15$ than at $T_9 = 2.05$ or 2.00, in contrast to the integrated neutron flux.

changes of the initial composition or hydrodynamic timescale because investigation of those questions does not seem to be necessary at the present level of accuracy.

c) Numerical Results

Table 2 lists the overabundances, defined as the ratio of the yield by mass X of each nuclear species produced by our three trial calculations to the mass fraction X_{\odot} of that species in solar material. For example, the fact that $X/X_{\odot} = 186$ for ²⁴Mg in the $T_9 =$ 2.15 explosion means that the ²⁴Mg concentration is 186 times greater after the explosion than it was before it; furthermore, it allows (but certainly does not demand) the simple interpretation that all of the natural 24Mg abundance was synthesized in this way when 1/186 of all galactic matter passed through these carbon explosions. That $X/X_{\odot} = 180$ for 36S implies that if that picture were correct, the natural 36S abundance would have been synthesized from 32 S and 36 Ar seed nuclei in the same events. That $X/X_{\odot}=1490$ for 71Ga would, on the other hand, imply that 71Ga would be overproduced by the factor 1490/186 = 8 in the same events if all of the nuclear details were accurate. Similarly only 21 percent of the ⁴³Ca would have been synthesized, etc. Nonetheless, the results are astonishing in that all species listed in table 2 are coproduced to within a factor of 8 by that simple hypothesis, and ³⁶S, ⁴⁰Ar, ⁴⁰K, ⁴⁸Ca, ⁴⁵Sc, ⁴⁷Ti, ⁴⁹Ti, ⁵⁰Ti, ⁵⁰V, ⁶²Ni, ⁶⁴Ni, ⁶⁵Cu, ⁶⁸Zn, ⁶⁹Ga, ⁷⁵As, and ⁷⁶Ge are coproduced to within a factor 3.

The results are quite temperature sensitive. For example, at $T_9 = 2.00$ the ⁷¹Ga now has negligible yield. The largest overproduction now belongs to ⁴⁶Ca, which is 67 times more overabundant than ²³Na, the most overabundant product of the carbon burning. These three columns of table 2 were calculated with the same cross-sections and Q-values, so we may infer that even if the nuclear physics were exactly known, the identity of the

TABLE 2 OVERABUNDANCES PRODUCED

		X/X_{\odot}					
PRODUCT	Primary Seed	$T_9 = 2.15$	$T_9 = 2.05$	$T_9 = 2.00$			
²⁰ Ne	C-burn	134	117	77			
²³ Na	C-burn	56	78	102			
$^{24}{ m Mg}\dots$	C-burn	186	82	44			
³⁶ S	³² S, ³⁶ Ar	180	1000	1100			
⁴⁰ Ar	³⁶ Ar, ³² S	300	220	110			
⁴⁰ K	³⁶ Ar, ³² S	290	28	1.6			
⁴³ Ca	$^{36}\mathrm{Ar}^{'}$	39	46	50			
⁴⁶ Ca	³⁶ Ar, ⁴⁰ Ca	730	3200	6700			
⁴⁸ Ca	⁴⁰ Ca [′]	110	170	140			
⁴⁵ Sc	³⁶ Ar	95	350	570			
⁴⁷ Ti	⁴⁰ Ca, ³⁶ Ar	86	230	130			
⁴⁹ Ti	⁴⁰ Ca	290	45	23			
⁵⁰ Ti	⁴⁰ Ca	68	58	58			
⁵⁰ V	⁴⁰ Ca	72	4.2	Small			
⁶² Ni	⁵⁶ Fe	190	300	320			
⁶⁴ Ni	⁵⁶ Fe	225	520	560			
⁶⁵ Cu	Fe(p, n)	930	205	57			
⁶⁷ Zn	$\operatorname{Fe}(p,n)$	690	510	170			
⁶⁸ Zn	58,60Ni	450	140	130			
⁷⁰ Zn	58,60Ni	1060	800	750			
⁶⁹ Ga	Ni(p, n)	170	Small	Small			
⁷¹ Ga	Ni(p, n)	1490	110	44			
⁷³ Ge	Ni(p, n)	770	84	34			
⁷⁵ As	Ni(p, n)	127	68	34			
⁷⁶ Ge	Zn	200	110	110			

most overabundant products would shift with changing explosive conditions. The overabundances of many of these species, moreover, depend critically on unknown nuclear

quantities, as we shall emphasize in § IV.

This order-of-magnitude success is nearly complete. Table 2 contains every rare neutron-rich nucleus between $36 \le A \le 76$ except ⁵⁴Cr, ⁵⁸Fe, and ⁶¹Ni. Because these systems of reactions necessarily occur in explosive carbon burning, we tentatively draw the following conclusion: a significant fraction of the natural abundance of all the nuclei listed in table 2 was synthesized in explosive carbon burning if ²³Na and ²⁴Mg were, but ⁵⁴Cr, ⁵⁸Fe, and ⁶¹Ni do not seem to have been so synthesized. The possible s-process origins of these last three nuclei have recently been analyzed by Peters, Fowler, and Clayton (1972); a significant amount of ^{61,62}Ni is produced in the dynamic e-process discussed by Arnett et al. (1971).

