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# Variable Star Field $96^{\prime}$ South Preceding the Nucleus of the Andromeda Galaxy 

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#### Abstract

Field IV in M31 is situated $96^{\prime}$ south preceding the nucleus in the sixth spiral arm. Twenty Cepheids were found in this area and from their periods and color the absorption free distance modulus to M31 is estimated to be 24.20 , corrected for +0 m .16 reddening. There are also 7 other variables that are 2 magnitudes fainter than the Cepheids which have been called "Population II" variables. The color-magnitude diagrams show the stars brighter than $M_{\mathrm{V}}=-2^{\mathrm{m}} 7$ in M31. They show main-sequence stars, the upper portion of the red giant branch, and possibly a few $G$ and $K$ type supergiants.


## 1. introduction

DR. Baade was interested in extending his knowledge of the stellar populations and obtaining a more accurate distance to the great Andromeda galaxy. For this project he wanted to examine the variables, particularly the Cepheids. He selected three fields, shown in Plate I, that are $15^{\prime}, 35^{\prime}$, and $50^{\prime}$ south preceding the nucleus of M31. Field I he described as amorphous; Field II, the middle one, he selected because it lies in a region of mixed character ; and Dr. S. Gaposchkin (1962) has published data on the variables in that area; Field III, $50^{\prime}$ away from the center, is in a well-developed spiral arm. The data for Fields I and III will be published in subsequent papers.

Many Cepheids were found in the three fields, but the preliminary period-luminosity diagram showed a great dispersion, which is attributed to varying absorption within M31 (Baade and Swope 1955). In order to avoid this obstacle in obtaining a good distance modulus, Baade selected a fourth field $96^{\prime}$ south preceding the nucleus, in what he has described as the sixth spiral arm (Baade 1963) and which he hoped would show the minimum of absorption. The outline of this arm is traced by several associations of blue stars and from patches of ionized hydrogen. It is this field that is discussed in this paper.

During 1952 through 1954, Baade accumulated about 100 plates. In order to find variables, he blinked 21 pairs of plates. He marked 60 stars as suspected variables, 54 of which have been verified.

Baade also blinked 3 pairs of photovisual plates and found about 100 more variables that do not appear on
the photographic plates, indicating that they are red variables either of irregular or long-period type. These variables have not yet been measured.
The magnitudes of the variables discussed in this paper were first estimated by eye, and the types of variations were thus determined. The Cepheids, eclipsing stars, and a few others not too near the edge of the field were later measured with an iris photometer. This is the only one of the four fields in M31 where this is possible, since the stars in the other fields are too crowded, which affects the photometric measures. The magnitudes of the variables not measured by the photometer were estimated twice by eye and the means taken.

## 2. MAGNITUDE STANDARDS

The magnitudes for this field were derived in very much the same way as were those for the Draco system (Baade and Swope 1961). A sequence of stars was selected in the center of the region and additional stars chosen to serve as local standards around each variable. These sequences are marked on Plate II and the magnitudes listed in Tables I and II. To obtain a standard scale, four plates were selected because of their good quality images over a large area of the plate. The iris photometer measures of each plate were reduced to one plate and means taken.

Because this fourth field has only 20 Cepheids, widely distributed, it was decided to check whether magnitude correction for distance from the plate center would be necessary. (This was not done for the Draco system as there were many RR Lyrae variables avail-


Plate I. Baade's four variable star fields of M31. The plate is an enlargement of a portion of a 48 -inch Schmidt plate. The circles represent the good area of the 200 -inch plates.


Plate II. Field IV, $96^{\prime}$ south preceding nucleus of M31 from a 200 -inch 103a-O plate. Capital letters, standard sequence; small letters, local sequences. Variables are numbered; objects marked PL1-6 are planetary nebulae.
able in the center of the plate on which to base the various relationships.) For this purpose Baade had taken a series of plates offset from the center. He outlined the area of good images on each plate. The standard stars falling in this area were used to form a reduction curve and the reduced readings for the other standards and local standards in this area were read off. The differences between the scale reading derived from the centered plates and from the offset plates were then
plotted against distance from the plate center and a mean correction curve formed. No sensible correction was necessary for the variables within 5.5 min of arc or 30 mm from the plate center. The scale correction was applied directly to the photometric readings because, at any given distance, it is the same for stars of all brightnesses, but when the scale reading is translated into magnitudes, the correction varies. As an example, at 8.8 of arc from the plate center, a star

Table I. Primary sequence of M31, Field IV.

| Sequence Star | Arp, photoelectric (1950) |  |  |  | Adopted, photographic (1960) |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | B | V | B-V | U-B | B | V | B-V |
| A | 16. 24 | 15.54 | +0. 70 | +0. 19 | 16. 24 | 15.52 | +0.72 |
| B | 16. 79 | 15.92 | +0.87 | +0.46 | 16. 80 | 15.93 | +0.87 |
| C | 16.97 | 16. 26 | +0.71 | -0.02 | 16.98 | 16. 30 | +0.68 |
| E | 17. 54 | 16. 56 | $+0.98$ | +0.78 | 17.54 | 16.56 | +0.98 |
| G | 17. 73 | 17.06 | $+0.67$ | +0.12 | 17.73 | 17. 10 | +0.63 |
| $\stackrel{\mathrm{H}}{\mathrm{H}}$ | 18. 26 | 17.56 | +0.70 |  | 18. 24 | 17.55 | +0.69 |
| $\mathrm{H}^{\prime}$ |  |  |  | +15 | 18. 38 | 17.87 | +0.51 |
| I | 18. 54 | 17. 49 | +1.05 | +1.15 | 18. 54 | 17. 45 | +1.09 |
| K | 19. 17 | 19.51 18.47 | -0. 25 +0.70 | -1.12 | 19. 25 | 19.51 18.55 | -0.26 +0.65 |
| L | 19. 27 | 18.74 | +0.53 |  | 19. 28 | 18.72 | +0.56 |
| M | 19.66 | 19.6 6 | 0.00 | -0. 19 | 19.65 | 19.66 | -0.01 |
| P | 20.54 | 20.58 | -0.04 | -1.06 | 20.50 | 20.66 | -0.16 |
| Q | 20.47 | 19.42 | +1.05 |  | 20.51 | 19.43 | +1.08 |
| R | 21.01 | 20.94 | +0.07 | -0.91: | 21.03 | 21. 23 | -0. 20 |
| S | 21. 29 | 20.81 | +0.48 | $+0.25$ | 21.36 | 20.63 | +0.73 |
| T | 21.12 | 20.25 | $+0.87$ | ... | 21.31 | 20.15 | +1.16 |
| U | 21. 30 | 21.03 | +0.27 |  | 21.35 | 21.04 | +0.31 |
| V | 21. 49 | 21.64 | -0.15 | -0.87 | 21.48 | 21.56 | -0.08 |
| W | 21.58 | 21.38 | +0. 20 | -0. 75 | 21.51 | 21.57 | -0.06 |
| X | 21. 71 | 21.53 | +0.18 |  | 21.69 | 21.53 | +0.16 |
| Y | 22. 38 | 22.05 | +0.33 |  | 22.37 | 22. 05 | +0.32 |
| Z | 22. 70 | 22. 40 | +0.30 |  | 22.60 | 22. 40 | +0.20 |

that is brighter than $20^{m} \cdot 5$ has a scale correction of +12 , which translates to -0.34 , whereas one fainter than 21 m. 5 has the same scale correction but in magnitude it is $-0^{\mathrm{m}} 52$.

The standard scale readings for the main sequence
and the corrected outlying local sequences now gave a consistent system and the variables measured on the iris photometer were reduced to this system. Magnitudes for the standard scale were first obtained from plates of Field IV and Selected Area $68\left(0^{\mathrm{h}} 14^{\mathrm{m}} 00^{\mathrm{s}}\right.$ $+15^{\circ} 33.6,1950$ ) that were taken in series and developed together. S. A. 68 magnitudes are based on extensive photoelectric photometry by Stebbins, Whitford, and Johnson (1950) and by Baum (unpublished). During one session a plate of S.A. 68 was measured on the iris photometer, then a plate of Field IV taken on the same night, and again the S. A. 68 plate. The photometer readings of the selected area were plotted against the magnitude and a reduction curve drawn through the points. The photometer readings of Field IV were then transformed to magnitudes by the use of the curve. The mean magnitudes obtained by transfer needed a systematic correction of -0.08 , but otherwise compared favorably with the later magnitudes obtained from a direct photoelectric sequence.

In 1959 H. C. Arp secured photoelectric measures of

Table II. Local sequences for variables.


Table III． 54 variables．

| Var． No． <br> （1） | $\mathrm{B}_{\text {max }}$ <br> （2） | $\mathrm{B}_{\text {min }}$ <br> （3） | Photo－ metry <br> （4） | Type <br> （5） | Period <br> （6） | $1 / p$ <br> （7） | B－V <br> （8） | Dist． <br> （9） | Zero Fhase （10） | Note <br> （11） |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | m | m |  |  |  |  |  | mm |  |  |
| 1 | 21． 25 | （22．5 | a | Eclipsing | 511 | 0.0001957 | －0． 20 | 50 | 0． 200 |  |
| 2 | 21.18 | 22． 34 | b，c | Cepheid | 4． 3678 | ． 22895 | ＋0．59 | 47 | ． 100 |  |
| 3 | 20． 40 | 22． 00 | b，c | Cepheid | 12． 7144 | ． 078651 | 0.91 | 43 | ． 000 |  |
| 4 | 19． 60 | 20． 70 | a | Semiregular |  |  | 2． 25 | 8 |  |  |
| 5 | 20.69 | 21.97 | b，c | Cepheid | 12．840 | ． 07788 | 1.01 | 11 | ． 550 |  |
| 6 | 21.00 | 22． 30 | b | Semiregular | Cycles of | $\pm$ days | 0.90 | 42 |  |  |
| 7 | 20.75 | 21． 35 | a | Eclipsing |  |  | 0.08 | 36 |  | 1 |
| 8 | 20． 60 | 21． 70 | a，c | Cepheid | 9． 6432 | ． 10370 | 0． 74 | 47 | ． 300 |  |
| 9 | 20.77 | 21． 85 | b，c | Cepheid | 8.5092 | ． 11752 | 0.76 | 34 | ． 950 |  |
| 10 | 21.81 | 22． 55 | b，c | Cepheid | 3． 0431 | ． 32861 | 0.60 | 18 | ． 400 |  |
| 11 | 21． 44 | 21.90 | b，c | Cepheid | 2． 9776 | ． 335839 | ＋0．59 | 14 | ． 050 |  |
| 12 | 21.54 | 22． 08 | b | Eclipsing | 2． 32415 | ． 430265 | －0．08 | 12 | ． 500 |  |
| 13 | 22． 11 | 22． 83 | b，c | Cepheid | 3． 8030 | ． 26295 | ＋0．86 | 8 | ． 900 |  |
| 15 | 19．78 | 21． 40 | a，c | Cepheid | 21． 263 | ． 04703 | 0.95 | 53 | ． 750 |  |
| 16 | 22． 20 | 22． 80 | a | Cepheid | 2． 5136 | ． 39783 |  | 54 | ． 600 |  |
| 17 | 21． 20 | 22． 36 | b，c | Cepheid | 6． 7317 | ． 14855 | ＋0．98： | 33 | ． 700 |  |
| 19 | 19．80 | 20． 40 | a | Irregular |  |  | －0．06 | 20 |  |  |
| 20 | 21.0 | 22． 4 | a | Semiregular | Cycles of | $0^{ \pm}$days | ＋1．07 | 7 |  |  |
| 21 | 21． 64 | 22． 66 | b，c | Cepheid | 3.3477 | ． 029871 | 0． 63 | 25 | 0.000 |  |
| 22 | 21． 45 | 22． 71 | b，c | RV Tauri | 37． 30 | ． 02681 | ＋0． 74 | 37 | 1． 100 |  |
| 23 | 20.75 | 21． 15 | a | Eclipsing | 6． 3235 | ． 15814 | －0．07 | 15 | 0.950 | 2 |
| 24 | 21． 00 | 21． 80 | b，c | Semiregular | 46． 25 | ． 02162 | ＋0．80 | 38 | 0.500 |  |
| 25 | 21． 75 | 22． 83 | a | RV Tauri | 39.43 | ． 02536 | ．．．． | 55 | 1.800 |  |
| 26 | 21． 75 | 22． 35 | a | Cepheid | 3.9451 | ． 25348 |  | 52 | 0.850 |  |
| 27 | 21.85 | 22． 69 | b，c | Cepheid | 2． 5928 | ． 38568 | －0．71 | 21 | ． 300 |  |
| 28 | 21.95 | （23．0 | a | Irregular |  |  | ＋1．23 | 27 |  |  |
| 29 | 21.54 | 21.96 | b | Eclipsing | 11.905 | ． 08400 | －0．17 | 24 | ． 450 |  |
| 30 | 20.78 | 21.98 | b，c | Cepheid | 12． 8783 | ． 07765 | ＋1．05 | 36 | ． 500 |  |
| 31 | 20.08 | 20.82 | b，c | Cepheid | 13．3360 | ． 074985 | 0.66 | 18 | ． 700 |  |
| 32 | 20． 60 | 21.00 | b | Irregular |  |  | ＋1．95 | 21 |  |  |
| 33 | 20.35 | 20． 70 | b | Irregular |  |  | －0． 27 | 22 |  |  |
| 34 | 20.95 | 21． 71 | a，c | Semiregular | 62.0 | ． 01613 | ＋0．75 | 19 | ． 100 | 3 |
| 35 | 21.85 | 22． 75 | b | Eclipsing | 2． 47225 | ． 40449 | 0.03 | 16 | ． 350 |  |
| 36 | 22.05 | 22． 89 | b，c | Cepheid | 3． 5935 | ． 27829 | ＋0．78 | 39 | ． 250 |  |
| 37 | 20.00 | 20.30 | b | Short |  |  | －0．05 | 23 |  |  |
| 39 | 22． 30 | 22． 70 | b | Cepheid？ |  |  |  | 35 |  |  |
| 40 | 20.90 | 21． 45 | a | Eclipsing？ |  |  | 0.00 | 45 |  | 4 |
| 41 | 21． 75 | 22． 15 | b | Irregular |  |  | ＋0．11 | 20 |  |  |
| 42 | 21.63 | 22． 25 ： | a | Cepheid | 3.0983 | ． 32276 |  | 64 | ． 550 |  |
| 44 | 21.60 | 21.85 | b | Eclipsing |  |  | 0.00 | 6 |  |  |
| 45 | 21.95 | 22． 70 | a | Eclipsing |  |  | 0.37 | 27 |  | 5 |
| 46 | 22．62 | 23． 30 ： | b，c | Cepheid | 3． 7110 | ． 26947 | 0.93 ： | 21 | ． 450 |  |
| 48 | 22． 34 | 22． 96 | b，c | Cepheid | 3.4032 | ． 29384 | 0.73 | 43 | ． 800 |  |
| 49 | 20.5 | 21.2 | a | Irregular |  |  |  | 52 |  |  |
| 50 | 21.0 | 21.6 | b | Irregular |  |  | 2． 02 | 32 |  |  |
| 52 | 22.15 | 22． 75 | a |  |  |  | ．．．． | 48 |  |  |
| 53 | 22． 35 | 22． 99 | a | W Virginis | 19.87 | ． 05032 | ．．．． | 57 | ． 330 |  |
| 54 | 20.4 | 21． 1 | a | Irregular |  |  |  | 65 |  |  |
| 55 | 22． 40 | 23．15： | a，c | W Virginis | 19． 26 | ． 05193 | 0.93 | 25 | ． 150 |  |
| 56 | 21.5 | 22.2 | b | Irregular |  |  | 0． 20 | 40 |  |  |
| 57 | 21.86 | 22． 20 | b，c | Semiregular | 53.5 | ． 0187 | 0.70 | 38 | 0.900 |  |
| 58 | 21.5 | 22． 0 | b | Irregular |  |  | 1.97 | 13 |  |  |
| 59 | 22． 30 | （23．0 | a | Long period | 230 | ． 00435 | ＋1．80 | 23 |  |  |
| 60 | 18.90 | 19.48 | b | Eclipsing | 7． 3303 | 0． 13642 | －0． 23 | 9 |  |  |

Explanation of Table II I

Col．（4）Photometry：a－mean of 2 eye estimates
b－iris photometer，photographic plates
c－iris photometer，photovisual plates
（7）Reciprocal period used in computing phases of Tables A，B，and C．
（8）Color index of eclipsing and irregular variables derived from 3 or 4 pairs of photographic and photovisual plates．
（9）Distance from plate center to indicate reliability of magnitude and amplitude．
（10）Computed phase that corresponds to zero phase of Figs． 2 to 9.
（11）Notes．1．Five minima，6＂preceding $15^{\mathrm{m}}$ star．
2． $1^{\prime \prime}$ preceding a $21^{\mathrm{m}} 05$ star．
3． $1^{\prime \prime}$ following a faint companion．
4．Two minima．
5． $3^{\prime \prime}$ south of a $21^{\mathrm{m}} \cdot 20$ star．


Fig. 1. Effect of GG 1 and GG 13 filters on magnitudes. Ordinate, difference in magnitude GG 1-GG 13; abscissa, Arp's photoelectric measures of $B-\mathrm{V}$.

22 stars in Field IV (Table I). To adjust them to the 200 -inch plates independently of the former standards and to extend the sequence to other comparison stars, two series of 103a-O plates were selected. They were plates that had been measured for variable stars and were chosen on the basis of the least scatter around preliminary reduction curves, which indicated a good field. The original photometric measures were plotted against Arp's photoelectric magnitudes, a smooth curve was drawn and new photographic magnitudes read off. One series of seven plates had been taken with a GG 1 filter and the other series of 8 plates with a GG 13 filter. The magnitudes from the two series were compared to determine whether there was a systematic difference
between the series dependent on the color indices, but no such difference was detected. This is shown in Fig. 1, where the difference in magnitudes of the two filter series is plotted against the photoelectric $B-V$ value.

That there is no evident systematic difference between the two series of plates is due in part to the fact that Baade always used the $f / 3.67$ Ross corrector, which cuts out much of the ultraviolet light and reduces by $40 \%$ the predicted difference (Arp 1961) between the GG 1 and GG 13 filters that were used with the 103a-O plates. The difference is further minimized because the $B-V$ measures of Fig. 1 have a limited range between -0.2 and +1.2 , and because the photometer readings of both series were reduced by the same photoelectric sequence.
The photovisual magnitudes are based on the measures of four 103a-D plates taken with a GG 11 filter. The final adopted $B$ and $V$ magnitudes used for the 200 -inch plates are given in the right-hand columns of Table I. Between the photoelectric and photographic sequences there are 4 differences in $B-V$ greater than $0^{\mathrm{m}} 20$. Star T, a red star, might have varied between 1957, the time of the last plate, and 1959, when Arp made his measures. Stars R, S, and W have large unaccountable differences in $V$.

The local standards corrected for distance from plate center and the variables for which they were used are


Fig. 2. Eclipsing binaries. Crosses for V1 are photovisual observations in 1957 adjusted by $-0^{\mathrm{m} .10}$; check marks, observations below plate limit. Magnitudes of V1 and V23 are eye estimates.
listed in Table II．The last column gives the number which the star has in Table D and in the $\mathrm{C}-\mathrm{M}$ diagram． The sequences in the center area are listed first，then those for the outer variables within $8^{\prime}$ of arc，and finally approximate magnitudes for those variables lying near the edge of the plate for which no photovisual magni－ tudes were obtained．

## 3．ECLIPSING BINARIES

Table III lists the 54 variables of Field IV in order of discovery number．Explanations of the various columns are given at the bottom of the table．Among the vari－ ables are 10 eclipsing binaries， 6 of which have periods． The remaining 4 are faint，have small amplitudes，and no periods were derived；they are suspected eclipsing binaries because of their colors and because of few observations at minimum．The light curves of those with periods are given in Fig． 2.

V1，with a period of 511 days，has a color index at maximum of $-0^{\mathrm{m}} \cdot 10$ ．Only 2 minima were observed； the first eclipse in 1953 lasted longer than 40 days，the second eclipse in 1957，which was observed on photo－ visual plates cannot have lasted longer than 100 days． In the figure the crosses represent the photovisual observations made brighter by 0 m .1 ．The magnitudes of V1 are very uncertain as the star lies close to the plate edge，but part of the scatter is probably due to irregular variations at maximum．Its blue color and absolute magnitude of about -3.5 are not inconsistent with the spectral classes and luminosities found by Popper（1948） for binaries of similar period．The other binaries of Fig． 2 are mostly of the $\beta$ Lyrae type，though V12 and V35 may be like Algol．V60 was discovered because it was originally used as a standard star．If it belongs to M31，its absolute magnitude is -6 ．V29 shows so much scatter compared to the other variables that the correct period may not have been found．

Table C lists the observations for the eclipsing variables．The first column is the Julian Day corrected for heliocentric time．The phase is computed using the reciprocal of the period（Table III）in the formula

$$
\text { Phase }=1 / p(\mathrm{JD} \text { of observation }-2434000) .
$$

## 4．irregular variables

There are also 17 miscellaneous variables，mostly irregular giants．They are shown in Fig． 3 in order of their approximate colors．They have been plotted to show their type of variation from 1952 through 1956. The open circles represent single observations；the dots represent 2 or more observations on consecutive days．The first variable，V4，is the brightest of the red variables with a range greater than $1^{\mathrm{m}} 0.0$ ．It may be cyclic or irregular，like $\mu$ Cephei．It appears to be the brightest star of a small association．The next 4 stars， with $B-V$ around $+2^{m} \cdot 0$ ，show small and slow changes from year to year，with rapid fluctuation superposed．


Fig．3．Irregular variables in order of decreasing redness． Dots，mean of 2 or more consecutive observations；open circles， single observations，and for V59，photovisual observations．

Their mean characteristics are amplitude $=0^{\mathrm{m}} 5, B-V$ $=+2^{\mathrm{m}} \cdot 0$ ，and mean $B=21^{\mathrm{m}} 15$ ．

V59 is the only long－period variable that was found on the 103a－O plates．It was seldom seen and therefore fainter than $23^{\mathrm{m}} 0$ ，and never observed at maximum in photographic light．On the photovisual plates it varies from $V=20^{\mathrm{m}} \cdot 4$ to $22^{\mathrm{m}} \cdot 3$ ．These observations are shown as open circles above the photographic obser－

Table IV. 20 Cepheids.

| Var. No. <br> (1) | Period <br> (2) | Log P <br> (3) | B |  |  |  | V |  |  |  | B-V |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Max. <br> (4) | Min. <br> (5) | Ampl. <br> (6) | $\begin{aligned} & \text { Mag. of } \\ & \text { Mean }_{\text {I }} \end{aligned}$ <br> (7) | Max. <br> (8) | Min. <br> (9) | Ampl. (10) | Mag. of Mean $_{\text {I }}$ (11) | Max. <br> (12) | Min. <br> (13) | Ampl. (14) | Mag. of Mean $_{I}$ (15) |
| 15 | 21. 263 | 1.328 | 19.78 | 21. 40 | 1.62 | 20.68 | 19.31 | 20.28 | 0.97 | 19.80 | 0.45 | 1. 20 | 0.75 | 0.95 |
| 31 | 13. 336 | 1.125 | 20.08 | 20.82 | 0. 74 | 20.46 | 19.57 | 20.07 | . 50 | 19.81 | . 52 | 0.80 | . 28 | 0.66 |
| 30 | 12. 878 | 1.110 | 20.78 | 21.98 | 1. 20 | 21. 38 | 20.05 | 20.77 | . 72 | 20.38 | . 72 | 1. 30 | . 58 | 1.05 |
| 5 | 12. 840 | 1. 109 | 20.69 | 21.97 | 1. 28 | 21. 32 | 19.94 | 20.68 | . 74 | 20.35 | . 65 | 1.35 | . 70 | 1.01 |
| 3 | 12. 714 | 1. 104 | 20.40 | 22.00 | 1.60 | 21.23 | 19.90 | 20.82 | . 92 | 20.38 | . 52 | 1. 206 | . 74 | 0.91 |
| 8 | 9. 643 | 0.984 | 20. 60 | 21. 70 | 1. 10 | 21.08 | 20.10 | 20. 70 | . 60 | 20.37 | . 50 | 1.06 | . 56 | 0.74 |
| 9 | 8. 508 | 0.930 | 20.77 | 21. 85 | 1.08 | 21. 29 | 20.30 | 20.86 | . 56 | 20.55 | . 47 | 1.03 | . 56 | 0.76 |
| 17 | 6. 732 | 0.828 | 21. 22 | 22. 34 | 1.12 | 21. 82 | 20.50: | 21.12: | . 62 | 20.83: | . 68 : | 1. 20 : | . 52 : | 1.01: |
| 2 | 4. 368 | 0.640 | 21.18 | 22. 34 | 1.16 | 21. 80 | 20. 75 | 21.55 | . 80 | 21. 24 | . 42 | 0.80 | . 38 | 0.59 |
| 26 | 3. 945 | 0.596 | 21. 75 | 22. 35 | 0.60 | 22. 13 |  |  |  |  |  |  | . . |  |
| 13 | 3. 803 | 0.580 | 22. 11 | 22. 83 | 0.72 | 22. 56 | 21. 45 | 21.85 | . 40 | 21. 72 | . 65 | 1.00 | . 35 | 0.86 |
| 46 | 3. 711 | 0.569 | 22. 62 | 23. 30 : | 0.68 : | 23.07: | 21.81 | 22.45: | . 64 : | 22.15: | . 75 | 1.10: | . 35 : | 0.93 : |
| 36 | 3.593 | 0.555 | 22. 05 | 22. 89 | 0.84 | 22.51 | 21.50 | 21.95 | . 45 | 21. 74 | . 55 | 1.05 | . 50 | 0.78 |
| 48 | 3. 403 | 0.532 | 22. 34 | 22.96: | 0.62: | 22.74: | 21.90 | 22.10: | . 20 : | 22.02: | . 40 | 0.90 : | . 50 : | 0.73 : |
| 21 | 3. 348 | 0.525 | 21. 64 | 22. 66 | 1.02 | 22. 25 | 21.19 | 21.93 | . 74 | 21.64 | . 38 | 0.82 | . 44 | 0.63 |
| 42 | 3. 098 | 0.491 | 21.63 | 22. 25 | 0.62 | 22. 00 |  |  |  |  |  |  |  |  |
| 10 | 3. 043 | 0.483 | 21.81 | 22.55 | 0. 74 | 22. 29 | 21. 30 | 21.90 | . 60 | 21.70 | . 47 | 0.71 | . 24 | 0.60 |
| 11 | 2. 978 | 0.474 | 21. 44 | 21.90 | 0.46 | 21.68 | 21.00 | 21.26 | . 26 | 21.09 | . 45 | 0.69 | . 24 | 0.59 |
| 27 | 2. 593 | 0.414 | 21. 85 | 22. 69 | 0.84 | 22.37 | 21.38 | 21.86 | 0. 48 | 21.68 | 0.50 | 0.92 | 0.42 | 0.71 |
| 16 | 2.514 | 0.400 | 22. 20 | 22.80: | 0.60: | 22.55: |  |  |  | . . | ... | ... | ... |  |

Table V. 7 "Population II" variables.

| Var. No. <br> (1) | Period <br> (2) | Log P <br> (3) | B |  |  |  | V |  |  |  | B-V |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Max. <br> (4) | Min. <br> (5) | Ampl. <br> (6) | Mag. of Mean $_{I}$ <br> (7) | Max. <br> (8) | Min. <br> (9) | Ampl. <br> (10) | Mag. of Mean $_{I}$ (11) | Max. (12) | Min. <br> (13) | Ampl. <br> (14) | Mag. of Mean $_{I}$ (15) |
| 34 | 62.0 | 1. 792 | 20.95 | 21. 71 | 0.76 | 21.33 | 20.33 | 20.81 | 0.48 | 20.59 | 0.55 | 0.95 |  |  |
| 57 | 53.5 | 1. 728 | 21. 86 | 22. 20 | 0. 34 | 22.04 | 21.18 | 21. 42 | . 24 | 21.33 | . 60 | 0.86 | . 26 | . 70 |
| 24 | 46. 25 | 1. 665 | 21.00 | 21. 80 | 0.80 | 21. 37 | 20.45 | 20.80 | . 35 | 20.58 | . 60 | 1.00 | . 40 | . 80 |
| 25 22 | 39.43 37.30 | 1.596 1.572 | 21.75 21.45 | 22.83 22.71 | 1.08 1.26 | 22.14 21.96 | 21.05 | 21.70 | .65 | $\stackrel{11 .}{ }{ }^{\text {a }}$ | .40 | 1.00 | $\because 60$ | . 74 |
| 53 | 19.87 | 1. 298 | 22. 35 | 22.99 | 0.64 | 22.63 |  |  |  |  |  |  |  |  |
| 55 | 19.26 | 1. 285 | 22. 40 | 23.15: | 0.75: | 22.74: | 21. 60 | 22.20: | 0.60 : | 21.81: | 0.70 | 1.15: | 0.45 : | 0.93 |

vations of V59 in Fig. 3. For the 5 years that it was observed it appears to have alternating high and low maxima. Its period is around 230 days.

The next 3 stars are semiregular. V28 has a $B-V$ $=+1 \mathrm{~m} .23$. It has a varying mean magnitude and may be similar to a variable like DF Cygni, though it should be observed for a longer time. V20 and V6 have cycles around 150 and 85 days, respectively, and $B-V$ of $+1^{\mathrm{m}} .07$ and $+0^{\mathrm{m}} \cdot 78$, but their variation is too irregular to obtain a mean light curve. It is possible that they might belong to the "Population II" variables that are discussed later. V49 with a range of 0 m 5 seems to vary from year to year. It is near the edge of the plates and no photovisual measures were made, but it seems to be neither red nor very blue.

The last 5 variables in Fig. 3 again have small amplitudes and slow variations. Their color indices are around zero. Of these, V19 is the only variable with distinct characteristics. In 1952 it was bright at $B=19.80$, and slowly decreased in luminosity until in 1956 it was about 20 m .4 . V19 lies in the brightest association of Field IV, as do the blue variable V33 and the red one, V32. The mean characteristics of the last 4 variables are amplitude $=0^{\mathrm{m}} \cdot 5, B-V=0^{\mathrm{m}} \cdot 0$, and mean $B=21^{\mathrm{m}} 4$.

Three variables have not been plotted. Their variation is probably short, and, if periodic, shorter than 4 days. They are V52, which is faint and near the edge
of the field; V39, also faint; and V37, which lies near the bright association, has a small amplitude, and is rather blue in color.

## 5. CEPHEIDS

Table IV lists the Cepheid variables in order of decreasing period and gives more extensive information about magnitudes and colors than Table III. Columns 7,11 , and 15 list the magnitudes of mean intensity which were derived from magnitudes taken at 20 equal phase intervals along the light curve, converted to light intensities, and then the mean intensity converted back to magnitude. The $B-V$ magnitudes, columns 12 and 13 , were also derived from the $B-V$ light curves and are not the same as column 7 minus column 11. The difference, due to different ways of deriving $B-V$, is greatest for those with greatest asymmetry.

Table A gives the photographic observations of Cepheids with the phase computed from the same formula as that used for the eclipsing stars. The number of the epoch from the initial Julian Day has been included. Table B for photovisual observations is similar to Table A, but when an observation is paired to a photographic plate taken just before or after it on the same night, the $B-V$ value is given. In a few cases when the observations occurred on a steep part of the curve, the photographic observation has been
extrapolated to the time of the photovisual observation. No $B-V$ difference is given when $V$ is fainter than $22^{\mathrm{m}} \cdot 10$, as the accidental error has increased and the $B-V$ value becomes almost meaningless.

Of the 20 Cepheids in Table IV, three (V16, V26, and V 42 ) are close to the edge of the plates and their magnitudes are based on eye estimates of photographic plates only. V8 and V15 also lie closer to the plate edge than do their comparison stars, and are brighter than $B=21^{\mathrm{m}} 6$ at minimum. Since V15 has the longest period in the field and V8 has a period close to 10 days, an effort has been made to bring their magnitudes into the system of the other Cepheids. The eye estimates, though they are subject to larger accidental errors, are not as seriously affected by systematic errors; therefore, a correction curve formed from the differences between the iris photometer and eye measures plotted against the eye-estimated magnitudes was used to correct the photometer measures. It is these corrected values that are plotted in the figures and are given in Tables A and B. These corrected values agree with the magnitudes made on the few available offset plates.

The magnitudes of V48 seem uncertain because the variable is in a position on the 200 -inch plates where the images break rapidly due to the edge of the Ross corrector. V46, close to the plate limit, suffers from bigger measuring errors. In measuring V17 on the photovisual plates, it was overlooked that there was a gap in the local sequence in $V$ of some two magnitudes over the interval of variation of the star. This may cause an error in $V$ of $\pm 0^{\mathrm{m}} \cdot 15$, which causes the error in $B-V$ to be exaggerated; hence the star has been omitted from any discussion of the relationships involving color.

The light curves of the 20 Cepheids are given in Figs. 4 through 8. The upper curves represent measures from the photographic plates, the middle ones show the photovisual observations, and the curves at the bottom are the $B-V$ differences. Single observations are plotted; the dots represent measures by the iris photometer and the open circles are from eye estimates. The lightly drawn $B$ and $V$ curves are derived from mean normal points. The curves for the $B-V$ observations are the differences for like phases of the mean $B$ and $V$ curves. This is because there are only 30 direct $B-V$ observations.

An intercomparison of the $B$ and $V$ amplitudes is shown in Fig. 9. This was done as a check on the relative correctness of the $B$ and $V$ scale of magnitudes, as most of the observations are fainter than $V=20$. A comparison of the photoelectric amplitudes of galactic Cepheids from lists of Eggen et al. (1957), Weaver et al. (1960), Irwin (1961), and Bahner et al. (1962) gives a slope of $V$ amplitude $=0.65 B$ amplitude, with a scatter of less than $\pm 0^{\mathrm{m}} 08$. Figure 9 shows the line of this slope and the scatter of the Field IV Cepheids around the curve. They fall for the most part within the allowable scatter, except for the faint variables, V46 and V48.

## 6. THE CEPHEID RELATIONSHIP OF PERIOD TO LUMINOSITY AND COLOR

The preceding section has discussed the variables as individuals; this section will examine the various relationships of the Cepheids. In Figs. 12 to 14, which show these relationships, the dots represent the classical Cepheids. The small open circles in Figs. 12 to 15 represent the mean of the Cepheids with periods over 8 days and those under 5 days. It is these mean points that are primarily used to fit the predicted relations.
The three sources of scatter around the mean curves of Figs. 12 to 14 are observational error, intrinsic differences in the variables, and differential absorption. The observational error increases with faintness of the magnitude and small errors in either or both $B$ and $V$ are magnified in $B-V$.
The second cause of scatter is the effect of the finite width of the instability gap, as predicted by Sandage (1958). Scatter due to this cause is shown by V31, a Cepheid of small amplitude and relative blueness which lies above the curve, while V3, of similar period with a large amplitude and redder, falls close to the mean P-L curve.
The third cause of scatter is differential reddening, which is so evident in two other fields of M31 (Baade and Swope 1955) and also apparent in Field II (Gaposchkin 1962) ; however, in this field with only 20 Cepheids and $96^{\prime}$ from the nucleus, the differential reddening has been ignored. This third cause of scatter will be further discussed in a later paper.

In Fig. 12(a) the straight-line period-luminosity curve is from Kraft's (1961) and Arp's (1960) equation $M_{B}=-1.33-2.25 \log P$, shifted in magnitude to give the best fit. In Fig. 12(b) the photovisual P-L curve has been fitted in the same manner but the equation used is the mean of Kraft's and Arp's slopes:

$$
M_{V}=-1.70-2.50 \log P
$$

Figure 13 shows the period-color relation; the equation for the solid line is $B-V=+0.35+0.34 \log P$, which was used instead of the quadratic equation given by Kraft (1961) for his mean relation for the galactic Cepheids corrected for reddening. Kraft had few Cepheids of long or short period and the equation for the straight line fits the segment between 2.5 and 25 days. The arrows indicate the dispersion of the galactic Cepheids about the mean curve. It is at once evident that the Cepheids in Andromeda are redder than the corrected galactic Cepheids. The dashed line represents the mean of the differences between the galactic relation and the observed colors of the Field IV Cepheids.

The mean color excess is $B-V=+0^{\mathrm{m}} \cdot 16 \pm 0.03$. The reddening for M31 expected from the cosecant law (Hubble 1934) is $+0^{\text {m. }} 15$, suggesting that most of the absorption is from our Galaxy and that little general reddening is due to Andromeda itself. This observational finding is not too surprising, as Stebbins and



Fig. 4. Cepheids. Dots, iris photometer measures; open circles, eye estimates.


Fig. 5. Cepheids. Dots, iris photometer measures; open circles, eye estimates.


Fig. 6. Cepheids. Dots, iris photometer measures; open circles, eye estimates.