IV. NUCLEAR DETAILS

This discussion will center on the key reactions and nuclear facts that determine the yields of the important products listed in table 2. In so doing we will concentrate on our calculations at $T_9 = 2.15$ because the most complex nucleosynthesis happens in this case. Because of the higher proton density and temperature, the (p, n) reactions play

a much more important role than at the two lower temperatures.

A significant understanding of this problem is aided by knowledge of the seed nucleus responsible for the rare products. We made a thorough investigation of this at $T_9 = 2.15$ by performing separate calculations with only a single seed nucleus (one of the group 32 S, 34 S, 36 Ar, 38 Ar, and 40 Ca in turn). Beacuse the differential equations are linear in the abundance, the yield from a weighted sum of seed nuclei is equal to the weighted yields from the single seed nuclei. Table 3 lists the contributions from the five most abundant seed nuclei between silicon and chromium to the final yields of rare nuclei in the same mass range. One immediately sees that the sum of the yields from these five seeds, shown in the last column, completely dominates the total yield from the complete set of seed nuclei, which is shown in the first column. It is also clear that the origins of the several species are rather widely distributed among seed nuclei. We now turn our attention to the specific nuclear reactions by which this comes about.

a) ³⁶S

One of the most interesting features of our calculations is the production of ³⁶S. As we can see from table 3, ³⁶S has ³²S, ³⁴S, and ³⁶Ar as its primary sources and is produced

Product	Total Seed	Раз	Five-Seed				
Nucleus	YIELD X	$i={}^{32}\mathrm{S}$	³⁴ S	³⁶ Ar	38Ar	⁴⁰ Ca	YIELD Σ X _i
40Ar	3.42(-6) 1.44(-6) 5.12(-6) 2.31(-6) 1.97(-5) 4.02(-6) 1.94(-5) 5.07(-5) 1.19(-5)	0.62(-5) 1.15(-6) 0.54(-6) 0.55(-6) 0.08(-6) 0.01(-5) 0.22(-6) 0.02(-5) 0.02(-5) 0.00(-5) 0.01(-7)		0.48(-5) 1.64(-6) 0.62(-6) 3.85(-6) 1.31(-6) 0.33(-5) 2.57(-6) 0.66(-5) 0.81(-5) 0.9(-5) 0.40(-7)	0.01(-5) 0.04(-6) 0.02(-6) 0.07(-6) 0.25(-6) 0.30(-5) 0.30(-6) 0.33(-5) 0.75(-5) 0.10(-5) 0.33(-7)	0.03(-5) 0.11(-6) 0.04(-6) 0.22(-6) 0.60(-6) 1.24(-5) 0.75(-6) 0.88(-5) 3.19(-5) 0.89(-5) 1.38(-7)	1.31(-5) 3.40(-6) 1.40(-6) 4.95(-6) 2.28(-6) 1.88(-5) 3.96(-6) 1.90(-5) 4.78(-5) 1.08(-5) 2.13(-7)

209

by the following reaction sequences:

$${}^{32}S(n, \gamma){}^{33}S(n, \gamma){}^{34}S(n, \gamma){}^{35}S(n, \gamma){}^{36}S$$

$${}^{35}S(n, \gamma){}^{35}C1(n, \gamma){}^{36}C1(n, \gamma){}^{36}S$$

$$(\sim 570\%)$$

or
$${}^{35}S(p, n){}^{36}Cl(n, p){}^{36}C$$
 (~57%)

and
$${}^{36}\text{Ar}(n, p){}^{36}\text{Cl}(n, p){}^{36}\text{S}$$
 (~35%).

Needless to say, the rates of these reactions play an important role in determining the final yield of 36S. In figure 2 we show selected currents (which govern the yield of 36S) as a function of time, defined as $J_{n,i;k,l} = Y_n Y_i \rho N_A \langle \sigma v \rangle_{i,k}$. Physically $J_{n,i;k,l}$ is the contribution of the forward rate of the reaction n(i, k)l to the time rate of change, for nuclear species n, of its abundance $Y_n(Y_n \equiv X_n/A_n)$. We see that ³⁶Ar quickly flows toward ³⁶S as the ³⁶Cl(n, p) ³⁶S reaction current equilibrates early with ³⁶Ar(n, p) ³⁶Cl; however, the latter current has a late surge due to the arrival of current from 32S seed via ${}^{35}S(p, n){}^{35}Cl(n, \gamma){}^{36}Cl$. The contribution from ${}^{32}S$ seed is attenuated by the large rate of the exothermic reaction $^{33}S(n, \alpha)^{30}Si$. Truran (1971) calculates the ratio of decay widths of the compound nuclear states of ³⁴S as $\Gamma_{\alpha}/\Gamma_{\gamma} \approx 22$. This branching ratio is important because 36S is easy to produce. It shows especially large overabundances at $T_9 = 2.05$ and 2.00 in table 2, and a reduction in the ratio of decay widths would cause increased overabundances. Conversely, if the branching ratio was large enough to prevent the contribution of 32 S seed to 36 S, table 3 shows that at $T_9 = 2.15$ the yield of 36 S would be reduced by a factor 2. Thus the rate of ${}^{33}S(n, \alpha){}^{30}Si$ has an important bearing on the yield of ³⁶S. The values of the radiative neutron-capture cross-sections for sulfur also enter critically in the final yield of 36 S. We have taken the rate of 34 S $(n, \gamma)^{35}$ S to be the smallest neutron-capture rate in the sulfur chain, and as a result almost 10 times as much mass remains in ³⁴S as remains in ³⁶S at the end of the calculation. An increase in this rate could increase the final yield of ³⁶S by a substantial amount. The ³⁴S is due to ³²S seed and to the ³⁷Cl(p, α)³⁴S reaction.