Whitford (1934) had estimated that the sun's relative position in M31, based on surface luminosities, would be about $1^{\circ}$ from the nucleus. Field IV, 1.6 from the nucleus, is more than $60 \%$ farther out and, therefore, less absorption may be expected than is observed in the neighborhood of the sun. Van der Hulst, Raimond, and van Worden (1957) also found that in M31, at
1.5 out from the nucleus on the southwest axis, very little hydrogen was observed.

## 7. distance

Having seen that the slope of the $\mathrm{P}-\mathrm{L}$ relationship for Andromeda is similar to that for our Galaxy and the Small Magellanic Cloud, and having determined the
average color excess, the distance to Andromeda can be obtained. The apparent modulus for each Cepheid in both $B$ and $V$ was found from the equations for absolute magnitude and the magnitudes of mean intensity from Table IV. For 20 Cepheids the mean apparent modulus in $B$ is 24.84 , with a mean error of $\pm 0^{\mathrm{m}} \cdot 08$, and for 17 Cepheids the modulus in $V$ is $24^{\mathrm{m}} .68 \pm 0.07$ m.e. Correcting for the mean reddening of $+0^{\mathrm{m}} \cdot 16 \pm 0.03$, the unreddened modulus for both $B$ and $V$ is $24 \cdot \mathrm{~m} \cdot 20 \pm 0 \mathrm{~m} \cdot 14$. The distance to Andromeda is $692 \pm 50 \mathrm{kpc}$, and the distance of the sixth spiral arm is 19300 pc south preceding the nucleus of M31.

The internal error from the material of M31 is around $10 \%$, but there are also errors due to the uncertainties in the fundamental sequences of M31 and to the uncertainties still remaining in the galactic standards, such as the estimated reddening for the galactic Cepheids. The slope of the P-L curve might also be changed if Cepheids of longer and shorter periods would be photoelectrically observed. These could double the mean error. There is also the question whether Cepheids in the Andromeda galaxy are the same as galactic Cepheids. So far the evidence indicates that they are very like the galactic Cepheids, but that


Fig. 7. Cepheids. Dots, iris photometer measures; open circles, eye estimates.


Fig. 8. Cepheids. Dots, iris photometer measures; open circles, eye estimates.
there may be differences between the Cepheids of these two galaxies and the Magellanic Cloud Cepheids. The Large Cloud apparently has a steeper P-L slope (Woolley et al. 1962), and both Clouds have many large-amplitude Cepheids with periods less than 5 days, which is contrary to what has been found so far in M31 and the Milky Way system.

## 8. Instability gap

Figure 14 shows the distribution of the Cepheids across the instability gap of the $\mathrm{C}-\mathrm{M}$ diagram; the
symbols are described in Sec. 6. The variables have been plotted using the left-hand and bottom coordinates corresponding to apparent $V$ and $B-V$. The lines that are shown have been plotted using the right-hand ordinate of absolute magnitudes and the top abscissa, which is $B-V$ corrected for reddening. The vertical line is the computed relation for galactic Cepheids from the equations for period, luminosity, and color (Sandage 1958; Kraft 1961), and the cross lines are the lines of constant period. The M31 and galactic Cepheids

Table VI．Absolute magnitudes of Cepheids and Population II variables in Field IV，M31．

| Var． | Log P | $\mathrm{M}_{\mathrm{B}}$ | $\mathrm{M}_{\mathrm{V}}$ |
| :---: | :---: | :---: | :---: |
| 15 | 1． 328 | －4．16 | －4． 88 |
| 31 | 1.125 | －4． 38 | －4． 87 |
| 30 | 1.110 | $-3.46$ | －4． 30 |
| 5 | 1． 109 | $-3.52$ | －4． 33 |
| 3 | 1． 104 | －3．61 | －4．30 |
| 8 | 0.984 | －3．76 | －4． 31 |
| 9 | ． 930 | －3．55 | －4． 13 |
| 17 | ． 828 | －3．02 | －3． 81 ： |
| 2 | ． 640 | －3．04 | －3． 44 |
| 26 | ． 596 | －2． 71 | ．．． |
| 13 | ． 580 | －2． 28 | －2．96 |
| 46 | ． 569 | －1．77： | －2．53： |
| 36 | ． 555 | －2． 33 | －2．94 |
| 48 | ． 532 | －2．10： | －2．66： |
| 21 | ． 525 | －2． 59 | －3．04 |
| 42 | ． 491 | －2． 84 |  |
| 10 | ． 483 | －2． 55 | －－2．98 |
| 11 | ． 474 | －3．16 | －3．59 |
| 27 | ． 414 | －2． 47. | $-3.00$ |
| 16 | 0． 400 | －－2． 29 ： | ． |
| 34 | 1． 792 | －3． 51 | －4． 09 |
| 57 | 1． 728 | $-2.80$ | $-3.35$ |
| 24 | 1． 665 | －－3． 47 | －4． 10 |
| 25 | 1． 596 | －－2． 70 |  |
| 22 | 1.572 | －－2．88 | $-3.41$ |
| 53 | 1． 298 | －2． 21 |  |
| 55 | 1． 285 | －2．10： | －2．87： |

appear to have similar luminosities and colors for the same period．
The other Cepheid relationships，such as amplitude， asymmetry，and frequency，that do not involve color have been left to a later paper when the more numerous Cepheids of Fields I and III will be discussed．

## 9．population il variables

There are 7 variables in Field IV with periods between 19 and 62 days．In Table III they have been listed as semiregular，RV Tauri，and W Virginis type variables．There seems to be a relation between their length of period and brightness．However，compared with the Cepheids of Table IV，they are less regular in period，they have a larger magnitude scatter around


Fig．9．Comparison of $B$ and $V$ amplitudes．Dots，Cepheids of Table IV；open squares，variables of Table V．Line is $B$ and $V$ amplitude relation of galactic Cepheids and arrows show dispersion．
the mean light curves，and for corresponding periods they are about two magnitudes fainter．Particularly for this last reason，and for the convenience of a general term，they have been called＂Population II＂variables in the rest of this paper．Because their characteristics are so varied，the designation＂Type II＂Cepheids seemed inappropriate as it expressed too limited a term． These 7 variables are listed in Table V．It is similar to Table IV，which was described in Sec．5．The individual observations are included in Tables A and B．

V34，V57，and V24（Fig．10）have periods between 46 and 62 days，with small amplitudes．V57 shows a great deal of scatter，which may be caused by the wrong period or the measures may suffer from the same troubles as do those for V48（Sec．5）．V34，which because of a close companion was estimated by eye only，seems fairly regular for the 6 yr observed．V24 has been treated as if it had a constant period but occasionally the time of maximum shifted．The lower curves on the left in Fig． 10 are the observations of V24 in 1952，1953，and 1957．The lower curves on the right are for 1954，1955，and 1956．The first observed shift was around JD 2434700，so the last 3 observations of 1953 are plotted in the light curve on the right－hand

Table VII．Absolute magnitudes for globular－cluster variables in the Milky Way system with periods over one day．

| Globular Cluster <br> Variables |  | Log P | Apparent Magnitude＊ |  |  | Cosecant Reddening | Corrected for Reddening |  |  | Absolute Magnitude （RR Lyr Var．+0.45 ） |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathrm{m}-\mathrm{M}$ | V | B－V | $(\mathrm{m}-\mathrm{M})_{0}$ |  | $\mathrm{V}_{0}$ | $(\mathrm{B}-\mathrm{V})_{0}$ | $\mathrm{m}-\mathrm{M}$ | $\mathrm{M}_{\mathrm{V}}$ |
| M2 | 11 |  | 1.53 | 16.1 | 12． 23 | 0.57 | 0.10 | 15.80 | 11.93 | 0． 47 | 15.35 | －3． 42 |
|  | 6 | 1． 29 | 13.03 |  | ． 67 | 12.73 |  |  | ． 57 | －2． 62 |  |
|  | 5 | 1． 25 | 13． 24 |  | ． 65 | 12.94 |  |  | ． 55 | －2． 41 |  |
|  | 1 | 1.19 | 13．39 |  | ． 63 | 13.09 |  |  | ． 53 | －2． 26 |  |
| M3 | 154 | 1.18 | 15.6 | 12.32 | ． 53 | 0.06 | 15.42 | 12.14 | ． 47 | 14.97 | －2．83 |
| M5 | 84 | 1． 42 | 15.0 | 11． 36 | ． 61 | 0.08 | 14． 76 | 11.12 | ． 53 | 14． 31 | －3．19 |
|  | 42 | 1． 41 |  | 11． 31 | ． 57 |  |  | 11.07 | ． 49 |  | －3． 24 |
| M10 | 2 | 1． 27 | 14． 7 | 11.83 | ． 82 | 0． 17 | 14． 19 | 11．32 | ． 65 | 13． 74 | －2． 42 |
|  | 3 | 0.90 |  | 12.76 | ． 76 |  |  | 12． 25 | ． 59 |  | －1．49 |
| M13 | 2 | 0.71 | 14.6 | 12． 78 | ． 59 | 0.09 | 14． 33 | 12.51 | ． 50 | 13.88 | －1．37 |
|  | 6 | 0.33 |  | 13.85 | ． 63 |  |  | 13.58 | ． 54 |  | －0．30 |
|  | 1 | 0.16 |  | 13.69 | ． 52 |  |  | 13.42 | ． 43 |  | －0．46 |
| M15 | 1 | 0.16 | 15.8 | 14.89 | 0.33 | 0.12 | 15． 44 | 14.53 | 0.21 | 14.99 | －0．46 |

＊Arp＇s（1955）magnitudes adjusted to $\mathrm{B}, \mathrm{V}$ system．
side. The last 3 observations of 1955 seem to fit better on the light curves on the left-hand side. Though V24 is unstable, it does not have the deep and shallow minimum typical of RV Tauri-type variables.

In Fig. 11 V25 and V53, both near the edge of the plate, were estimated by eye and on photographic plates only. V22 and V25 have characteristic RV Tauri-type light curves. The double periods have been plotted in Fig. 11; however, the single periods are given
in the table, are used to compute phases, and have been plotted in the graphs showing relationships. V25 has varied fairly regularly for the five years observed. V22 has shifted the time of its deep minima. This happened in 1955 and in 1957; they have been plotted in Fig. 11 as open circles, but shifted by one-half period.

The last 2 variables, V53 and V55, are both faint and have similar light curves. They are probably W Virginistype variables.


FIG. 10. "Population II" variables or semiregular variables. For V24, which shifted time of maximum, light curves on lower left represent observations in 1952, 1953, and 1957; those on lower right, observations of 1954, 1955, and 1956. For V34, only eye estimates because of close companion.


Fig. 11. "Population II" variables. Two RV Tauri and two W Virginis-type variables. V25 and V53 are eye estimates. Check marks indicate observations below plate limit; open circles in V22 are observations of 1955 and 1957 shifted by one-half period.


Figs. 12(a) and $12(\mathrm{~b})$. Period-luminosity relation in $B$ and $V$, respectively. Dots, Cepheids; open squares, Population II variables; small open circles, mean points.
10. RELATION OF THE POPULATION II VARIABLES TO THE CLASSICAL CEPHEIDS

In Figs. 12 through 15 the Population II variables of Table $V$ are plotted as open squares. The small open circle is the mean of the variables with periods over 35 days. The $\mathrm{P}-\mathrm{L}$ slope for the Population II Cepheids has been drawn parallel to that determined for the Cepheids of Population I. It was not possible to make an independent determination of slope as the Population II variables are too few and have too limited a range of period. The parallel curves were shifted up and down


Fig. 13. Period-color relation. Symbols are the same as in Fig. 12. Solid line is the $\mathrm{P}-\mathrm{C}$ relation for galactic Cepheids and arrows show the disnersion. Dashed line indicates the average reddening of 0 m 16 for M31 Cepheids.
to find the best separation between the two classes of variables. For the photographic observations [Fig. $12(\mathrm{a})]$ the separation is about $2^{\mathrm{m}} .00$; for the photovisual curves [Fig. 12(b)] the Population II variables are $2^{\mathrm{m}} 15$ fainter. In Fig. 13 the Population II variables are bluer than would be expected for the colors of Cepheids with periods of equal length. This blueness is also characteristic of W Virginis-type variables found in globular clusters. Though there is no diagram for the period-amplitude relation in this paper, for their length of period these variables seem to have rather smaller amplitudes than regular Cepheids of like periods.

In Fig. 14 the Population II variables also fall in the instability gap. However, the displacement between the periods of a Cepheid and a Population II variable


FIG. 14. Instability gap. Symbols are the same as in Fig. 12. Left-hand and bottom coordinates are annarent $V$ and $B-V$; right-hand and ton coordinates are absolute $M_{V}$ and $B-V$ corrected for reddening. Vertical line is Kraft's (1961) luminositycolor relation for galactic Cepheids and cross lines show the period grid for Cepheids. For periods for Population II variables, see Sec. 10.
of the same luminosity and color is derived from Fig. 12 , and the relation between periods of the same luminosity is given by

$$
\log P_{\mathrm{II}}=\log P_{\mathrm{I}}+0.8
$$

where $P_{\mathrm{I}}$ and $P_{\mathrm{II}}$ are the periods of the Cepheids and Population II variables, respectively.
11. Population il variables of m31 and globular CLUSTER VARIABLES WITH PERIODS GREATER THAN ONE DAY

It is apparent that these 7 variables of Table V form a sequence in $\mathrm{P}-\mathrm{L}$ and $\mathrm{P}-\mathrm{C}$ relationships which are displaced from those observed for the classical Cepheids.

Fig. 15. Period-luminosity relation. Dots and open squares, Cepheids and Population II variables in M31, respectively; crosses, variables with $P>1$ day in Milky Way globular clusters; small open circles are mean values. Coordinates are visual absolute magnitude $M_{V}$ and $\log P$. Upper line is $M_{V}=-1.70-2.50 \log P$; lower line is $M_{\mathrm{V}}=+0.45-2.50 \log P$.


This gives weight to the idea that they do not lie in the spiral arms but may really belong to the disk population. With both classical Cepheids and "Population II" variables found in M31, it is tempting to try to see whether the W Virginis stars of the Milky Way globular clusters can be fitted to them. For this purpose the absolute magnitudes for the variables of Field IV are listed in Table VI and are plotted as dots and open squares in Fig. 15. Table VII lists the variables with periods greater than a day found in globular clusters of our Milky Way system. The table is based on Arp's material (1955a,b) with the magnitudes adjusted to the $B, V$ system and corrected for cosecant reddening (Arp 1962).
In determining the distance moduli of the clusters, it has been assumed that the absolute magnitudes of the RR Lyrae stars are the same for all systems. An arbitrary zero absolute magnitude was first chosen and the $M_{V}$ 's of the variables were plotted against $\log P$. This graph was then fitted to the Population II variables of Fig. 15 by keeping $\log P$ the same and shifting the magnitudes up and down. There is very little overlap between the periods of the globularcluster variables and those of Population II in Field IV, but the best, though tentative, fit indicates that the absolute magnitude of the RR Lyrae variables is between 0 m 4 and $0 . \mathrm{m}$.

It is probably a coincidence that when the straight line through the Population II variables-drawn parallel to the classical Cepheids-is extended, it passes through $M_{V}=0.45$ at $\log P=0$. It was from these two not completely independent methods that $M_{V}$ $=+0^{\mathrm{m}} \cdot 45$ was derived as the absolute magnitude of the globular-cluster RR Lyrae stars. This value was used to compute the absolute magnitudes of the globularcluster variables with periods over 1 day that are given in the last column of Table VII and are plotted as crosses in Fig. 15. The equation for the extended line, $M_{V}=+0^{\mathrm{m}} \cdot 45-2 \mathrm{~m} \cdot 50 \log P$, gives a slope that fits as well as any for the limited material now available. The classical Cepheids and the Population II variables of M31 and the W Virginis Cepheids of the globular clusters all give the same mean scatter of $\pm 0^{m} \cdot 23$ around the $\mathrm{P}-\mathrm{L}$ slopes, as they are drawn in Fig. 15.

Since the number of variables considered is small, it is not yet possible to say whether the $\mathrm{P}-\mathrm{L}$ relation for the Population II variables is definitely parallel to that for the classical Cepheids and the luminosity difference is constant, or whether there should be a different slope, or even whether there should be a curvature in the $\mathrm{P}-\mathrm{L}$ slope of one or both kinds of variables. However, the material does show that for the variables with periods longer than 16 days the difference between the two populations is $V=2 \mathrm{~m} 15$.


Plate III. Enlargement of a 200 -inch photovisual plate of central area showing stars measured for the color-magnitude diagram. Region of spiral arm indicated.

## 12. $\mathrm{C}-\mathrm{M}$ DIAGRAM

Baade's Field IV is the only field in Andromeda for which a color-magnitude diagram has been attempted,

Table VIII. Plates measured for color-magnitude diagram.

| Plate | Emulsion, Filter | Exposure |  |
| :---: | :---: | :---: | :---: |
| PS 1463-B | $103 \mathrm{a}-\mathrm{D}+$ GG 13 | $30^{\mathrm{m}}$ |  |
| 1477 | $"$ | $"$ | 30 |
| 1488 | $"$ | $"$ | 30 |
| PS 1140-B | $103 \mathrm{a}-\mathrm{D}+\mathrm{GG} \mathrm{11}$ |  |  |
| 1462 | $"$ | $"$ | 90 |
| 1505 | $"$ | $"$ | 60 |

for it is the only field of the four where the star images are not too crowded and there is no bright background to affect the measurements in the iris photometer.
Plate III shows the area that was measured. It has a radius of 5.2 and covers about 85 square minutes of arc. It is the area in which no correction for distance from plate center has had to be made. Plates IV and V are enlargements of the associations that are seen in the spiral arms. The photometry for the color-magnitude diagram was done on the six plates listed in Table VIII, All stars that are free standing, fainter than $V=15^{\mathrm{m}} \cdot 0$. and brighter than $V=22^{\mathrm{m}} \cdot 0$ have been measured. The $B$ limit is $23 \cdot \mathrm{~m} .0$, and about 69 stars were measured that


Plati IV. Three small associations in spiral arm, with stars measured for C-M diagram marked.
are fainter than $B=22^{m} 0$ but have no photovisual magnitudes. As the selection of stars was made primarily on the 103a-O plates, there is not a good count of stars that are redder than $B-V=+1^{\mathrm{m}} 4$ and between $V=21$ and 22 mag., but which would be fainter than $23^{m} \cdot 0$ on the photographic plates.

The color-magnitude diagram of Fig. 16 shows all the stars of Table D and the standard-sequence stars of Table I. It is evidently a combination of stars of M31 and foreground stars. To try to disentangle which stars belong to which system, a star count was made on a 48-inch Schmidt plate (PS 2474, 103a-D, amber filter

Fig. 16. Color-magnitude diagram for Field IV, M31. Includes the 566 stars of Table D and Table I.



Fig. 17. Color-magnitude diagram of 222 stars outside apparent spiral arm in $\mathrm{C}-\mathrm{M}$ area. Symbols for variables are: open circles, cepheids and Population II variables; triangles, eclipsing stars; crosses, irregular variables.

Fig. 18. Color-magnitude diagram of 344 stars in spiral arm as outlined in Plate III. Symbols for variables are the same as in Fig. 17.
and 20 -min exposure). An area was counted that was nine times the size of that for the $\mathrm{C}-\mathrm{M}$ diagram, on a field 1.5 of arc following Field IV, and located on the same relative part of the 48 -inch plate as Field IV.
Field IV was also counted as a check, and the count seemed reasonably close to the count from the C-M diagram. Therefore, in the following discussion, the number of stars for Field IV are taken from the C-M measures.
The stars on the Schmidt plate were counted from $V=15^{\mathrm{m}} 0$ to about the plate limit of $V=19^{\mathrm{m}} .7 \pm 0.1$. For the check field it gave an average of $85 \pm 9$ stars for an area equal in size to the C-M area in Field IV. In Fig. 16 there are 106 stars redder than $+0^{\mathrm{m}} 2$ 2 and brighter than $V=19 \mathrm{~m} 7$. These limits exclude the mainsequence stars of M31 and should correspond to the colors of the stars counted in the outside area. The count indicates that at least $80 \%$ of the stars brighter than $19^{\mathrm{m}} 7$ and redder than 0 m .2 are probable foreground stars, and that there is a fifty-fifty chance that from 0 to $20 \%$ of the stars may be members of M31.

The approximate outline of the sixth spiral arm is shown in Plate III. It is defined by the greater frequency of stars and by the associations. The stars outside this arm have been called "field stars" and are plotted in Fig. 17. They show the faint beginning of the main sequence and the upper part of the giant branch of M31. The frequency of stars brighter than 19 m 7 is about that found for the outside area counted on the Schmidt plate ; therefore it is assumed that most of them belong to the foreground and are members of our Galaxy. In Fig. 18 the distribution of the stars in the spiral arms and the associations are shown. The strength of the main sequence is pronounced. The stars that are brighter than $19^{\mathrm{m}} .7$ and redder than $+0^{\mathrm{m}} 2$ are more frequent per unit area than they are in Fig. 17, indicating that about $15^{ \pm}$stars belong to M31, and of these about half are in the giant branch-particularly the stars that have $B-V=+1^{\mathrm{m}} .8$ and are redder than any in Fig. 17.
Figure 19 shows the distribution of stars in the three small associations, as shown on Plate IV, and Fig. 20


Plate V. Big association in spiral arm, with stars measured for $\mathrm{C}-\mathrm{M}$ diagram marked.
shows the stars in the big, bright association of Plate V. The two figures are similar, but, since the features are more clearly defined in Fig. 20, it has been used as the basis of the following discussion. The main sequence of the bright association can be fitted to the main sequence of h and $\chi$ Persei (Sandage 1957) by shifting M31 blueward by about $0^{\mathrm{m}} 16$, which is the same reddening as found for the Cepheids from the period-color relation (Sec. 6). The two brightest stars in the main sequence have absolute magnitudes between -6 and -7 , which is also like the brightest main sequence stars of $h$ and $\chi$ Persei (Johnson and Hiltner 1956).
Another feature of Fig. 20 is that there are 5 stars clustered around the 17th magnitude with colors about +0 m, and that there are no other stars between the main sequence and the giant branch. An inspection of Fig. 17 of the number of stars brighter than $19^{\mathrm{m}} .7$ and redder than +0 m.2 shows that only one star should be expected in an area the size of the big association; therefore, it possibly suggests that from two to four of these bright stars in Fig. 20 are real members of M31 and do not belong to the foreground. This means that they may be G and K supergiants in the big cluster with absolute magnitudes about -7.5 .

The positions of the variable stars have been indicated in Figs. 17 and 18, the C-M diagrams for the field and spiral arms, respectively. The different kinds of variables are shown with different symbols. It is interesting to note that there does not seem to be a concentration of Cepheids within the apparent spiral arm. Of the 20 Cepheids in Field IV, only 8 lie within the C-M diagram area, and of these only 4 are within the outlined spiral arm. This distribution may differ from that found in the fields closer to the Andromeda nucleus and may be related to period length, but this matter will be discussed in greater detail in a later paper. The Population II variables all lie outside the spiral arm. The eclipsing binaries and irregular variables seem to occur more frequently per number of stars involved within the arms rather than outside, but the variables are few and no definite conclusion should as yet be drawn as to their distribution.

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This paper was written under much the same circumstances as was the "The Draco System" (Baade and Swope 1961). Dr. Baade selected the field and took all the plates and found the variables. Dr. Arp furnished


Fig．19．Color－magnitude diagram of 3 small associa－ tions in spiral arms as shown in Plate IV．

Fig．20．Color－magnitude diagram of big，bright association in spiral arm as shown in Plate V．
the excellent photoelectric sequence，which represents many hours of valuable observing time at the telescope． In addition，much helpful advice was given to me by Drs．Kraft and Sandage and by others of the Observa－ tory Staff．

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Table A. Photographic observations and phases of twenty Cepheids and seven "Population II" variables.

| JD | $\vee 2$ |  | $\vee 3$ |  | $\checkmark 5$ |  | $\checkmark 8$ |  | $\checkmark 9$ |  | $\vee 10$ |  | $\checkmark 11$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2,430,000+ | $B$ | Phase | B | Phase | B | Phase | B | Phase | B | Phase | B | Phase | $B$ | Phase |
| 4184.95 | 21.74 | 42.344 | 21.85 | 14.546 | 21.43 | 14.404 | 20.88 | 19.179 | 21.72 | 21.735 | 22.38 | 60.776 | 21.43 | 62.113 |
| 224.89 | 21.82 | 51.489 | 22.08 | 17.688 | 20.72 | 17.514 | . 59 | 23.321 | . 70 | 26.429 | . 63 | 73.901 | . 82 | 75.527 |
| 243.83 | 22.22 | 55.825 | 20.95 | 19.177 | 21.74 | 18.989 | . 54 | 25.285 | . 77 | 28.655 | 22.42 | 80.125 | . 57 | 81.888 |
| 244.84 | 21.51 | 50.056 | 21.06 | . 256 | . 90 | 19.068 | 20.95 | . 390 | 21.54 | . 774 | 21.88 | . 457 | . 65 | 82.227 |
| 245.84 | . 66 | . 285 | . 40 | . 335 | . 90 | . 146 | 21.25 | . 494 | 20.90 | . 891 | 22.41 | . 786 | . 94 | . 563 |
| . 90 | . 63 | . 299 | . 46 | . 340 | . 96 | . 151 | . 26 | . 500 | . 89 | . 897 | . 53 | . 805 | . 83 | . 583 |
| 246.81 | . 95 | . 507 | . 57 | . 411 | 21.76 | . 222 | . 35 | . 594 | 20.82 | 29.005 | . 60 | 81.105 | . 69 | . 889 |
| 277.75 | 21.99 | 63.591 | 21.23 | 21.844 | 20.78 | 21.631 | . 94 | 28.803 | 21.60 | 32.641 | . 45 | 91.271 | . 62 | 93.279 |
| 304.70 | 22.03 | 69.761 | 20.62 | 23.965 | 21.08 | 23.730 | . 09 | 31.597 | 21.39 | 35.807 | 22.30 | 100.127 | . 76 | 102.330 |
| 305.66 | . 08 | . 981 | . 39 | 24.040 | . 32 | . 805 | 21.71 | . 697 | 20.86 | . 920 | 21.81 | . 443 | . 87 | . 652 |
| 330.70* | 22.20 | 80.714 | 20.40 | 26.010 | 21.25: | 25.760 | 20.70 | 34.293 | 20.90 | 38.864 | - | - | . 40 | 111.052 |
| 334.64 | 21.98 | 81.616 | 21.40 | . 320 | 22.01 | 26.032 | 21.68 | . 702 | 21.46 | 39.327 | 22.34 | 109.966 | . 84 | 112.385 |
| 360.61 | 21.95 | 82.562 | . 33 | 28.362 | 21.82 | 28.084 | . 09 | 37.395 | . 51 | 42.379 | 21.85 | 118.500 | . 45 | 121.107 |
| 361.61 | 22.16 | . 791 | 21.67 | . 441 | . 81 | . 162 | . 33 | . 499 | . 77 | . 496 | 22.44 | . 829 | . 81 | . 443 |
| 362.67 | 21.70 | 83.033 | 22.06 | . 524 | 21.97 | . 245 | 21.75 | . 609 | 21.88 | . 621 | 22.40 | 119.177 | 21.74 | . 799 |
| 4596.91 | 21.99 | 136.663 | 20.85 | 46.948 | 20.82 | 46.487 | 21.70 | 61.900 | 21.08 | 70.149 | 22.55 | 196.150 | 21.80 | 200.466 |
| 597.88 | 22.08 | . 885 | . 62 | 47.024 | . 72 | . 563 | 20.76 | 62.000 | . 33 | . 263 | 21.86 | . 468 | . 70 | . 792 |
| 598.88 | 21.08 | 137.114 | . 69 | . 103 | . 83 | . 640 | . 68 | . 104 | . 54 | . 380 | 22.28 | . 797 | . 46 | 201.128 |
| 599.87 | 21.77 | . 340 | 20.95 | . 181 | 20.98 | . 717 | . 85 | . 206 | . 70 | . 497 | 22.38 | 197.122 | . 96 | . 460 |
| 600.88 | 21.99 | . 571 | 21.17 | . 260 | 21.43 | . 796 | . 90 | . 311 | . 88 | . 615 | 21.88 | . 454 | . 74 | .79\% |
| 601.96 | 22.29 | . 819 | . 30 | . 345 | . 48 | . 881 | 20.87 | . 423 | . 55 | . 742 | 22.38 | . 809 | . 38 | 202. 162 |
| 602.88* | 21.77 | 138.029 | 21.50 | . 417 | . 60 | . 952 | 21.15 | . 519 | . 05 | . 850 | . 40 | 198.112 | . 75 | . 471 |
| 625.77* | . 51 | 143.270 | 20.95 | 49.217 | . 04 : | 48.735 | . 80 | 64.892 | . 80 | 73.540 | . 28 | 205.634 | . 55 | 210.158 |
| . 89 | . 55 | . 297 | 21.08 | . 227 | . 16 | . 744 | 21.50: | . 905 | . 82 | . 554 | . 40 | . 673 | . 37 | . 198 |
| 626.77 | . 93 | . 499 | . 15 | . 296 | . 41 | . 813 | 20.98 | . 996 | . 69 | . 658 | . 60 | . 962 | . 88 | . 494 |
| .87* | 21.90 | . 522 | . 20 | . 304 | . 43 | . 820 | . 80 | 65.006 | . 70 | . 670 | . 63 | . 996 | . 90 | . 527 |
| 627.76 | 22.08 | . 726 | . 67 | . 374 | . 54 | . 890 | . 74 | . 099 | 21.55 | . 774 | . 22 | 206.288 | - | - |
| 628.91 | 21.89 | . 989 | . 72 | . 464 | 21.90 | . 978 | . 61 | . 218 | 20.86 | . 909 | . 55 | . 666 | . 67 | 211.212 |
| 629.76 | . 35 | 144. 183 | . 93 | . 531 | 22.00 | 49.046 | 20.46 | . 306 | . 69 | 74.009 | . 48 | . 945 | . 80 | . 498 |
| 630.78 | . 79 | . 417 | . 83 | . 611 | 22.14 | . 125 | 21.09 | . 412 | 20.98 | . 130 | . 50 | 207.281 | . 64 | . 840 |
| 633.76 | . 21 | 145.099 | . 54 | . 340 | 21.50 | . 357 | . 54 | . 721 | 21.65 | . 480 | . 47 | 208.260 | . 72 | 212.840 |
| 634.85 | . 59 | . 349 | 21.34 | . 931 | . 33 | . 442 | . 68 | . 834 | . 84 | . 608 | . 28 | . 618 | . 53 | 213.208 |
| 660.75 | 21.57 | 151.279 | 20.44 | 51.969 | . 04 | 51.459 | . 16 | 68.520 | 21.77 | 77.651 | . 55 | 217.129 | . 60 | 221.906 |
| 663.80 | 22.00 | . 977 | 20.95 | 52.209 | . 00 | . 697 | . 57 | . 836 | 20.84 | 78.010 | . 48 | 218.138 | . 58 | 222.530 |
| 680.64 | 22.35 | 155.832 | 21.96 | 53.533 | 21.84 | 53.009 | . 09 | 70.582 | 20.81 | 79.989 | . 29 | 223.665 | . 94 | 228.585 |
| 681.69 | 21.32 | 156.073 | . 96 | . 615 | 22.00 | . 091 | . ${ }^{2}$ | . 691 | 21.10 | 80.112 | . 68 | 224.010 | . 60 | . 938 |
| 682.66 | 21.56 | . 295 | 21.90 | . 692 | 21.84 | . 10 6 | 21.57 | . 792 | 21.16 | . 226 | . 03 | . 329 | . 65 | 229.264 |
| 714.65* | 22.11 | 163.619 | 20.90 | 56.208 | . 00 | 55.657 | 20.80 | 74.109 | 20.75 | 83.986 | - | - | . 35 | 240.007 |
| 717.61 | 21.57 | 164.297 | 21.76 | . 441 | . 69 | . 888 | 21.09 | . 416 | 21.33 | 84.333 | . 65 | 235.814 | . 54 | 241.001 |
| 718.62 | 21.58 | . 528 | 21.84 | . 520 | 21.70 | . 966 | 21.22 | . 521 | 21.77 | . 452 | 22.53 | 236.146 | 21.70 | . 340 |
| 4923.95 | 22.06 | 211.538 | 21.84 | 72.670 | 21.68 | 71.957 | 21.62 | 95.814 | 21.78 | 108.582 | 22.20 | 303.619 | 21.69 | 310.298 |
| 924.95 | 22.25 | . 767 | . 86 | . 749 | 21.91 | 72.035 | 21.68 | . 917 | . 90 | . 700 | . 65 | . 948 | . 80 | . 634 |
| 925.95 | 21.93 | . 996 | . 42 | . 828 | 22.01 | . 113 | 20.95 | 96.021 | 21.21 | . 817 | . 49 | 304.276 | . 49 | . 970 |
| 926.95 | . 49 | 212.225 | 21.62 | . 906 | 21.86 | . 191 | . 76 | . 125 | 20.80 | . 935 | . 20 | . 605 | . 72 | 311.306 |
| 927.95* | 21.83 | . 454 | 20.40 | . 984 | . 75 | . 269 | - | - | 20.90 | 109.053 | - | - | . 85 | . 642 |
| 928.95 | 22.10 | . 683 | . 63 | 73.063 | . 41 | . 347 | . 71 | . 332 | 21.11 | . 170 | . 27 | 305.262 | . 50 | . 978 |
| 929.95 | 22.36 | . 912 | 20.81 | . 141 | 21.29 | . 425 | 20.83 | . 436 | . 29 | . 287 | . 16 | . 591 | . 62 | 312.313 |
| 930.95 | 21.23 | 213.141 | 21.11 | . 220 | 20.70 | . 503 | 21.25 | . 540 | . 62 | . 405 | . 46 | . 19 | . 74 | . 650 |
| 931.94 | 21.75 | . 368 | . 25 | . 298 | . 84 | . 580 | . 40 | . 642 | . 60 | . 521 | . 50 | 306.245 | . 44 | . 981 |
| 932.96 | 22.11 | . 601 | 21.50 | . 378 | 20.93 | . 659 | 21.67 | . 748 | . 80 | . 640 | . 33 | . 580 | . 76 | 313.324 |
| 954.97 | 21.92 | 218.640 | 20.81 | 75.109 | 21.27 | 74.373 | 20.84 | 99.030 | . 25 | 112.227 | . 34 | 313.813 | . 78 | 320.716 |
| 979.83* | . 78 | 224.332 | . 50 | 77.065 | . 45 : | 76.310 | 21.50 | 101.608 | . $05{ }^{\text {: }}$ | 115.150 | - | - | . 35 | 329.065 |
| 980.89* | 21.91 | . 575 | 20.80 | . 148 | . 32 | . 392 | . 70 | . 718 | . 20 | . 274 | - | - | . 80 | . 421 |
| 981.88 | 22.07 | . 801 | 21.11 | . 226 | 21.10 | . 470 | 21.54 | . 821 | . 48 | . 390 | . 32 | 322.656 | . 78 | . 754 |
| 983.86 | 21.51 | 225.255 | , | - | 20.78 | . 624 | 20.74 | 102.026 | . 82 | . 622 | . 18 | 323.306 | . 76 | 330.419 |
| 984.92 | 21.96 | . 497 | . 72 | . 465 | 20.97 | . 706 | . 76 | . 136 | . 65 | . 748 | . 29 | . 657 | . 76 | . 775 |
| 985.86 | 22. 15 | . 713 | . 88 | . 539 | 21.23 | . 780 | . 61 | . 234 | . 15 | . 858 | . 53 | . 964 | . 54 | 331.090 |
| . 98 | 22.15 | . 740 | 21.90 | . 549 | . 25 | . 790 | 20.64 | . 246 | . 11 | . 873 | . 53 | 324.003 | . 56 | . 131 |
| 5006.79 | 21.88 | 230.504 | 20.95 | 79.185 | 21.37 | 78.409 | 21.07 | 104.404 | . 31 | 118.318 | . 57 | 330.841 | . 61 | 338.119 |
| 007.81 | 22. 15 | . 738 | 21.21 | . 265 | 20.80 | . 488 | . 15 | . 510 | . 55 | . 438 | 22.63 | 331.176 | . 86 | . 462 |
| 008.79 | 22.22 | . 962 | . 43 | . 343 | . 69 | . 565 | . 39 | . 612 | . 92 | . 553 | 21.94 | . 499 | . 74 | . 791 |
| 009.74 | 21.30 | 231.180 | . 48 | . 417 | . 90 | . 639 | . 60 | . 710 | . 70 | . 664 | 22.48 | . 811 | . 53 | 339.110 |
| . 82 | . 38 | . 198 | . 62 | . 424 | 20.88 | . 645 | . 62 | . 718 | . 82 | . 674 | . 48 | . 837 | . 48 | . 137 |
| 010.76 | 21.88 | . 413 | . 70 | . 498 | 21.00 | . 719 | . 65 | . 816 | 21.50 | . 784 | 22.53 | 332.146 | - | - |
| 011.79 | 22.03 | . 649 | . 86 | . 578 | 21.34 | . 799 | . 35 | . 922 | 20.94 | . 905 | 21.97 | . 485 | . 82 | . 798 |
| 035.74 | 21.23 | 237.133 | . 70 | 81.462 | 20.98 | 80.663 | . 04 | 107.406 | 21.82 | 121.720 | 21.95 | 340.354 | . 78 | 347.842 |
| 036.87 | . 75 | . 391 | . 82 | . 551 | 21.16 | . 751 | . 28 | . 523 | 21.05 | . 853 | 22.42 | . 726 | . 49 | 348.222 |
| 037.70 | . 98 | . 581 | 21.85 | . 617 | . 39 | . 816 | . 50 | . 609 | 20.70 | . 951 | . 54 | . 999 | . 90 | . 500 |
| . 84 | 22.00 | . 613 | 22.00 | . 627 | . 39 | . 827 | . 48 | . 624 | . 76 | . 967 | . 46 | 341.045 | . 88 | . 547 |
| 038.70 | 22.15 | . 810 | 22.02 | . 695 | . 56 | . 894 | . 56 | . 713 | 20.94 | 122.068 | . 20 | . 328 | . 68 | . 836 |
| 064.63 | . 10 | 243.747 | 21.96 | 83.734 | . 67 | 82.914 | . 20 | 110.402 | 21.02 | 125.115 | . 63 | 349.848 | . 87 | 357.544 |
| 065.63 | 22.06 | . 976 | . 44 | . 813 | . 71 | . 992 | . 23 | . 506 | . 19 | . 232 | . 68 | 350.176 | . 78 | . 880 |
| 066.63 | 21.39 | 244.205 | 21.48 | . 892 | . 92 | 83.070 | . 62 | . 610 | . 41 | . 350 | . 12 | . 505 | . 58 | 353.216 |
| 067.62 | 21.86 | . 432 | 20.45 | . 970 | . 93 | . 147 | . 76 | . 712 | . 67 | . 467 | . 40 | . 830 | . 85 | . 549 |
| 068.62 | 22.16 | . 661 | . 39 | 84.049 | . 84 | . 224 | . 67 | . 816 | . 86 | . 584 | 22.55: | 351. 159 | . 70 | . 884 |
| 069.62 | . 22 | . 889 | . 75 | . 127 | . 59 | . 302 | . 46 | . 919 | . 65 | . 702 | 21.94 | . 488 | . 59 | 359.220 |
| . 81 | 22.37 | . 933 | 20.84 | . 142 | 21.54 | . 317 | . 25 | . 939 | 21.58 | . 724 | 22.19 | . 550 | . 60 | . 284 |
| 097.63 | 21.62 | 251.302 | 21.28 | 86.330 | 20.97 | 85.483 | . 66 | 113.824 | 20.86 | 128.993 | . 34 | 360.692 | . 91 | 368.627 |
| . 76 | . 59 | . 332 | . 33 | . 340 | . 78 | . 493 | . 66 | . 838 | 20.81 | 129.009 | . 40 | . 735 | . 88 | . 670 |
| 098.64 | 21.93 | . 534 | . 59 | . 408 | . 64 | . 562 | 21.17 | . 929 | 21.05 | . 112 | 22.54 | 361.024 | . 51 | . 966 |
| 099.66 | 22.04 | . 767 | 21.80 | . 487 | 20.95 | . 641 | 20.85 | 114.035 | . 15 | . 232 | 21.82 | . 359 | 21.59 | 369.309 |
| 100.68 | 22.00 | 252.001 | 22.02 | . 569 | 21.09 | . 721 | 20.84 | . 140 | 21.56 | . 352 | 22.32 | . 695 | 22.04 | . 651 |