As we can see from figure 2, the 36 S is built to a high abundance during the neutron-dominated phase and then is destroyed by 36 S(p, γ) 37 Cl in the proton-dominated phase. At $T_9 = 2.15$ the abundance of 36 S is reduced by an order of magnitude from its peak value by the (p, γ) reactions, and it is the relative weakness of the proton flux at $T_9 = 2.00$ and 2.05 that results in the larger overabundance of 36 S at those temperatures. In fact, we have found that the final yield of 36 S varies inversely with the rate of 36 S(p, γ) 37 Cl. For example, at $T_9 = 2.05$, we increased Truran's value for this rate by a factor 5

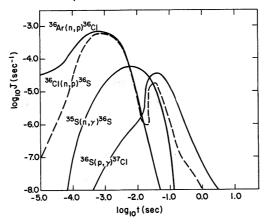


Fig. 2.—Some important reaction currents J involved in the synthesis of 36 S are shown as a function of time during the burning at $T_9 = 2.15$. The source of 36 Cl(n, p) 36 S after the 36 Ar is exhausted is the reaction sequence 35 S(p, n) 36 Cl (n, γ) 36 Cl. At this temperature the proton flux is sufficient to reduce the yield of 36 S by almost an order of magnitude.

and found a decrease in the yield of 36 S by about the same factor, making its overabundance comparable to those of the primary products of carbon burning. However, in this experiment we have exchanged one embarrassing result for another—there results a comparable overabundance of 37 Cl. There exists ample evidence that 37 Cl owes its thermonuclear origin primarily to explosive-oxygen-burning phases; thus to produce it here could cause an overproduction. At $T_9 = 2.15$, on the other hand, the 37 Cl is not produced because the proton flux is sufficient to destroy the 37 Cl, mostly by (p, α) reactions back to 34 S. We see here the tendency to establish a loop involving 34 S, 36 S, and 37 Cl, and the value of each cross-section in this loop is important, as are the (n, γ) and (p, γ) reactions on 37 Cl that cause leaks from the loop.

We conclude that the rates of ${}^{36}S(p, \gamma){}^{37}Cl(p, \alpha){}^{34}S(n, \gamma){}^{35}S$, and the branching ratio in the compound nuclear states of ${}^{34}S$, ${}^{37}Ar$, and ${}^{38}Ar$ formed by ${}^{33}S + n$, ${}^{36}Ar + n$, and ${}^{37}Cl + p$, respectively, are vital in determining the yield of ${}^{36}S$ and, by our basic assumption, placing constraints on the conditions that produce the Mg isotopes in nature.

We should first mention that the solar-system abundance of ⁴⁰Ar is very uncertain. Cameron (1968) estimated its abundance by assuming that ³⁶S, ⁴⁰Ar, and ⁴⁶Ca are synthesized by the same thermonuclear processes and should have roughly the same abundance. Since the abundance of ⁴⁰Ar is not experimentally determined, we should not place heavy emphasis on the agreement of our calculated value with Cameron's value. By the same token, an experimental determination of solar ⁴⁰Ar is badly needed.

As seen from table 3 the major sources of 40 Ar (made as itself) are 36 Ar(\sim 48 percent), 32 S(\sim 33 percent), and 34 S(\sim 13 percent). The initial neutron flow in the argon isotopes bypasses 40 Ar since the flow is not halted until it encounters the low neutron separation energies of 45 Ar and 47 Ar. During the proton-dominated phase the 40 Ar is made from the destruction of 36 S by the following reaction sequences: 36 S(p, r) 37 Cl(p, r) 38 Cl(p, r) 39 Cl(p, r) 39 Ar(r), r) 40 Ar, and 36 S(r), r) 37 Cl(r), r) 38 Ar(r), r) 39 Ar(r), r

The radioactive species 40 K has a half-life $\tau_{1/2} = 1.26 \times 10^9$ years, and its yield is not accounted for in ordinary explosive oxygen or silicon burning. In our calculation at $T_9 = 2.15$ its overabundance is 1.6 times greater than the overabundance of the primary product 24 Mg. At the two lower temperatures its overabundance seems insignificant. These overabundances, moreover, are with respect to the abundance 40 K = 4.3 per 106 silicon atoms in the solar nebula. The total production by continuous nucleosynthesis must exceed this value by a factor of 5–10 to account for its decay between nucleosynthesis and formation of the solar nebula. Thus we regard our present calculations as encouraging, but not quite adequate to explain the natural abundance of 40 K.