Table A (continued)

|  | $\checkmark 2$ |  | $\vee 3$ |  | $\checkmark 5$ |  | $\vee 8$ |  | $\checkmark 9$ |  | $\checkmark 10$ |  | $\vee 11$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $2,430,000$ | B | Phase | B | Phase | B | Phase | B | Phase | B | Phase | B | Phase | B | Phase |
| 5342.82 | 21.90 | 3.97 .439 | 22.16 | 105.614 | 20.66 | 104.579 | 20.61 | 139.250 | 21.42 | 157.808 | 22.48 | 440.264 | 21.53 | 450.971 |
| 370.89 | 22.29 | 313.865 | 21.46 | 107.822 | 21.20 | 106.765 | . 78 | 142.161 | . 00 | 161.107 | . 65 | 450.488 | . 7 | 460.398 |
| 371.74 | 21.46 | 314.060 | - | - | . 46 | . 831 | . 65 | . 249 | - | - | . 48 | . 767 | . 91 | . 684 |
| . 88 | . 23 | . 092 | 21.52 | . 900 | . 45 | . 842 | . 68 | . 264 | . 07 | . 223 | . 49 | . 813 | . 90 | . 730 |
| 372.76 | . 60 | . 293 | - | - | . 53 | . 910 | . 94 | . 355 | . 23 | . 327 | . 47 | 451.103 | . 46 | 461.026 |
| 373.94 | . 90 | . 564 | - | - | 21.74 | 107.002 | 20.98: | . 478 | - | - | . 10 | . 490 | . 78 | . 423 |
| 394.69 | 21.78 | 319.314 | 22.15: | 109.694 | 20.85 | 108.618 | 21.49 | 144.629 | 21.02 | 163.904 | . 00 | 458.309 | . 70 | 468.391 |
| 395.77 | 22.04 | . 562 | 21.67 | . 780 | 21.05 | . 703 | . 70 | . 741 | 20.78 | 164.031 | . 40 | . 664 | . 99 | . 754 |
| . 94 | 21.90 | . 600 | . 50 | . 792 | . 13 | . 716 | . 88 | . 759 | 21.03 | . 051 | . 38 | . 720 | . 80 | . 811 |
| 396.68 | 22.16 | . 770 | . 38 | . 851 | . 26 | . 773 | . 58 : | . 835 | . 11 | . 138 | . 70 | . 963 | . 40 | 469.060 |
| . 84 | - | - | - | - | . 25 | . 786 | - | - | - | - | 22.53 | 459.016 | . 41 | . 113 |
| 397.90 | 21.71 | 320.049 | . 00 | . 946 | . 43 | . 868 | . 10 | . 962 | 21.28 | . 282 | 21.70 | . 364 | . 85 | . 469 |
| 403.84* | 21.86 | 321.409 | 21.50 | 110.413 | 21.40 | 109.331 | 21.39 | 145.578 | 20.70 | . 979 | - | - | - | - |
| 426.83* | 22.03 | 326.673 | 20.90 | 112.222 | 22.00 | 111.122 | 20.98 | 147.962 | 21.65 | 167.681 | - | - 711 | - | - |
| 450.69 | 21.35 | 332.135 | 20.66 | 114.098 | 21.93 | 113.980 | 21.03 | 150.437 | 21.70 | 170.485 | 22.45 | 476.711 | 21.57 | 487.198 |
| 5690.94 | 21.23 | 387.141 | 20.37 | 132.994 | 21.04 | 131.691 | 20.97 | 175.350 | 21.70 | 198.719 | 22.40: | 555.660 | 21.70 | 567.883 |
| 692.88 | 22.07 | . 585 | 20.75 | 133.147 | . 26 | . 841 | 21.35 | . 550 | 20.85 | . 947 | . 34 | 556.297 | . 92 | 568.535 |
| 693.88 | . 16 | . 814 | 21.00 | . 226 | 21.47 | . 920 | . 50 | . 655 | 21.00 | 199.065 | . 20 | . 626 | . 80 | . 871 |
| 715.78 | 22.24 | 392.828 | 20.80 | 134.948 | 20.75 | 135.625 | . 40 | 177.926 | . 85 | 201.638 | . 65 | 563.822 | .61 | 576.226 |
| 716.77 | 21.60 | 393.054 | . 55 | 135.026 | 21.04 | . 702 | 20.75 | 178.029 | . 52 | . 755 | . 55 | 564.148 | . 94 | . 558 |
| 717.79 | . 64 | . 288 | 20.63 | . 106 | . 22 | . 781 | . 80 | . 135 | 21.07 | . 875 | . 05 | . 483 | . 60 | . 901 |
| 718.77 | . 95 : | . 512 | 21.00 | . 183 | . 32 | . 858 | 20.65 | . 236 | 20.80 | . 990 | . 50 | . 805 | . 56 | 577.230 |
| 719.8:0 | . 95 : | . 749 | . 05 | . 264 | . 54 | . 938 | 21.05 | . 343 | 21.10 | 202.112 | 22.75 | 565.143 | . 91 | . 576 |
| 808. 18 | 21.09 | 419.120 | 21.00 | 142.262 | 21.47 | 140.867 | 21.50 | 187.570 | 21.90: | 212.567 | 21.80 | 594.383 | 21.85 | 607.459 |
|  | V I3 |  | V $15^{*}$ |  | $\vee 16 *$ |  | $\vee 17$ |  | $\vee 21$ |  | $\checkmark$ 26* |  | $\vee 27$ |  |
| 4184.95 | 22.68 | 48.633 | 19.90 | 8.698 | 22.40 | 73.578 | 22.06 | 27.474 | 22.20 | 55.246 | 21.76 | 46.881 | 21.82 | 71.332 |
| 224.89 | . 46 | 59.135 | 21.20 | 10.576 | . 73 | 89.468 | . 58 | 33.407 | . 02 | 67.177 | 21.74 | 56.005 | 22.68 | 86.735 |
| 243.83 | . 39 | 64.115 | . 35 | 11.467 | . 73 | 97.003 | . 12 | 36.221 | 22.65 | 72.834 | 22.06 | 61.806 | . 60 | 94.040 |
| 244.84 | . 98 | . 381 | . 40 | . 514 | . 78 | . 405 | . 14 | . 371 | 21.99 | 73.136 | . 16 | 62.062 | . 12 | . 430 |
| 245.84 | . 85 | . 644 | . 26 | . 561 | . 53 | . 802 | . 14 | . 519 | 22.38 | . 434 | . 12 | . 315 | . 54 | . 815 |
| . 90 | . 84 | . 660 | . 23 | . 563 | . 53 | . 826 | 22.22 | . 528 | . 55 | . 452 | . 28 | . 330 | . 48 | . 838 |
| 246.81 | . 04 | . 899 | 21.46 | . 608 | . 73 | 98.188 | 21.35 | . 664 | 22.58 | . 724 | . 32 | . 561 | . 43 | 95.189 |
| 277.75 | . 16 | 73.034 | 20.93 | 13.062 | - | - | 22.26 | 41.260 | 21.88 | 82.967 | - | -- | . 63 | 107.123 |
| 304. 0 | . 36 | 80.121 | 21.15 | 14.330 | - | - | . 28 | 45.263 | 21.60 | 91.017 | . 28 | 77.235 | . 10 | 117.517 |
| 305.66 | . 80 | . 373 | . 50 | . 376 | . 20 | 121.601 | . 40 | . 406 | 22.44 | . 304 | 22.32 | . 479 | . 85 | . 888 |
| 330.70* | . 20 | 86.957 | 21.50 | 15.553 | . 24 | 131.562 | 22.10 | 49.125 | 22.73 | 98.783 | 21.76 | 83.826 | . 31 | 127.544 |
| 334.64 | . 21 | 87.993 | 19.85 | . 738 | - | - | 21.30 | . 711 | 21.69 | 99.960 | 21.92 | 84.825 | . 57 | 129.064 |
| 360.61 | . 70 | 94.822 | 20.65 | 16.959 | . 73 | 143.461 | . 76 | 53.569 | 22.44 | 107.718 | 22.32 | 91.407 | . 58 | 139.080 |
| 361.61 | . 29 | 95.085 | . 75 | 17.006 | 22.58 | . 859 | . 30 | . 717 | 21.71 | 108.017 | . 32 | . 661 | . 21 | . 466 |
| 362.067 | 22.77 | . 364 | 20.70 | . 053 | - | - | 21.52 | . 878 | 22.58 | . 333 | 22.04 | . 930 | 22.55 | . 874 |
| 4596.91 | 22.07 | 156.957 | 20.80 | 28.073 | 22.63 | 237.469 | 21.23 | 88.671 | 22.30 | 178.303 | - | - | 22.26 | 230.216 |
| 597.88 | . 68 | 157.212 | 20.90 | . 118 | . 68 | . 855 | . 55 | . 815 | . 50 | . 593 | 22.20 | 151.551 | . 38 | . 590 |
| 598.88 | . 98 | . 474 | 21.11 | . 165 | . 68 | 238.252 | . 88 | . 964 | 22.24 | . 891 | . 00 | . 804 | 22.60 | . 976 |
| 599.37 | . 59 | . 735 | . 11 | . 213 | . 16 | . 646 | 21.99 | 89.111 | 21.98: | 179.191 | . 14 | 152.055 | 21.92 | 231.358 |
| 600.38 | . 25 | 158.000 | . 30 | . 260 | . 58 | 239.048 | 22.18 | . 261 | 22.50 | . 489 | . 24 | . 311 | 22.51 | . 747 |
| 601.96 | . 80 | . 284 | . 40 | . 309 | . 44 | . 478 | . 12 | . 421 | 22.58 | .811 | 22.32 | . 585 | . 38 | 232.164 |
| 602.88* | . 73 | . 527 | . 26 | . 354 | . 63 | . 844 | 22.00 | . 558 | 21.88 | 180.086 | 21.76 | . 818 | 22.14: | . 519 |
| 625.77* | . 83 | 164.546 | . 40 | 29.430 | - | - | 21.70 | 92.958 | . 95 | 186.924 | 22.36 | 158.620 | 21.85 | 241.347 |
| . 39 | . 82 | . 578 | . 50 | . 436 | . 73 | 248.998 | . 85 | . 976 | 21.62 | . 960 | 22.40 | . 650 | 22.04 | . 393 |
| 626.77 | . 74 | . 809 | . 46 | . 477 | (22.7 | 249.348 | 21.94 | 93.107 | 22.20 | 187.223 | 21.58 | . 873 | . 48 | . 733 |
| . $87 *$ | . 60 | . 835 | . 50 | . 482 | (22.7 | . 388 | 22.00 | . 121 | . 28 | . 252 | 21.60 | . 898 | . 55 | . 772 |
| 627.76 | . 49 | 165.069 | . 30 | . 524 | - | - | . 38 | . 254 | . 36 | . 518 | - | - | . 45 | 242.114 |
| 628.91 | . 70 | . 372 | . 35 | . 578 | 22.63 | 250. 199 | 22.22 | . 424 | 22.50 | . 862 | 22.38 | 159.416 | . 28 | . 557 |
| 629.76 | . 95 | . 595 | 21.46 | . 617 | . 36 | . 537 | 21.82 | . 551 | 21.94 | 188.116 | 22.42 | . 631 | 22.70 | . 885 |
| 630.78 | . 24 | . 863 | 20.63 | . 665 | - | - | 21.23 | . 702 | 22.53 | . 420 | 21.88 | . 890 | 21.88 | 243.279 |
| 633.76 | . 68 | 166.647 | . 05 | . 805 | ( 22.8 | 252.129 | 22.06 | 94.145 | . 20 | 189.310 | - | - | 22.24 | 244.428 |
| 634.85 | . 38 | . 933 | . 14 | . 856 | 22.36 | . 562 | 22.42 | . 307 | . 60 | . 636 | 21.70 | 160.922 | . 58 | . 848 |
| 660.75 | . 73 | 173.744 | 20.71 | 31.075 | . 53 | 262.866 | 21.98 | 98.154 | . 40 | 197.373 | 22.20 | 167.487 | . 60 | 254.838 |
| 663.80 | . 75 | 174.546 | 21.30 | . 218 | ( 22.7 | 264.079 | . 62 | . 607 | . 26 | 198.284 | . 20 | 168.260 | . 80 | 255.014 |
| 680.64 | . 15 | 178.974 | 20.84 | 32.010 | 22.63 | 270.779 | 21.98 | 101. 109 | . 40 | 203.314 | . 36 | 172.529 | . 22 | 262.509 |
| 681.69 | . 66 | 179.250 | 20.75 | . 060 | . 73 | 271.197 | 22. 10 | . 265 | . 60 | . 628 | 22.02 | . 795 | 22.60 | . 914 |
| 682.66 | 22.75 | . 505 | 21.19 | . 105 | . 28 | . 582 | 22.26 | . 409 | . 00 | . 918 | 21.99 | 173.041 | 21.84 | 263.288 |
| 714.65* | 21.95 | 187.917 | 21.30 | 33.610 | - | - | - | - | - | - | 22.10 | 181. 149 | 22.50 | 275.626 |
| 717.61 | 22.89 | 188.695 | 19.71 | . 749 | . 44 | 285.487 | 21.68 | 106.601 | . 48 | 214.357 | 21.72 | . 900 | . 78 | 276.768 |
| 718.62 | 21.94 | . 961 | 19.85 | . 796 | 22.63 | . 858 | 21.26 | . 751 | 22.68 | . 659 | 22.16 | 182. 155 | 22.63 | 277.157 |
| 4923.95 | 22.20 | 242.953 | 21.40 | 43.453 | 22.20 | 367.575 | 22.24 | 137.253 | 21.64 | 275.993 | 22.05 | 234.203 | 22.04 | 356.349 |
| 924.95 | . 75 | 243.216 | . 23 | . 500 | - | - | 22.50 | . 401 | 22.60: | 276.292 | . 36 | . 456 | . 69 | . 735 |
| 925.95 | . 93 | . 479 | . 50 | . 547 | . 73 | 368.371 | 21.86 | . 550 | . 60 | . 590 | 22.34 | . 710 | . 42 | 357.120 |
| 926.95 | . 83 | . 742 | . 30 | . 594 | . 63 | . 768 | . 13 | . 698 | . 36 | . 889 | 21.98 | . 963 | . 30 | . 506 |
| 927.95* | . 10 | 244.004 | 21.20 | . 641 | - | - | . 35 | . 847 | . 08: | 277. 188 | 22.24 | 235.217 | 22.70 | . 892 |
| 928.95 | . 76 | . 267 | 20.45 | . 688 | . 28 | 369.564 | 21.94 | . 995 | . 53 | . 487 | . 34 | . 470 | 21.92 | 358.277 |
| 92995 | . 88 | . 530 | 19.77 | . 735 | . 68 | . 962 | 22.06 | 138.144 | 22.55 | . 785 | (22.4 | . 724 | 22.40 | . 663 |
| 93095 | . 87 | . 793 | . 77 | . 782 | (22.7 | 370.360 | . 34 | . 293 | 21.78 | 278.084 | 21.92 | . 977 | 22.58 | 359.048 |
| 93194 | . 28 | 245.053 | . 85 | . 829 | 22.63 | . 754 | 22.48 | . 440 | 22.20 | . 380 | 22.24 | 236.228 | 21.96 | . 430 |
| 932.96 | . 58 | . 322 | 19.94 | . 877 | - | - | 21.78 | . 591 | . 73 | . 684 | . 36 | . 486 | 22.68 | . 823 |
| 954.97 | . 22 | 251.109 | 20.05 | 44.911 | . 48 | 379.916 | . 52 | 141.861 | . 16 | 285.259 | . 34 | 241.066 | 21.65 | 368.313 |
| 979.83* | . 73 | 257.646 | 20.90 | 46.081 | 22.58 | 389.806 | . 80 | 145.554 | 22.73 | 292.685 | 22.32 | 248.367 | 22.60: | 377.901 |
| 980.89* | 22.16 | . 925 | 21.10 | . 131 | - | - | 21.30 | . 711 | 21.55 | 293.002 | - | - | 21.75: | 378.310 |