As mentioned previously, the 40 K is produced in the proton phase at $T_9 = 2.15$ by the reaction sequence 36 S $(p, \gamma)^{37}$ Cl $(p, \gamma)^{38}$ Ar $(p, \gamma)^{39}$ K $(n, \gamma)^{40}$ K. The (p, γ) reactions enter critically, of course, as does the rate of 39 K $(n, \gamma)^{40}$ K, which we have inferred from Allen et al. (1971).

Calculation of the ⁴⁰K abundance remains an exciting possibility. Once a viable theory for the formation of ⁴⁰K is determined, we will have another constraint for calculations of nuclear cosmochronology. Perhaps it has more than one source. Peters *et al.* (1972) showed that it may have significant contributions from weak *s*-process irradiations.

At $T_9 = 2.15$, the relative production of ⁴³Ca is a factor of 5 below that of ²⁴Mg, ⁴⁴Ca is a factor 100 below it, and ⁴⁶Ca is overproduced by a factor 4. The (n, γ) chain in

into the result.

calcium flows through these nuclei without substantial residual. They are produced instead in the proton phase when the neutrons are almost exhausted. The 43 Ca is produced as 43 Ca(\sim 63 percent), 43 K(\sim 18 percent), and 43 Cl(\sim 18 percent), with 36 Ar(\sim 75 percent) as its primary source through the reaction sequence 36 Ar(n, p) 36 Cl(n, p) 36 S(p, γ) 37 Cl(p, γ) 38 Ar(n, γ) 49 Ar(n, γ) 41 Ar(n, γ) 42 Ar(p, n) 42 K(n, γ) 43 K(p, n) 43 Ca. The rates of the unmeasured (p, n) reactions on 42 Ar and 43 K, as well as the neutron separation energy of 43 Ar, are critical in determining the final yields. An interesting feature of this calculation is the way the (p, γ), (p, n), and (n, γ) reactions interplay in rearranging the 36 S into higher-mass nuclei. The 43 Cl contribution to 43 Ca results from

energy of ⁴⁴Cl (unmeasured) stops the neutron flow by (γ, n) reactions. At $T_9 = 2.05$, if we increase the rate of ³⁶S $(p, \gamma)^{37}$ Cl to eliminate the ³⁶S overproduction as described earlier, the yield of ⁴³Ca is close to its solar-system value relative to ²⁴Mg. Under this circumstance, however, the ⁴³Ca is produced by the sequence ³⁶Ar $(n, \gamma)^{37}$ Ar $(n, p)^{37}$ Cl $(n, \gamma) \dots$ ⁴²Cl $(n, \gamma)^{43}$ Cl, where again the low ⁴⁴Cl neutron separation energy halts the flow. This Q-value, along with the rate of ³⁷Ar $(n, p)^{37}$ Cl enter critically

the sequence ${}^{36}\mathrm{S}(p,\,\gamma){}^{37}\mathrm{Cl}(n,\,\gamma)$... ${}^{42}\mathrm{Cl}(n,\,\gamma){}^{43}\mathrm{Cl}$, where the low neutron separation

The 44 Ca is produced as itself in a way similar to 43 Ca. None of the calculations come close to producing a large 44 Ca overabundance, however, so we do not think that this process is an important contributor to the 44 Ca abundance. Indeed, we did not in advance regard 44 Ca as a "rare neutron-rich nucleus"; surely it is synthesized in an α -particle process as 44 Ti. For the process described here there is simply an insufficient amount of available seed. Essentially all of the 32 S would have to be converted into 44 Ca to account for its solar-system abundance. We will not consider 44 Ca further, and it is not entered in table 2.

The 46 Ca (created as itself) has the primary sources 36 Ar(\sim 57 percent) and 40 Ca(\sim 26 percent) through the sequences 36 Ar(n, γ) 37 Ar(n, p) 37 Cl(n, γ)... 45 Cl(p, n) 45 Ar(γ , n) 44 Ar(p, n) 44 K(n, γ) 45 K(p, n) 45 Ca(n, γ) 46 Ca, and also 40 Ca(n, γ) 41 Ca(n, α) 38 Ar(n, γ)... 44 Ar(p, n) 44 K(n, γ) 45 K(p, n) 45 Ca(n, γ) 46 Ca. These snakelike chains have a kind of fascination, and the reader will easily spot nuclear question marks. The branching ratios of the three decay modes of 42 Ca are becoming very important:

$$^{42}\text{Ca} + \gamma + 11.47 \text{ MeV}$$
 $^{41}\text{Ca} + n \xrightarrow{41}\text{K} + p + 1.20 \text{ MeV}$
 $^{38}\text{Ar} + \alpha + 5.23 \text{ MeV}$.

The Coulomb barrier for an α -particle in an ³⁸Ar nucleus is only $E_{\text{Coul}} = 7.85$ MeV, so the α -channel is not inhibited much. We have taken the ratio of the branching to be $\Gamma_{\alpha}:\Gamma_{p}:\Gamma_{\gamma}=8.78:2.39:4.22$. The amount of ⁴⁰Ca seed that can be converted into ⁴³Ca and ⁴⁶Ca is dependent upon the α -particle branch. It is important to measure these three branching ratios in order to calculate the yields of ⁴⁶Ca under explosive conditions, in addition to the rates for ³⁷Ar(n, p)³⁷Cl, ³⁷Cl(n, γ)³⁸Cl, ⁴⁵Cl(p, n)⁴⁵Ar(p, n)⁴⁵K(p, n)⁴⁵Ca, ⁴⁵Ca(n, γ)⁴⁶Ca, and ⁴⁶Ca(n, γ)⁴⁷Ca. Perhaps with improved cross-section information the relative overproduction of ⁴⁶Ca may disappear.

The 46 Ca yield also depends on unknown neutron separation energies in neutron-rich matter—especially that of 45 Ar. We used Q=5.21 MeV for 44 Ar(n, γ) 45 Ar from Garvey et al. (1969), but quite acceptable uncertainties in this number change greatly the fraction of the argon (n, γ) flow that can reach 46 Ar, and at lower temperatures a significant fraction of the 46 Ca is made in this way. To check this conclusion numerically we repeated the calculations with the Q-value reduced by 400 keV. The much smaller concentration of 45 Ar, in equilibrium with 44 Ar and neutrons, allowed only a much reduced flow into 46 Ar. This had no effect on the yield at $T_9=2.15$ which, as we just explained, is

controlled by (p, n) flows; but it reduced the ⁴⁶Ca overabundance at $T_9 = 2.00$ by a factor of 5. We are thus not too discouraged by the very large overabundances of ⁴⁶Ca listed at $T_9 = 2.00$ in table 2, as it could easily be reduced by a factor of 50 with moderate changes in nuclear cross-sections and Q-values. Nonetheless it is probably the most serious systematic obstacle to synthesis near $T_9 = 2.0$, so it bears watching. As usual, only better nuclear facts can provide the answer. The ⁴⁸Ca is produced as itself from the sources ⁴⁰Ca, ³⁶Ar, and ³⁸Ar. This is the first product for which ⁴⁰Ca dominates ³⁶Ar and ³⁸Ar as a source and is the result of the impediment of the neutron flow in the calcium isotopes by a (γ, n) reaction on ⁴⁹Ca. Nonetheless, measurements of ⁴⁸Ca (n, γ) ⁴⁹Ca are needed. The ⁴⁸Ca abundance is also reduced by a factor 2 by (p, γ) reactions as the neutrons are exhausted. Measurements of that radiative capture are needed. The ³⁶Ar and ³⁸Ar is converted to ⁴⁸Ca via long sequences of (n, γ) and (p, n) chains (see ⁴⁶Ca and ⁴⁷Ti). Because the yield from ⁴⁰Ca seed is primarily due to (n, γ) reactions in calcium, it is proportional to the (n, γ) branch of ⁴¹Ca + n, again emphasizing the importance of laboratory measurements of ⁴¹Ca + n (see fig. 3).

e) 45Sc

The 45 Sc is produced as 45 Sc(\sim 45 percent), 45 Ca(\sim 38 percent), and 45 K(\sim 17 percent) with its principal sources as 36 Ar(\sim 64 percent) and 40 Ca(\sim 19 percent). The 36 Ar is converted into 45 Sc by (p, n) reactions on the 45 Ca made in the sequences described under 46 Ca production. The (n, γ) and (p, n) cross-sections of 45 Ca seem rather important, therefore.

f) 47Ti, 49Ti, 50Ti, and 50V

The synthesis of these four nuclei is closely associated with that of ⁴⁸Ca. The ⁴⁷Ti is produced as ⁴⁷Ti(\sim 13 percent), ⁴⁷Sc(\sim 34 percent), ⁴⁷Ca(\sim 37 percent), and ⁴⁷K(\sim 16 percent), with its principal sources being ⁴⁰Ca(\sim 45 percent), ³⁶Ar(\sim 34 percent), and ³⁸Ar(\sim 17 percent). The ⁴⁰Ca and ³⁸Ar seed contribute through the reaction sequence ⁴⁰Ca(n, γ) ⁴¹Ca(n, α) ³⁸Ar(n, γ) ... ⁴⁴Ar(p, n) ⁴⁴K(n, γ) ... ⁴⁷K(p, n) ⁴⁷Ca(p, n) ⁴⁷Sc(p, n) ⁴⁷Ti, and the ³⁶Ar seed nuclei contribute by the sequence ³⁶Ar(n, γ) ³⁷Ar(n, p) ³⁷Cl(n, γ) ... ⁴⁵Cl(p, n) ⁴⁵Ar(n, γ) ⁴⁶Ar(p, n) ⁴⁶K(p, γ) ⁴⁷Ca(p, n) ⁴⁷Sc(p, n) ⁴⁷Ti. The reactions ⁴¹Ca(n, α) ³⁸Ar, and ³⁷Ar(n, p) ³⁷Cl and (p, n) reactions, especially at A = 47, again play the dominant role.