Table A (continued)

| JD | $\vee 13$ |  | V 15* |  | $\checkmark 16^{*}$ |  | V 17 |  | $\vee 21$ |  | $\checkmark 26$ * |  | V 27 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2,430,000+ | B | Phase | B | Phase | B | Phase | B | Phase | B | Phase | B | Phase | B | Phase |
| 4981.88 | 22.49 | 258. 185 | 21.30 | 46.178 | 22.28 | 390.621 | 21.58 | 145.858 | 22.63 | 293.297 | 21.84 | 248.887 | 22.40 | 378.691 |
| 983.86 | . 90 | . 706 | . 39 | . 271 | . 83 | 391.409 | 22.10 | 146.152 | . 28 | . 887 | 22.46 | 249.389 | . 20 | 379.455 |
| 984.92 | . 22 | . 985 | . 26 | . 319 | . 53 | . 831 | . 20 | . 310 | . 20 | 294.205 | 22.28 | . 657 | . 63 | . 864 |
| 985.86 | . 60 | 259.232 | . 40 | . 365 | (22.7 | 392.205 | . 34 | . 449 | . 55 | . 486 | 21.80 | . 896 | 22.14 | 380.226 |
| . 98 | . 54 | . 263 | . 40 | . 371 | 22.73 | . 253 | 22.33 | . 466 | . 50 | . 521 | . 84 | . 926 | 21.98 | . 272 |
| 5006.79 | . 78 | 264.735 | . 28 | 47.349 | . 16 | 400.531 | 21.84 | 149.559 | 22.80 | 300.738 | 21.98 | 255.201 | 21.88 | 388.299 |
| 007.81 | . 30 | 265.003 | . 19 | . 396 | . 53 | . 937 | . 23 | . 710 | 21.75 | 301.042 | 22.30 | . 459 | 22.60 | . 693 |
| 008.79 | . 58 | . 261 | . 39 | . 443 | . 68 | 401.327 | . 64 | . 856 | 22.42 | . 335 | 22.34 | . 707 | . 52 | 389.071 |
| 009.74 | . 73 | . 511 | . 45 | . 488 | . 58 | . 705 | . 88 | . 997 | - | - | 21.84 | . 948 | . 02 | . 436 |
| . 82 | . 95 | . 531 | . 39 | . 492 | . 44 | . 736 | 21.94 | 150.009 | 22.81 | . 643 | 21.86 | . 968 | . 30 | . 468 |
| 010.76 | . 73 | . 778 | . 35 | . 536 | . 73 | 402.111 | 22.02 | . 148 | 21.92 | . 924 | 22.30 | 256.207 | . 80 | . 830 |
| 011.79 | . 24 | 266.049 | 21.25 | . 584 | . 24 | . 520 | 22.27 | . 301 | 22.25 | 302.232 | . 30 | . 468 | . 16 | 390.227 |
| 035.74 | . 85 | 272.348 | 19.89 | 48.711 | . 68 | 412.048 | 21.55 | 153.859 | . 32 | 309.386 | 22.30 | 262.539 | . 16 | 399.464 |
| 036.87 | . 89 | . 645 | . 83 | . 764 | . 53 | . 498 | 22.02 | 154.027 | 22.65 | . 723 | 21.80 | . 826 | . 61 | . 900 |
| 037.70 | . 30 | . 864 | . 91 | . 803 | . 58 | . 828 | . 13 | . 150 | 21.64 | . 971 | 22.00 | 263.036 | 22.20 | 400.220 |
| . 84 | . 10 | . 900 | 19.89 | . 809 | . 68 | . 884 | . 10 | . 171 | 21.58 | 310.013 | . 02 | . 072 | 21.78 | . 274 |
| 038.70 | . 42 | 273.126 | 20.08 | . 850 | (22.7 | 413.226 | . 26 | . 299 | 22.28 | . 270 | 22.24 | . 290 | 22.48 | . 606 |
| 064.63 | . 06 | 279.944 | . 57 | 50.069 | 22.28 | 423.542 | . 06 | 158.151 | 21.78 | 318.016 | 21.78 | 269.862 | . 48 | 410.606 |
| 065.63 | . 63 | 280.207 | 20.96 | . 116 | . 48 | . 939 | . 25 | . 299 | 22.34 | . 314 | 22.12 | 270.116 | 22.73 | . 992 |
| 066.63 | . 85 | . 470 | 21.19 | . 164 | . 78 | 424.337 | 22.45 | . 448 | . 63 | . 613 | . 36 | . 369 | 21.96 | 411.377 |
| 067.62 | . 93 | . 730 | . 23 | . 210 | . 58 | . 731 | 21.58 | . 595 | . 02 | . 909 | 22.32 | . 620 | 22.42 | . 759 |
| 068.62 | . 12 | . 994 | . 27 | . 257 | . 78 | 425.129 | . 30 | . 743 | . 16 | 319.207 | 21.91 | . 874 | . 68 | 412.145 |
| 069.62 | . 65 | 281.257 | . 26 | . 304 | . 36 | . 527 | . 57 | . 893 | . 48 | . 506 | 22.24 | 271.127 | . 43 | . 531 |
| . 81 | . 80 | . 307 | . 30 | . 314 | . 16 | . 603 | 21.67 | . 921 | . 42 | . 563 | . 08 | . 175 | . 34 | . 604 |
| 097.63 | . 83 | 288.622 | . 42 | 51.621 | . 28 | 436.670 | 22.13 | 162.053 | . 35 | 327.873 | . 32 | 278.227 | . 00 | 423.334 |
| . 76 | . 83 | . 656 | 21.30 | . 627 | . 53 | . 722 | . 12 | . 072 | . 03 | . 912 | . 30 | . 260 | . 00 | . 384 |
| 098.64 | . 12 | . 887 | 20.64 | . 669 | . 83 | 437.072 | . 17 | . 203 | . 02 | 328.175 | . 28 | . 463 | . 59 | . 723 |
| 099.66 | . 40 | 289.156 | 19.80 | . 716 | . 63 | . 478 | . 29 | . 354 | . 44 | . 479 | . 22 | . 742 | . 57 | 424.117 |
| 100.68 | 22.68 | . 424 | 19.83 | . 764 | 22.63 | . 883 | 22.16 | . 506 | 22.50 | . 784 | 22.14 | 279.000 | 22.41 | . 510 |
| 5342.82 | 22.34 | 353.094 | 21.19 | 63. 153 |  |  | 22.28 | 199.476 | 21.88 | 401.114 |  |  | 22.56 | 517.899 |
| 370.89 | . 77 | 360.475 | . 42 | 64.472 |  |  | 21.35 | 203.646 | 22.44 | 409.479 |  |  | . 50 | 528.725 : |
| 371.74 | . 85 | . 699 | - | - |  |  | - | - | . 72 | . 752 |  |  | . 73 | 529.062 |
| . 88 | . 84 | . 736 | . 30 | . 519 |  |  | 21.40 | . 793 | 22.70 | . 794 |  |  | . 60 | . 107 |
| 372.76 | . 20 | . 967 | - | - |  |  | - | - | 21.82 | 410.057 |  |  | . 04 | . 446 |
| 373.94 | . 80 | 361.278 | . 19 | . 616 |  |  | - | - | 22.36 | . 410 |  |  | . 50 | . 901 |
| 394.69 | . 56 | 366.734 | . 50 | 65.593 |  |  | 22.16 | 207.181 | 22.45 | 416.608 |  |  | . 88 | 537.904 |
| 395.77 | . 26 | 367.018 | . 40 | . 643 |  |  | . 22 | . 341 | 21.85 | . 930 |  |  | 22.00 | 538.321 |
| . 94 | . 26 | . 054 | . 09 | . 651 |  |  | .20: | . 360 | 21.56 | . 970 |  |  | 21.97 | . 373 |
| 396.68 | . 73 | . 257 | 20.45 | . 686 |  |  | 22.50 | . 477 | 22.23 | 417.202 |  |  | 22.65 | . 672 |
| . 84 | 22.78 | . 299 | - | - |  |  | - | - | - | 17.202 |  |  | . 53 | . 733 |
| 397.90 | 23.00 | . 578 | 19.70 | . 743 |  |  | 21.20 | . 657 | . 70 : | . 567 |  |  | . 75 | 539.142 |
| 403.84* | 22.40 | 369.140 | 20.78 | 66.023 |  |  | . 90 : | 208.540 | - | , |  |  | . 00 | 541.433 |
| 426.83* | . 50 | 375.185 | 20.94 | 67.103 |  |  | 21.80: | 211.956 | - | - |  |  | . | 54.433 |
| 450.69 | 22.80 | 381.459 | 21.22 | 68.226 |  |  | 22.13 | 215.500 | 22.47 | 433.336 |  |  | 22.35 | 559.502 |
| 5690.94 | 22.80 | 444.633 | 21.45 | 79.525 |  |  | 22.00 | 251. 189 | 21.90 | 505.101 |  |  | 22.60 | 652.162 |
| 692.88 | . 40 | 445.143 | . 47 | . 616 |  |  | 22.17 | . 477 | 22.65 | . 680 |  |  | 22.55 | . 910 |
| 693.88 | . 75 | . 406 | 21.00 | . 663 |  |  | 21.50 | . 624 | 21.65 | . 979 |  |  | 21.92 | 653.296 |
| 715.78 | . 61 | 451.164 | 20.15 | 80.693 |  |  | . 50 | 254.879 | 22.80 | 512.521 |  |  | 22.55 | 661.742 |
| 716.77 | . 76 | . 425 | 19.75 | . 740 |  |  | 21.90 | 255.026 | . 60 : | . 816 |  |  | . 57 | 662.124 |
| 717.79 | . 71 | . 693 | . 82 | . 788 |  |  | 22.05 | . 178 | . 08 | 513.121 |  |  | . 45 | 662. 517 |
| 718.77 | . 03 | . 950 | 19.87 | . 834 |  |  | . 05 : | . 323 | . 55 | . 414 |  |  | 22.90 | . 895 |
| 719.80 | . 55 | 452.221 | 20.15 | . 882 |  |  | 22.20 | . 476 | . 70 | . 721 |  |  | 21.83 | 663.292 |
| 808.78 | 22.95 | 475.619 | 20.62 | 85.068 |  |  | 21.17 | 268.694 | 22.43 | 540.301 |  |  | 22.40 | 697.610 |
|  | $\vee 30$ |  | $\vee 31$ |  | $\vee 36$ |  | $\checkmark 42$ * |  | V 46 |  | $\vee 48$ |  |  |  |
| 4184.95 | 21.45 | 14.361 | 20.40 | 13.868 | 22.36 | 51.470 | 22.08 | 59.694 | 23.01 | 49.838 | 23.10 | 54.346 |  |  |
| 224.89 | 20.73 | 17.461 | . 46 | 16.863 | . 58 | 62.585 | 21.72 | 72.585 | 22.78 | 50.601 | 22.65 | 66.082 |  |  |
| 243.83 | 21.79 | 18.932 | . 64 | 18.283 | . 93 | 67.855 | . 88 | 78.698 | 22.95 | 65.705 | 2.65 .90 | 71.647 |  |  |
| 244.84 | 22.00 | 19.010 | . 57 | . 359 | . 58 | 68.136 |  | , | 23.29 | . 978 | . 58 | . 944 |  |  |
| 245.84 | . 12 | . 085 | . 44 | . 434 | . 30 | . 415 | - | - | . 29 | 66.247 | . 68 | 72.237 |  |  |
| . 90 | 22.08 | . 093 | . 48 | . 438 | . 42 | . 431 | - | - | 23.44 | . 263 | . 78 | . 255 |  |  |
| 246.81 | 21.90 | . 164 | . 34 | . 506 | . 63 | . 684 | . 82 | 79.660 | 22.63 | . 509 | . 83 | . 522 |  |  |
| 277.75 | 20.97 | 21.567 | . 33 | 20.827 | . 16 | 77.295 | - | 7.66 | 23.07 | 74.845 | . 8 | . 52 |  |  |
| 304.70 | 20.97 | 23.660 | . 41 | 22.848 | . 93 | 84.795 | - | - | 23.07 | 74.845 | - | - |  |  |
| 305.66 | 21.27 | . 734 | . 53 | . 920 | . 93 | 85.062 | 21.96 | 98.655 | . 38 | 82.366 | . 38 | 89.815 |  |  |
| 330.70* | 21.10 | 25.679 | . 30 | 24.798 | - | - | 22.04: | 107.737 | - | 82.366 | . 38 | 8.815 |  |  |
| 334.64 | 22.02 | . 985 | . 81 | 25.093 | . 53 | 93.127 | 22.08 | 108.008 | - | - | - | - |  |  |
| 360.61 | 21.84 | 28.001 | . 75 | 27.040 | . 16 | 100.354 | 21.96 | 116.389 | 23.26 | 97.174 | . 68 | 105.962 |  |  |
| 361.61 | . 94 | . 079 | . 78 | . 115 | 22.68 | . 632 | 21.96 | 116.389 | 22.58 | . 444 | . 83 | 106.256 |  |  |
| 362.67 | 21.70 | . 161 | 20.69 | . 194 | - |  | (22.1 | 117.055 | 23.10 | . 729 | 22.93 | . 567 |  |  |
| 4596.91 | 21.40 | 46.350 | 20.19 | 44.759 | 22.64 | 166. 114 | 21.. 6 | 192.659 | 23.08 | 160.849 |  |  |  |  |
| 597.88 | 21.37 | . 425 | . 34 | . 832 | . 26 | . 384 | 22.12 | 192.659 .972 | 23.08 .32 | 160.849 161.110 | 22.92 .78 | 175.396 .681 |  |  |
| 598.88 | 20.78 | . 503 | . 41 | . 907 | . 60 | . 662 | - | . | . 20 | . 380 | . 63 | . 975 |  |  |
| 599.87 | 20.81 | . 580 | . 52 | . 981 | . 43 | . 938 | 21.69 | 193.614 | . 08 | . 648 | . 6 | . 9 |  |  |
| 600.88 | 21.10 | . 658 | . 71 | 45.057 | . 16 | 167.219 | 22.04 | . 940 | . 32 | . 919 | . 88 | 176.562 |  |  |
| 601.96 | . 25 | . 742 | . 83 | . 138 | . 48 | . 519 | 22.08 | 194.289 | 23.26 | 162.210 | . 53 | 176.562 |  |  |
| 602.88* | 21.40 | . 814 | . 84 | . 207 | . 70 | . 775 | 21.80 | . 585 | 22.73 | r . | . 5 | . 88 |  |  |
| 625.77* | 20.90 | 48.591 | . 48 | 46.923 | . 40 | 174.146 | 22.08 | 201.973 | . 83 | 168.626 | - | - |  |  |
| . 89 | 20.98 | . 600 | 20.51 | .932 | 22.36 | . 179 | 22.12 | 202.012 | 22.93 | 168.626 .658 | 22.58 | 183.912 |  |  |

Table A (continued)