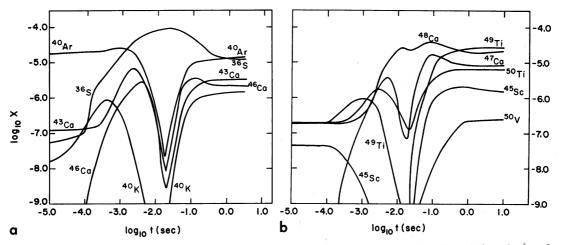


Fig. 3.—(a) and (b). The abundances of important nuclei are shown as a function of time during the burning at $T_9 = 2.15$. The abundances of those nuclei due to (p, n) and (p, γ) reactions (40 Ar, 40 K, 43 Ca, 46 Sc, 47 Ca, 49 Ti, 50 Ti, and 50 V) increase very rapidly between 10^{-2} and 10^{-1} s, while the abundances of those nuclei due to neutron induced reactions (36 S and 48 Ca) are somewhat reduced during this time. See details in text.

The ⁴⁹Ti is produced as ⁴⁹Ti(\sim 50 percent) and ⁴⁹Sc(\sim 50 percent) with the sources ⁴⁰Ca(\sim 63 percent), ³⁶Ar(\sim 16 percent), and ³⁸Ar(\sim 15 percent). The ⁴⁹Ti is produced in the proton phase from the following continuation of the above-mentioned reaction sequences: ⁴⁷Ca(n, γ)⁴⁸Ca(p, γ)⁴⁹Sc(p, n)⁴⁹Ti, and ⁴⁷Ca(p, n)⁴⁷Sc(n, γ)⁴⁸Sc(n, γ)⁴⁹Sc(p, n)⁴⁹Ti.

The ⁵⁰Ti is produced as ⁵⁰Ti(\sim 58 percent) and ⁵⁰Sc(\sim 42 percent) and also has as its sources ⁴⁰Ca(\sim 75 percent), ³⁶Ar(\sim 9 percent), and ³⁸Ar(\sim 9 percent) through the following reactions on ⁴⁹Sc: ⁴⁹Sc(p, n) ⁴⁹Ti(n, γ) ⁵⁰Ti and ⁴⁹Sc(n, γ) ⁵⁰Ti.

The nucleus ⁵⁰V is essentially stable, having a half-life $\tau_{1/2} = 6 \times 10^{15}$ years, and is surrounded by the stable isobars ⁵⁰Cr and ⁵⁰Ti. In this calculation we produce the ⁵⁰V from ⁴⁰Ca(\sim 61 percent), ³⁶Ar(\sim 18 percent), and ³⁸Ar(\sim 15 percent) by the reaction sequences ⁴⁹Ti(p, n)⁴⁹V(n, γ)⁵⁰V and ⁴⁹Ti(p, γ)⁵⁰V. The ⁵⁰V is easily destroyed during the burning by ⁵⁰V(n, p)⁵⁰Ti.

It will be clear that each of the reactions mentioned is of some importance and that careful nuclear measurements are needed.

Because of the large abundances just beyond Cr, the capture by Cr seed did not enrich significantly the natural abundance of any nucleus. Of special interest (Peters et al. 1972) is the fact that ⁵⁴Cr definitely does not owe its abundance to such events as described here.

The neutron cross-sections in Ni and Fe are large enough that the seed is quickly driven out to more massive isotopes until it is stopped by (γ, n) reactions on an isotope that has a low (\sim 4.5–5.0 MeV) neutron separation energy. The situation resembles the traditional picture of the r-process (Burbidge et al. 1957; Seeger, Fowler, and Clayton 1965; Clayton 1968) except that there is insufficient time for β -decays to allow the flow to continue and the flow terminated at the waiting point. The effect of (p, n) reactions can be ignored for the establishment of the isotopic equilibrium, although they play the role of the β -decays. The flow in Ni is halted at ⁶⁸Ni and ⁷⁰Ni because an equilibrium is established between (n, γ) and (γ, n) reactions between ⁶⁸Ni and ⁶⁹Ni and between ⁷⁰Ni and ⁷¹Ni. These equilibria are established because of the low neutron separation energies of ⁶⁹Ni and ⁷¹Ni, which are not experimentally determined. After the explosive ejection, ⁶⁸Ni and ⁷⁰Ni decay to ⁶⁸Zn and ⁷⁰Zn, and we see in table 2 that the solar abundances of ⁶⁸Zn and ⁷⁰Zn are well accounted for if such zones are responsible for all of the production of ²⁴Mg.

A similar situation occurs for Fe. The neutron flow is halted at ⁶²Fe and ⁶⁴Fe because of the low neutron separation energies of ⁶³Fe and ⁶⁵Fe, which are also not experimentally determined. After the explosive ejection the ⁶²Fe and ⁶⁴Fe decay to ⁶²Ni and ⁶⁴Ni in amounts roughly sufficient to account for their natural abundances.