| $\begin{aligned} & \text { JD } \\ & 2,430,000+ \end{aligned}$ | $\vee 30$ |  | $\vee 31$ |  | $\vee 36$ |  | $\vee 42$ * |  | $\checkmark 46$ |  | $\vee 48$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | B | Phase | B | Phase | B | Phase | B | Phase | B | Phase | B | Phase |
| 4626.77 | 21.03 | 48.668 | 20.64 | 46.998 | 22.24 | 174.424 | 22.04 | 202.295 | 23.41 | 168.905 | 22.68 | 184.170 |
| .87* | . 10 | . 676 | . 65 | 47.006 | . 40 | . 452 | 22.12 | . 328 | - | - | - | - |
| 627.76 | . 35 | . 745 | . 66 | . 073 | . 78 | 699 | 21.96 | . 616 | 23.44 | 169.162 | . 73 | . 461 |
| 628.91 | . 65 | . 834 | . 84 | . 159 | . 88 | 175.019 | 22.08 | . 987 | 22.60 | . 472 | . 24 | . 799 |
| 629.76 | . 58 | . 900 | . 80 | . 222 | . 00 | . 256 | - | - | 22.88 | . 701 | . 83 | 185.049 |
| 630.78 | . 82 | . 979 | . 75 | . 299 | . 38 | . 540 | 21.62 | 203.590 | 23.19 | . 976 | . 88 | . 348 |
| 633.76 | . 76 | 49.211 | . 30 | . 522 | . 22 | 176.369 | 21.50 | 204.552 | . 33 | 170.779 | 22.93 | 186.224 |
| . 334.85 | . 64 | . 283 | . 22 | . 604 | . 80 | . 672 | 22.04 | . 904 | . 38 | 171.073 | 23.03 | . 544 |
| . 660.75 | 21.41 | 51.307 | . 28 | 49.546 | . 70 | 183.880 | . 12 | 213.264 | . 50 | 178.052 | 22.90 | 194. 155 |
| 663.80 | 20.88 | . 544 | . 22 | . 775 | . 75 | 184.728 | 22.28 | 214.248 | . 26 | . 874 | - | - |
| . 580.64 | 21.62 | 52.852 | . 69 | 51.038 | . 38 | 189.415 | 21.88 | 219.683 | 23.10 | 183.413 | 22.95 | 200.000 |
| . 681.69 | . 84 | . 933 | . 84 | . 117 | . 53 | . 707 | 22.28 | 220.022 | 22.93 | . 696 | - | - |
| . 582.66 | 21.88 | 53.009 | . 82 | . 189 | .75: | . 977 | 22.22 | . 335 | 23.41 | . 957 | 23.14 | . 593 |
| 714.65* | 20.75 | 55.492 | . 20 | 53.588 | . 90 | 198.880 | 21.72 | 230.660 | - | - | - | - |
| 717.61 | 21.35 | . 722 | . 32 | . 810 | . 70 | 199.703 | . 72 | 231.616 | 23.11 | 193.374 | 22.48 | 210.863 |
| 718.62 | 21.46 | . 800 | 20.46 | . 886 | 22.93 | . 984 | 21.96 | . 942 | 22.94 | . 646 | 22.95 | 211.160 |
| -4923.95 | - | - | 20.72 | 69.282 | 22.42 | 257.126 | 22.04 | 298.214 | 23.22 | 248.977 | 22.98 | 271.493 |
| 924.95 | 21.45 | 71.823 | . 60 | . 357 | . 18 | . 404 | 21.54 | . 537 | 23.35 | 249.247 | 22.44 | . 787 |
| 925.95 | . 70 | . 900 | . 55 | . 432 | . 63 | . 683 | - | - | 22.75 | . 516 | 23.00 | 272.081 |
| 926.95 | . 88 | . 978 | . 32 | . 507 | . 95 | . 861 | 22.04 | 299. 182 | 23.30: | . 787 | 22.83 | . 374 |
| 927.95* | . 90 | 72.055 | . 13 | . 582 | . 05 | 258.239 | 21.69 | . 505 | - | - | - | - |
| 928.95 | . 90 | . 133 | . 13 | . 657 | . 40 | . 517 | 22.12 | . 829 | - | - | . 78 | . 962 |
| 929.95 | . 84 | . 211 | . 14 | . 732 | . 80 | . 796 | - | - | 22.70 | 250.593 | . 88 | 273.256 |
| '930.95 | . 46 | . 289 | . 32 | . 807 | 22.83 | 259.074 | 21.92 | 300.473 | 23.38 | . 863 | . 95 | . 550 |
| 931.94 | . 60 | . 365 | . 47 | . 88 i | 2 i .98 | . 349 | 22.00 | . 793 | - | - | . 29 | . 841 |
| 932.96 | 21.10 | . 445 | . 55 | . 957 | 22.48 | . 633 | 22.28 | 301.122 | 22.90 | 251.405 | 22.80 | 274.141 |
| 954.97 | 22.06 | 74.153 | . 06 | 71.608 | . 88 | 265.758 | - | - | 23.14 | 257.338 | 23.08 | 280.608 |
| 979.83* | 21.90 | 76.084 | - | - | . 55 | 272.677 | - | - | - | - | - | - |
| 980.89* | . 90 | . 166 | . 30 | 73.552 | . 90 | . 972 | 21.50 | 316.592 | - | - | - | - |
| 981.88 | . 86 | . 243 | . 19 | . 626 | . 24 | 273.247 | . 85 | .911 | 22.90 | 264.587 | 23.14 | 288.516 |
| 983.86 | 21.39 | . 397 | . 17 | . 774 | . 80 | . 798 | . 76 | 317.551 | 23.26 | 265.121 | 22.65 | 289.098 |
| 984.92 | 20.82 | . 479 | . 43 | . 854 | . 88 | 214.092 | 21.92 | . 893 | 22.85 | . 406 | . 83 | . 409 |
| 985.86 | . 88 | . 552 | . 48 | . 924 | . 18 | . 354 | 22.28 | 318.196 | . 75 | . 660 | . 88 | . 686 |
| . 98 | 20.86 | . 562 | . 52 | . 933 | . 30 | . 387 | . 28 | . 235 | 22.82 | . 692 | . 65 | . 721 |
| 5006.79 | 21.82 | 78.177 | . 44 | 75.494 | . 40 | 280. 179 | . 16 | 324.952 | 23.14 | 271.300 | . 38 | 295.835 |
| 007.81 | . 70 | . 256 | . 25 | . 570 | . 48 | . 463 | 22.28 | 325.281 | 22.67 | . 575 | . 88 | 296.135 |
| 008.79 | . 54 | . 332 | . 17 | . 644 | . 68 | . 735 | 21.72 | . 597 | 23.20 | . 839 | . 93 | . 423 |
| 009.74 | . 30 | . 406 | . 10 | . 715 | . 75 | 281.000 | 22.28 | . 904 | . 30 | 272.095 | . 74 | . 702 |
| . 82 | 21.31 | . 412 | . 18 | . 721 | 22.83 | . 022 | . 16 | . 929 | . 22 | . 117 | . 55 | . 726 |
| 010.76 | 20.78 | . 485 | . 25 | .791 | 21.98 | . 284 | 22.28 | 326.233 | 23.29 | . 370 | . 73 | 297.002 |
| . 011.79 | 20.90 | . 565 | . 45 | . 869 | 22.50 | . 570 | 21.72 | . 565 | 22.90 | . 648 | . 83 | . 305 |
| 035.74 | 21.20 | 80.425 | . 16 | 77.665 | . 11 | 288.236 | 22.04 | 334.295 | 23.18 | 279.101 | . 84 | 304.342 |
| 036.87 | 20.80 | . 513 | . 16 | . 749 | . 62 | . 551 | 21.88 | . 660 | 22.85 | . 405 | . 82 | . 675 |
| 1037.70 | . 85 | . 578 | . 35 | . 812 | . 62 | . 782 | 22.16 | . 928 | . 91 | . 629 | . 54 | . 918 |
| . 84 | 20.94 | . 588 | . 32 | . 822 | . 78 | . 821 | 22.28 | . 973 | 22.88 | . 667 | . 75 | . 960 |
| 1038.70 | 21.19 | . 655 | . 46 | . 887 | . 70 | 289.060 | - | - | 23.32 | . 899 | . 70 | 305.212 |
| 064.63 | . 06 | 82.669 | . 35 | 79.831 | . 10 | 296.276 | 21.80 | 343.620 | 23.38 | 286.886 | . 40 | 312.831 |
| 065.63 | . 45 | . 747 | . 54 | . 906 | . 50 | . 555 | 22.04 | . 943 | - | - | . 79 | 313.125 |
| 066.63 | . 64 | . 824 | . 66 | . 981 | . 77 | . 833 | 22.28 | 344.265 | 22.70 | 287.425 | . 82 | . 419 |
| 067.62 | . 74 | . 902 | . 80 | 80.055 | - | - | 21.69 | . 585 | 23.22 | . 692 | . 70 | . 710 |
| 068.62 | 21.82 | . 979 | . 84 | . 130 | . 19 | 297.386 | 22.08 | . 908 | . 41 | . 961 | . 71 | 314.004 |
| 069.62 | 22.00 | 83.057 | . 88 | . 205 | . 63 | . 665 | . 32 | 345.231 | . 40 | 288.231 | . 71 | . 297 |
| . 81 | 22.00 | . 071 | . 82 | . 219 | . 88 | . 717 | - | - | . 20 | . 282 | 22.98 | . 353 |
| 097.63 | 21.65 | 85.231 | . 78 | 82.306 | . 31 | 305.459 | - | - | . 04 | 295.778 | 23.14 | 322.528 |
| . 76 | . 74 | .241 | . 69 | . 316 | . 42 | . 495 | 22.16 | 354.313 | . 41 | . 813 | - | - |
| 098.64 | . 55 | . 309 | . 57 | . 382 | . 72 | . 740 | 21.62 | . 597 | . 32 | 296.050 | 22.27 | . 824 |
| 099.66 | 21.47 | . 389 | . 46 | . 459 | . 80 | 306.024 | 22.04 | . 926 | 23.23 | . 225 | 22.84 | 323.124 |
| 100.68 | 20.86 | . 468 | 20.37 | . 535 | 22.16 | . 308 | 22.08 | 355.255 | 22.78 | . 600 | - |  |
| 5342.82 | 21.58 | 104.270 | 20.06 | 100.691 | 22.42 | 373.693 |  |  | 22.98 | 361.850 | - | - |
| 370.89 | 21.00 | 106.449 | . 27 | 102.796 | . 42 | 381.505 |  |  | . 96 | 369.414 | 22.36 | 402.822 |
| 371.74 | 20.88 | . 515 | . 43 | . 860 | . 70 | . 748 |  |  | 22.95 | . 648 | - | - |
| . 88 | 20.83 | . 526 | . 37 | . 870 | . 89 | . 780 |  |  | 23.00 | . 681 | . 75 | 403.113 |
| 372.76 | 21.00 | . 594 | . 46 | . 936 | - | - |  |  | . 23 | . 917 | - | - |
| 373.94 | - | - | . 63 | 103.025 | - | - |  |  | . 32 | 370.236 | - | - |
| 394.69 | . 40 | 108.298 | . 20 | 104.581 | . 75 : | 388.128 |  |  | . 10 | 375.827 | . 35 : | 409.816 |
| 395.77 | 21.42 | . 381 | . 11 | . 662 | . 24 | . 428 |  |  | . 20 | 376.118 | 22.75 | 410.132 |
| . 94 | - | - | . 03 | . 675 | . 32 | . 467 |  |  | . 20 | . 164 | 23.03 | . 183 |
| 396.68 | 20.90 | . 452 | . 15 | . 730 | . 72 | . 682 |  |  | .00: | . 363 | 22.73 | . 400 |
| . 84 | . 72 | . 465 | . 18 | . 742 | - | - |  |  | 23.10: | . 406 | . 73 | . 447 |
| 397.90 | 20.80 | . 547 | . 36 | . 821 | . 70 : | 389.021 |  |  | 22.95 | . 692 | . 35 | . 758 |
| 403.84* | 22.00 | 109.008 | . 70 | 105.267 | . 60 | 390.675 |  |  | - | - | - | - |
| 426.83* | 21.40 | 110.793 | . 70 | 106.991 | - | - |  |  | - | - | - | - |
| 450.69 | 21.09 | 112.646 | 20.24 | 108.780 | 22.60: | 403.712 |  |  | 23. 10: | 390.917 | 22.90 | 426.271 |
| . 5690.94 | 21.40 | 131.301 | 20.18 | 126.795 | 22.30 | 470.571 |  |  | 22.75 | 455.658 | 22.45 | 496.866 |
| 692.88 | 20.90 | . 452 | . 55 | . 941 | . 70 | 471.111 |  |  | - | - | . 85 : | 497.436 |
| 693.88 | 20.82 | . 530 | . 73 | 127.016 | . 10 | . 390 |  |  | . 55 | 456.451 | . 60 | . 729 |
| 715.78 | 21.60 | 133.230 | . 13 | 128.658 | . 30 | 477.484 |  |  | - | - | . 80 | 504. 165 |
| 716.77 | . 37 | . 307 | . 20 | . 732 | . 65 | . 760 |  |  | 22.75: | 462.618 | . 80 | . 456 |
| 717.79 | 21.40 | . 386 | . 30 | . 808 | . 75 | 478.044 |  |  | 23.00 | . 893 | . 50 | . 755 |
| 718.77 | 20.95 | . 452 | . 39 | . 882 | . 00 | . 361 |  |  | 23.20 | 463.157 | . 70 | 505.044 |
| 719.80 | . 72 | . 542 | . 55 | . 959 | . 50 | . 601 |  |  | 22.70 | . 435 | . 80 | . 346 |
| 808.78 | 20.95 | 140.451 | 2U. 20: | 135.631 | 22.20 | 503.365 |  |  | 22.90 | 487.412 | 22.90: | 531.495 |

Table A (continued)