The next even-Z element, zinc, is driven to ⁷⁶Zn, from which it decays to ⁷⁶Se after the event with approximately the proper yield, as shown in table 2.

These seem to be the only elements in which the element abundance exceeds by two orders of magnitude the abundance of the waiting-point isobar. Thus, for example, the heavy r-process nuclei discussed by Seeger et al. (1965) are definitely not due to events like those described here. The values of the neutron-capture cross-sections matter very little in these calculations. It is the neutron separation energies that matter. It seems to us that a great opportunity exists here, because the relative yields of these five nuclei depend almost entirely on only a few separation energies for nuclei that are not hopelessly far removed from the valley of beta stability, as they are in the conventional r-process. The spins of low-lying states of neutron-rich nuclei also play a role in their contribution to the nuclear partition functions. Consider the example of 63Fe in equi-

librium with 62Fe and neutrons:

$$\frac{N(^{63}\mathrm{Fe})}{N(^{62}\mathrm{Fe})} \propto N_n \frac{\omega(^{63}\mathrm{Fe})}{\omega(^{62}\mathrm{Fe})} \exp\left[-\frac{S_n(^{63}\mathrm{Fe})}{kT}\right].$$

The value of this ratio is very important because the 63 Fe concentration determines the (n, γ) flow that is able to penetrate onward to 64 Fe. Although the 63 Fe concentration is negligible insofar as synthesis of nuclei at A=63 is concerned, it does moderate the 62 Fe/ 64 Fe ratio and, thereby, the 62 Ni/ 64 Ni yield. What the formula reminds us is that the separation energy of a neutron from 63 Fe and the statistical weight $\omega(^{63}$ Fe) = $\Sigma_{Ei}(2J_i+1) \exp(-E_i/kT)$ of the 63 Fe nucleus, as reflected by the spins J_i and excitations E_i of its quantum states, enter in important ways into this calculation. Reliable nuclear information will thus place very tight constraints on the explosions capable of satisfying the solar 62 Ni/ 64 Ni abundance ratio.

However, it may be that 62 Ni is synthesized in an e-process followed by an alpha-rich freezeout (Arnett, Truran, and Woosley 1971), which successfully and convincingly coproduces 60,61,62 Ni. Its success would suggest that 62 Ni should not be synthesized from seed nuclei as in this paper. On the other hand, one must put the Fe seed nuclei somewhere. If about $1/200 \text{ g g}^{-1}$ of matter have passed through explosive carbon burning, as is suggested by the coproduction of 20 Ne, 23 Na, 24,25,26 Mg, and 27 Al, then 1/200 of the iron mass fraction must appear as neutron-rich isotopes. Only 60 Ni and 62 Ni are capable of absorbing this mass ($\sim 5 \times 10^{-6} \text{ g g}^{-1}$); and it does not appear, from our calculations, that the (n, γ) flow in Fe can possibly stop at 60 Fe in explosive carbon burning. Thus if we take the position that 62 Ni is not produced from seed nuclei as we have described, we are led to ask, "Where does the Fe seed go?" There is no abundance capable of hiding it. It will probably be some time before this problem is correctly unraveled, but this calculation certainly illuminates the problem.

The odd-Z nuclei do not have sufficiently large abundances to form seed for nucleosynthesis. If, on the other hand, of order 10 percent of Fe and Ni undergo (p, n) reactions while held up at their waiting points, the resultant production of Co and Cu isotopes is sufficient to allow synthesis of the nuclei listed above. The Co flow waits at 65 Co and 67 Co, with their relative abundances determined largely by the unknown 66 Co neutron separation energy. The Cu isotopes distribute themselves at A=69,71,73, and 75 in rather uncertain abundance ratios because of the uncertain neutron separation energies.

We calculated (p, n) cross-sections for Fe and Ni isotopes with the optical model approach described by Michaud and Fowler (1970), and our results were included in table 1. The fraction of nickel undergoing (p, n) transmutation, for example, drops from 27 percent to 1 percent as T_9 drops from 2.15 to 2.00. As a result, we see in table 2 that the odd-A overabundances show a strong temperature dependence. If we are to have these nuclei coproduced in this way, our results suggest that explosive carbon burning occurs primarily at temperatures less than $T_9 = 2.15$ but at least as great at $T_9 = 2.0$. It is interesting that the final yields of the primary products suggest the same conclusion. For the final yields of these nuclei we shall need good estimates of the (p, n) cross-section of 62,64 Fe, 68,70 Ni, 65,67 Co, and 69,71,73,75 Cu, as well as good estimates of the relevant neutron separation energies and nuclear statistical weights.

A preliminary account of this investigation has already been published (Howard *et al.* 1971). Subsequent recalculation of the (p, n) rates on neutron-rich isotopes of Fe and Ni indicated somewhat larger cross-sections than the estimates we used for that preliminary report. The reader will note some differences in the earlier table from the $T_9 = 2.15$

column of table 2 due to these recalculations. The larger (p, n) cross-sections used in this paper cause larger overabundances of the odd-A heavy nuclei.

It is natural to wonder if this combination of (p, n) and (n, γ) chains cannot account for even more massive r-process nuclei. We doubt it for explosive carbon burning, although there may be other contexts in which the combination might also work quite naturally. The seed/product ratio becomes much smaller at larger atomic weights.

V. DISCUSSION

These calculations have rested on a system we call the "perturbation method": the free nucleon densities are computed separately from a carbon-burning network as in Arnett (1969), and these densities are then used to calculate the abundance alteration of heavier nuclei. We assume that the existence of the heavier nuclei has not invalidated the free-nucleon densities. It is reasonable to now examine the validity of this approach. The heavy nuclei $(Z \ge 16)$ started with an initial mass fraction $X_{\text{initial}}^{\text{seed}} = 2.14 \times 10^{-2}$ 10^{-3} and initial neutron excess per nucleon $\eta_{\text{initial}}^{\text{seed}} \equiv (N-Z)/(N+Z) = 5.0 \times 10^{-2}$ and evolved to final quantities $X_{\text{final}}^{\text{seed}} = 2.31 \times 10^{-3}$ and $\eta_{\text{final}}^{\text{seed}} = 13.9 \times 10^{-2}$. The changes are largely due to the capture of free neutrons and are dominated by the iron seed. The density of excess neutrons in the primary material is $\eta = 2 \times 10^{-3}$ g of neutrons per gram of matter, located in our calculation in ¹⁸O, whereas the density of neutrons captured by heavy seed is only $X^{\text{seed}} = (2.3 \times 10^{-3}) (8.9 \times 10^{-2}) =$ 2.0×10^{-4} g of neutrons per gram of matter. Thus the basic carbon-burning network loses about 10 percent of its excess neutrons to the seed nuclei, suggesting that their explicit inclusion in the basic program (unfortunately prohibitive) would have reduced the free-neutron density by the order of 10 percent. We actually confirmed this result by including a single neutron-capturing seed nucleus in the basic program. Thus this aspect of the perturbation concept is satisfactory. As far as the basic carbon-burning program is concerned, one need only take into account that its η is effectively reduced 10 percent (at all three temperatures) by the seed nuclei. Because these neutrons are captured early in the burning, the basic carbon-burning program can be accurately doctored by inclusion of a single dummy seed nucleus (for convenience, 56 Fe) at a mass fraction X(Fe) = 2.2×10^{-3} and allowing that nucleus to capture six neutrons per seed nucleus with a cross-section near 10 millibarns, after which its (n, γ) cross-section is set equal to zero. This approximation is sufficiently accurate. The proton absorption by the seed nuclei can be neglected altogether in the generation of the free-proton density.

The approximation that the seed nuclear interactions can be decoupled from the carbon burning begins to break down at the temperature $T_9 = 2.15$ for a different reason. The final ³²S abundance, which is a steeply rising function of the burning temperature, was 6 times its initial seed abundance after this carbon-burning calculation. However, the ³²S is being produced near $t \simeq 6.0 \times 10^{-2}$ s when the neutrons are beginning to be exhausted. We expect the growing 32S to provide an increased contribution from 32S seed to 36S, 40Ar, and 40K by no more than a factor 3. This results in a total increase in the yield of ³⁶S by a factor 2 and less for ⁴⁰Ar and ⁴⁰K. We feel that this uncertainty is no more significant than the uncertainties introduced by lack of nuclear data, although this is the highest temperature at which we feel the perturbation approach as we have done it is applicable. At $T_9 \ge 2.15$ it would be preferable to enlarge the carbon-burning network to include S-Cl-Ar isotopes.

We have presented only a limited survey of the possibilities. Significant alterations of the free-nucleon densities are possible within the basic program by (1) altering the density; (2) altering the hydrodynamic timescale; (3) altering the initial composition, e.g. $X(^{12}C)$, $X(^{18}O)$, $X(^{22}Ne)$, etc.; and (4) altering the major reaction rates governing the free-nucleon densities. These effects should first be explored within the basic survey of carbon burning, rather than in the heavy-seed problem, and it seems sensible to await more thorough descriptions of the hydrodynamics of exploding carbon shells of stars.

We must acknowledge that these calculations we have presented only scratch the surface of a difficult problem. Our results *are* promising and suggest that, with adequate nuclear information, severe constraints could be placed on the explosive circumstances.

In this whole system there exists a challenge for laboratory nuclear astrophysics. Only careful measurements of key nuclear facts can clarify the correctness of the hypothesis. Basic to these are the cross-sections. To emphasize this we included in table 1 and in its footnotes the symbol * after each important reaction rate and the symbol *! after those of the highest importance to this problem. We urge those engaged in laboratory nuclear astrophysics to consider which of these reactions they can investigate by measurements or nuclear theory. Also needed are the neutron separation energies and statistical weights of neutron-rich nuclei. This problem is not new. It has existed since the *r*-process was formulated. But the information needed for this problem is for nuclei close to the mass valley of stability. Unless nuclear facts disprove this scheme, it seems likely that it can explain the origins of many of the rare nuclear species.

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