| JD | $\vee 22$ |  | $\vee 24$ |  | $\checkmark 25 *$ |  | $\vee 34 *$ |  | $\checkmark 53 *$ |  | $\checkmark 55$ |  | V 57 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2,430,000+ | B | Phase | B | Phase | B | Phase | B | Phase | B | Phase | B | Phase | B | Phase |
| 4184.95 | 22.40 | 4.958 | 21.83 | 3.999 | 22. 12 | 4.690 | 21.64 | 2.983 | 22.48 | 9.307 | 23.14 | 9.604 | 22. 18 | 3.459 |
| 224.84 | 21.80 | 6.029 | . 85 | 4.862 | 21.88 | 5.703 | . 45 | 3.627 | . 15 | 11.316 | 22.98 | 11.678 | . 10 | 4. 205 |
| 243.83 | 22.20 | . 537 | . 27 | 5.271 | 22.04 | 6.183 | . 33 | . 933 | . 73 | 12.269 | (23.0 | 12.662 | . 13 | . 560 |
| 244.84 | . 14 | . 564 | . 33 | . 292 | 21.80 | . 209 | . 54 | . 951 | . 48 | . 320 | 22.98 | . 714 | 22.30 | . 578 |
| 245.84 | . 30 | . 591 | . 33 | . 314 | 22.16 | . 235 | . 33 | . 966 | . 18 | . 370 | (23.0 | . 766 | 21.98 | . 597 |
| . 90 | . 28 | . 593 | . 39 | . 315 | . 20 | . 237 | - | - | - | - | 23.26 | . 769 | 21.90 | . 598 |
| 246.81 | . 26 | . 617 | 21.29 | . 336 | . 16 | . 259 | . 31 | . 981 | . 53 | . 419 | . 14 | . 817 | 22.02 | . 615 |
| 277.75 | 22.20 | 7.446 | 22.10 | 6.006 | (22.3 | 7.044 | . 67 | 4.480 | . 73 | 13.976 | - | - | . 06 | 5.194 |
| 304.70 | 21.50 | 8.170 | 21.30 | . 588 | 21.60 | . 727 | . 20: | . 915 | . 27 | 15.332 | (22.7 | 15.823 | . 08 | . 698 |
| 305.66 | 21.84 | . 195 | . 37 | . 609 | 21.76 | . 752 | . 33 | . 931 | . 63 | . 381 | 23.26 | . 873 | 22.00 | . 716 |
| 330.70* | 22.50 | . 866 | . 40 | 7.150 | 22. 10 | 8.386 | . 10 | 5.334 | . 59 | 16.641 | 22.40 | 17.173 | 21.90 | 6.184 |
| 334.64 | . 44 | . 972 | . 48 | . 234 | 21.90 | . 486 | . 19 | . 398 | . 73 | . 839 | . 60 | . 378 | 22.18 | . 258 |
| 360.61 | . 02 | 9.668 | . 48 | . 796 | 22.73 | 9.145 | . 45 | . 817 | . 83 | 18.146 | (22.7 | 18.726 | . 03 | . 743 |
| 361.61 | . 32 | . 695 | . 58 | . 818 | . 48 | . 170 | . 70 | . 833 | . 73 | . 196 | (22.7 | . 728 | . 20 | . 762 |
| 362.67 | 22.40 | . 723 | 21.86 | . 841 | 22.48 | . 197 | 21.31 | . 850 | 22.36 | . 249 | 23.0: | . 833 | 22.26 | . 781 |
| 4596.91 | 21.60 | 16.003 | 21.65 | 12.905 | 22.28 | 15. 138 | 21.64 | 9.628 | 22.98 | 30.036 | 22.52 | 30.997 | 21.80 | 11.162 |
| 597.88 | . 60 | . 029 | . 69 | . 926 | . 48 | . 162 | . 64 | . 644 | . 98 | . 085 | . 50 | 31.048 | . 85 | . 180 |
| 598.88 | . 60 | . 056 | . 74 | . 948 | . 32 | . 188 | . 70 | . 660 | . 68 | . 136 | . 40 | . 100 | . 92 | . 199 |
| 599.87 | . 76 | . 083 | . 82 | . 970 | . 73 | . 213 | . 70 | . 676 | . 83 | . 185 | . 40 | . 151 | 21.86 | . 217 |
| 600.88 | . 62 | . 110 | . 76 | . 991 | . 73 | . 238 | . 67 | . 692 | . 73 | . 236 | . 24 | . 203 | 22.03 | . 235 |
| 601.96 | . 67 | . i39 | . 76 | 13.013 | . 98 | . 266 | . 62 | . 709 | . 53 | . 290 | . 22 | . 260 | 21.90 | . 257 |
| 602.88* | 21.65 | . 163 | . 60 | . 034 | 22.98 | . 289 | 21.76 | . 724 | . 28 | . 337 | . 51 | . 307 | 22.10 | . 274 |
| $625.77 *$ | 22.40 | . 777 | . 00 | . 529 | 21.65 | . 870 | 20.90 | 10.094 | . 63 | 31.489 | . 95 | 32.496 | . 10 | . 702 |
| . 89 | . 58 | . 780 | . 10 | . 530 | . 65 | . 873 | . 97 | . 096 | . 49 | . 495 | 22.93 | . 502 | . 24 | . 704 |
| 626.77 | . 60 | . 804 | 21.10 | . 551 | . 70 | . 895 | 20.97 | . 110 | . 44 | . 539 | 23.08 | . 548 | . 02 | . 720 |
| . $87 *$ | . 65 | . 806 | 20.95 | . 553 | . 80 | . 897 | 21.05 | . 111 | . 36 | . 545 | . 00 | . 553 | 22. 10 | . 722 |
| 627.76 | . 75 | . 830 | 21.29 | . 573 | . 80 | . 920 | 20.91 | . 128 | . 36 | . 586 | (22.9 | . 600 | 21.86 | . 739 |
| 628.91 | . 50 | . 861 | . 21 | . 595 | . 72 | . 949 | 20.97 | . 144 | . 60 | . 647 | 22.93 | . 659 | 22.02 | . 761 |
| 629.76 | . 65 | . 884 | . 13 | . 616 | 21.88 | . 971 | 21.02 | . 158 | ${ }^{-}$ | . 647 | (23.0 | . 703 | 21.84 | . 776 |
| 630.78 | . 90 | . 911 | . 27 | . 638 | 22.08 | . 997 | . 17 | . 175 | (22.5 | . 741 | (23.0 | . 756 | . 86 | . 795 |
| 633.76 | 22. 10 | . 9990 | . 17 | . 702 | . 28 | 16.072 | 21.06 | . 223 | 22.73 | . 891 | 22.88 | . 911 | . 94 | . 85 \% |
| 634.85 | 21.92 | 17.020 | . 33 | . 724 | 22.12 | . 100 | 20.94 | . 239 | . 83 | . 946 | . 70 | . 968 | . 72 | . 870 |
| 660.75 | 22.46 | . 715 | . 15 | 14.286 | 21.88 | . 757 | 21.64 | . 658 | . 53 | 33.249 | . 26 | 34.313 | 21.94 | 12.356 |
| 663.80 | 22.32 | . 797 | . 02 | . 351 | 21.76 | . 834 | . 67 | . 708 | . 36 | . 403 | . 98 | +.471 | 22.14 | . 2.413 |
| 680.64 | 21.72 | 18.248 | . 50 | . 715 | 22.63 | 17.261 | . 41 | . 979 | (22.7 | 34.250 | . 32 | 35.346 | . 22 | . 728 |
| 681.69 | . 65 | . 276 | . 50 | . 738 | . 98 | . 288 | . 29 | . 995 | 22.36 | . 303 | . 38 | 35.346 .400 | . 18 | . 748 |
| 682.66 | . 74 | . 302 | . 76 | . 759 | 22.98 | . 312 | . 17 | 11.011 | . 44 | . 351 | . 98 | . 450 | . 17 | . 766 |
| 714.65* | . 45 | 19.159 | .90: | 15.470 | 21.80 | 18.124 | , | . | (22.4 | 35.961 | 22.30: | 37.111 | . 15 | 13.364 |
| 717.61 | . 71 | . 239 | . 67 | . 514 | . 80 | . 199 | . 33 | . 575 | (22.7 | 36.110 | 22.38 | . 265 | . 06 | 13.364. .419 |
| 718.62 | 21.78 | . 266 | 21.76 | . 536 | 21.88 | . 224 | 21.58 | . 591 | (22.7 | . 161 | 22.34 | . 318 | 22.14 | . 438 |
| 4923.95 | 22.60 | 24.771 | 20.95 | 19.975 | 22.98 | 23.431 |  | 14.903 |  |  |  |  |  |  |
| 924.95 | . 50 | . 798 | 21.04 | . 996 | 22.83 | . 457 | 21.46 .33 | 14.909 | ${ }^{22} 2.3$ | 46.493 .543 | 22.68 .24 | 48.033 | 22.34 .28 | 17.278 .296 |
| 925.95 | . 53 | . 825 | 21.04 | 20.018 | 22.63 | . 482 | . 65 | . 936 | 22.63 | . 593 | . 42 | 48.033 .084 | . 28 | . .315 |
| 926.95 | . 78 | . 851 | 20.98 | . 040 | 23.03 | . 507 | . 56 | . 952 | . 53 | . 644 | . 53 | . 136 | . 09 | . 334 |
| 927.95* 928.95 | .70 .95 | .878 .905 | 21.05 .10 | . 062 | 22.90 | . 533 | - | - | (22.3 | . .694 | . 60 | . 188 | . 30 | . .353 |
| 928.95 929.95 | .95 .55 | .905 .932 | .10 .19 | .083 .104 | .93 .40 | . 558 | .37 .39 | . 9883 | 22.73 | . 745 | . 38 | . 240 | . 45 | . 37 ¢ |
| 929.95 930.95 | . 55 | . .932 | .19 .19 | .104 .126 | . 40 | . 584 | . 39 | 15.000 .016 | .73 $(22.7$ | .795 .845 | .40 .70 | . 292 | . 24 | . 390 |
| 931.94 | . 80 | . 985 | . 19 | . 148 | 22.00 | . 634 | . 10 | . 032 | (22.7 | . 845 | . 70 | . 344 | . 24 | . 409 |
| 932.96 | 22.40 | 25.013 | . 36 | . 170 | 21.65 | . 660 | . 11 | . 047 | (22.5 | . 947 | . 78 | .396 .449 | .36 22.30 | . 428 \% |
| 954.97 | 21.74 | . 603 | . 23 | . 645 | 22.70 | 24.318 | . 30 | . 404 | 23.00 | 48.054 | 23.05 | .449 49.591 | 22.30 21.90 | . 848 |
| 979.83 | . 70 | 26.269 | . 35 | 21.184 | . 10 | . 848 | - | - | 22.28 | 49.305 | 23.05 | 4.51 | 22.10: | 18.323. |
| 980.89 981.88 | .80: | . 298 | . 50 | . 207 | .10 | . 875 | - | - | . 36 | . 358 | 22.70: | 50.938 | 2.10: | - 343. |
| 981.88 | 21.89 | . 324 | . 86 | . 228 | 22.00 | . 900 | . 48 | . 838 | . 44 | . 398 | . 70 | . 989 | . 18 | . 361 |
| 983.86 | 22.08 | . 377 | . 65 | . 272 | 21.92 | . 951 | . 58 | . 870 | . 58 | . 497 | . 44 | 51.092 | . 26 | . 398 |
| 984.92 985.86 | 22.10 21.98 | . 405 | . 69 | . 293 | 22.00 | . 978 | . 69 | . 886 | . 63 | . 561 | . 32 | . 147 | . 14 | . 417 |
| 985.86 .98 | 21.98 22.02 | . 431 | .84 21.88 | .315 .316 | .08 21.88 | 25.001 .004 | . 45 | . 902 | . 73 | . 608 | . 40 | . 195 | . 10 | . 436 |
| 5006.79 | . 30 : | . .992 | 20.99 | . 767 | 21.88 22.28 | . .532 | . 04 | 16.239 | . 63 | .614 50.662 | . 48 | 52.282 | 22.18 | . 437 |
| 007.81 | . 08 | 27.019 | . 95 | . 789 | 21.88 | . 558 | . 02 | 16.239 .255 | . 68 | 50.662 .713 | . 48 | 52.282 .335 | 21.93 22.03 | . 827 |
| 008.79 | 22.04 | . 046 | 20.95 | . 810 | 22.12 | . 583 | . 06 | . 271 | . 78 | . 762 | . 63 | . 386 | 21.78 | . 8864 |
| 009.74 | 21.75 | . 071 | 21.10 | . 831 | 22.16 | . 607 | . 15 | . 286 | . 73 | . 810 | . 63 | . 386 | . 87 | . 8882 |
| .82 010.76 | . 74 | . 073 | 20.98 | . 832 | - | - | 21.09 | . 287 | . 63 | . 814 | . 71 | . 440 | . 72 | . 883 |
| 010.76 011.79 | .67 21.45 | . 098 | 20.98 | . 853 | 21.88 | . 633 | 20.97 | . 304 | (22.5 | . 861 | . 90 | . 489 | . 90 | . 901 |
| 035.74 | 22.30 | . 1268 | 21.00 .74 | .875 22.392 | 21.80 22.48 | .659 26.266 | 21.21 .69 | . 320 | 22.83 | 5.913 | 22.98 | . 542 | 21.89 | . 921 |
| 036.87 | . 26 | . 798 | . 67 | . 414 | . 46 | 26.296 .295 | . 70 | . 722 | . 83 | 52.118 .175 | (23.0 | 53.786 | 22.18 | 19.367 |
| 037.70 | . 20 | . 821 | . 74 | . 435 | . 53 | . 316 | . 72 | . 737 | (22.7 | . 217 | 23.05 | . 845 | . 23 | .388 .405. |
| . 84 | . 24 | . 824 | . 85 | . 436 | . 48 | . 320 | . 78 | . 738 |  | . | (23.0 | . 895 | . 22 | . 405. |
| 038.70 | . 30 | . 848 | . 86 | . 457 | . 44 | . 341 | . 64 | . 753 | (22.5 | . 267 | (23.0 | . 940 | 22.24 | .408: |
| 064.63 | . 06 | 28.543 | . 29 | 23.017 | . 12 | . 999 | . 10 | 17. 172 | 22.60 | 53.572 | 22.53 | 55.286 | 21.94 | . 908 : |
| 065.63 066.63 | .12 .14 | . 570 | .30 .30 | . 038 | . 12 | 27.024 | 21.02 | . 189 | . 50 | . 622 | . 70 | . 338 | 22.08 | . 927 |
| 066.63 067.62 | . 14 | . 596 | . 30 | . 060 | .28 .53 | .050 .075 | 20.92 21.08 | .205 .220 | .73 .58 | . 673 | . 48 | . 390 | 22.08 | . 945 |
| 068.62 | . 28 | . 650 | . 22 | . 103 | . 12 | . 100 | 21.08 20.88 | . 2237 | . 58 | . 722 | .73 .73 | . 442 | 21.98 | . 964 |
| 069.62 | . 38 | . 677 | . 36 | . 125 | . 28 | . 126 | . 94 | . 253 | . 73 | . 823 | ${ }_{(23.0}^{.73}$ | . 493 | 22.08 21.90 | [.983: |
| .81 097 | 22.44 | . 682 | . 31 | . 126 | 22.20 | . 130 | 20.91 | . 256 | . 63 | . 832 | 22.93 | . 555 | 21.90 21.90 | 20.001 .005 |
| 097.63 .76 | 21.90 | 29.427 | . 28 | . 730 | 21.87 | . 836 | 21.73 | . 705 | . 44 | 55.233 | . 82 | 57.000 | 22.08 | . 525 |
| .76 098.64 | 22.00 21.98 | . 431 | .21 .23 | .731 .752 | .76 .69 | . 839 | 80 | - | . 58 | . 239 | . 68 | . 007 | . 18 | . 528 |
| 099.66 | 21.95 | . 482 | . 13 | . 752 | . 69 | . 862 | . 80 | . 721 | . 28 | . 284 | . 46 | . 052 | . 18 | . 544 |
| 100.68 | 22.00 | . 509 | 21.08 | . 797 | 21.80 | . 913 | 21.82 | . 754 | 2.28 | .335 .386 | - 23.58 | . 105 | . 18 | . 562 |
|  |  |  |  |  |  |  |  |  |  |  | 22.55 | . 158 | 22. 10 | . 583 |

Table A (continued)

| $\begin{aligned} & \text { JD } \\ & 2,430,000+ \end{aligned}$ | $\vee 22$ |  | $\vee 24$ |  | $\vee 25^{*}$ |  | $\checkmark 34 *$ |  | $\checkmark 53$ * |  | $\checkmark 55$ |  | $\checkmark 57$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | B | Phase | B | Phase | B | Phase | B | Phase | B | Phase | B | Phase | B | Phase |
| 5342.82 | 22.40: | 36.001 | 21.19 | 29.031 | 21.88 | 34.054 | 21.80 | 21.660 | (22.3 | 67.571 | - | - | 21.93 | 25.112 |
| 370.89 | 21.84 | . 754 | . 70 | . 637 | . 80 | . 766 | 20.97 | 22.112 | (22.7 | 68.983 | 22.40 | 71.190 | 22.15 | . 636 |
| 371.74 | 22.20 | . 776 | . 70 | . 657 | . 70 | . 787 | 20.97 | . 126 | 23.00: | 69.026 | . 50 | . 234 | . 12 | . 652 |
| . 88 | 22.00 | . 780 | . 65 | . 658 | . 70 | . 791 | 21.10 | . 128 | (22.7 | . 033 | . 57 | . 242 | . 14 | . 654 |
| 372.76 | 21.96 | . 804 | . 70 | . 679 | . 80 | . 813 | 20.97 | . 143 | (22.7 | . 077 | . 50 | . 287 | . 12 | . 673 |
| 373.94 | 22.20 | . 835 | . 60 | . 705 | 21.70 | . 843 | 21.11 | . 161 | 22.75 | . 137 | . 70 | . 349 | 22.05 | . 693 |
| 394.69 | . 00 | 37.392 | . 40 | 30.153 | 22.70 | 35.369 | . 62 | . 496 | (22.7 | . 181 | . 75 | 72.426 | 21.85 | 26.081 |
| 395.77 | . 13 | . 421 | . 60 | . 176 | . 80 | . 397 | . 65 | . 513 | (22.5 | . 235 | . 87 | . 482 | . 87 | . 101 |
| . 94 | . 13 | . 425 | . 65 | . 180 | . 85 | . 401 | . 60 | . 516 | (22.5 | . 244 | . 95 | . 491 | . 99 | . 104 |
| 396.68 | . 10 | . 445 | . 50 | . 197 | . 90 | . 420 | . 60 | . 528 | (22.5 | . 281 | . 98 | . 530 | 21.92 | . 118 |
| . 84 | - | - | . 45 | . 199 | . 85 | . 424 | . 70 | . 531 | 22.70: | . 289 | - | - | 22.06 | . 121 |
| 397.90 | . 11 | . 478 | . 60 | . 223 | . 85 | . 451 | . 64 | . 547 | . 40 | . 342 | 23.00: | . 593 | 22.02 | . 140 |
| 403.84* | 22.10: | . 835 | . 10 | . 351 | . 00 | . 601 | . 60 | . 644 | (22.3 | 70.641 | 23.00: | . 901 | 21.90 | . 252 |
| 426.83* | 21.50 | 38.252 | . 35 | . 848 | 22.00 | 36.184 | . 16 | 23.015 | (22.3 | 71.798 | 22.44 | 74.095 | . 95 | . 682 |
| 450.69 | 22.45 | . 893 | 21.10 | 31.364 | - | - | 21.35 | . 400 | (22.5 | 72.999 | 22.70 | . 334 | 21.90 | 27.128 |
| 5690.94 | 21.55 | 45.334 | 21.58 | 36.558 | 21.95 | 42.882 | 21.07 | 27.275 | (22.7 | 85.088 | (23.00 | 87.811 | 22.30 | 31.621 |
| 692.88 | . 65 | . 387 | . 30 | . 600 | . 90 | . 931 | . 13 | . 306 | (22.7 | . 186 | 23.00 | . 911 | . 20 | . 657 |
| 693.88 | . 60 | . 413 | . 33 | . 622 | 21.90 | . 957 | . 14 | . 322 | 22.50 | . 236 | 22.70 | . 963 | 22.22 | . 675 |
| 715.78 | . 63 | 46.000 | . 20 | 37.095 | 22.80 | 43.512 | . 64 | . 675 | . 50 | 86.338 | . 40 | 89.100 | 21.85 | 32.085 |
| 716.77 | . 40 | . 027 | . 20 | . 117 | . 70 | . 537 | . 71 | . 691 | . 60 | . 388 | . 37 | . 152 | . 85 | . 104 |
| 717.79 | . 40 | . 054 | . 10 | . 139 | . 60 | . 563 | . 90 | . 708 | . 30 | . 439 | . 45 | . 204 | . 87 | . 122 |
| 718.77 | . 33 | . 080 | . 25 | . 160 | 22.60 | . 588 | . 84 | . 724 | . 20 | . 489 | . 52 | . 256 | . 87 | . 141 |
| 719.80 | 21.40 | . 108 | . 25 | . 183 | 21.90 | . 614 | . 68 | . 741 | . 20 | . 540 | . 58 | . 309 | 21.97 | . 161 |
| 808.78 | 22.12 | 48.493 | 21.35 | 39.106 | 21.80 | 45.871 | 21.04 | 29.176 | (22.5 | 98.018 | 22.95 | . 929 | 22.10 | 33.825 |

Table B. Photovisual observations and phases of seventeen Cepheids and five Porulation II variables.

| $\begin{aligned} & \text { JD } \\ & 2,430,000+ \end{aligned}$ | $\checkmark 2$ |  |  | $\vee 3$. |  |  | V 5 |  |  | $\vee 8$ |  |  | $\vee 9$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | V | Phase | B-V | V | Phase | B-V | V | Phase | B-V | V | Phase | $B-V$ | V | Phase | $B-V$ |
| 4596.95 | 21.42 | 136.672 | $+0.57$ | 20.20 | 46.951 | +0.65 | 20.08 | 46.490 | $+0.74$ | 20.66 | 61.904 | $+1.04$ | 20.50 | 70.154 | +0.58 |
| 4932.92 | 21.36 | 213.592 | . 75 | 20.35 | 73.378 | 1. 15 | 20.08 | 72.656 | . 85 | 20.66 | 96.744 | 1.01 | 20.91 | 109.635 | . 89 |
| 5009.78 | . 00 | 231.189 | . 38 | $\therefore .47$ | 79.420 | 1.07 | . 10 | 78.642 | . 79 | . 72 | 104.714 | . 88 | . 76 | 118.669 | 1.00 |
| 011.75 | 21.36 | . 640 | . 67 | . 53 | . 575 | 1.33 | . 24 | . 796 | 1.10 | . 51 | . 918 | . 84 | . 42 | . 901 | . 52 |
| 035.78 | 20.75 | 237.142 | . 48 | . 50 | 81.465 | 1.20 | . 19 | 80.666 | . 79 | . 36 | 107.410 | . 68 | . 94 | 121.724 | . 88 |
| 036.90 | - | - | - | . 50 : | . 553 | 1.32 | . 40 | . 754 | . 76 | . 41 | . 527 | . 87 | . 30 | . 854 | . 75 |
| 037.66 | 21.29 | . 572 | . 69 | . 75 | . 613 | 1.10 | . 32 | . 813 | 1.07 | . 57 | . 605 | . 93 | . 35 | . 945 | . 35 |
| 065.67 | . 68 | 243.985 | . 38 | . 58 | 83.816 | . 86 | . 52 | 82.995 | 1.19 | . 24 | 110.510 | . 99 | . 45 | 125.237 | . 74 |
| 066.68 | . 04 | 244.216 | . 35 | . 57 | . 896 | . 91 | . 60 | 83.074 | 1.32 | . 50 | . 615 | 1. 12 | . 55 | . 356 | . 86 |
| 068.67 | . 54 | . 672 | . 62 | . 02 | 84.052 | . 37 | . 49: | . 238 | 1.35 | . 66 | . 821 | 1.01 | . 88 | . 590 | . 98 |
| 069.67 | . 79 | . 901 | . 51 | . 05 | . 131 | . 70 | . 50 | . 305 | 1.09 | . 56 | . 925 | . 89 | . 83 | . 708 | . 82 |
| 097.68 | . 00 | 251.314 | . 60 | . 32 | 86.334 | . 96 | 20.17 | 85.487 | . 80 | . 61 | 113.829 | 1.05 | . 30 | 128.999 | . 56 |
| 098.68 | . 29 | . 543 | . 64 | . 50 | . 412 | 1.09 | 19.99 | . 567 | . 65 | . 28 | . 933 | . 89 | . 35 | 129.117 | . 70 |
| 099.71 | 21.23 | . 779 | . 81 | 20.60 | . 493 | 1.20 | 20.03 | . 645 | . 92 | 20.16 | 114.040 | . 69 | 20.35 | . 238 | . 80 |
| 5370.93 | 21.65 | 313.874 | . 64 | 20.60 | 107.825 | . 86 | 20.25 | 106.768 | . 95 | 20.16 | 142.165 | . 62 | 20.35 | 161.112 | . 65 |
| 371.91 | 20.76 | 314.099 | . 47 | . 55 | . 903 | . 97 | . 40 | . 844 | 1.05 | . 11 | . 267 | . 57 | . 30 | . 227 | . 77 |
| 394.75 | 21.10 | 319.328 | . 68 | . 83 | 109.699 | 1.32 | . 07 | 108.623 | . 78 | . 61 | 144.636 | . 88 | . 40 | 163.911 | . 62 |
| 395.74 | . 23 | . 555 | . 81 | . 70 | . 777 | . 97 | . 10 | . 700 | . 95 | . 72 | . 738 | . 98 | . 30 | 164.027 | . 48 |
| 396.71 | . 54 | . 777 | . 62 | . 60 | . 854 | . 78 | . 25 | . 776 | 1.01 | . 56 | . 838 | 1.02 | . 45 | . 142 | . 66 |
| 397.87 | 21.39 | 320.042 | . 32 | . 45 | . 944 | . 55 | . 30 | . 866 | 1. 13 | . 41 | . 959 | . 69 | . 55 | . 278 | . 73 |
| 450.72 | 20.76 | 332.142 | . 59 | 20.05 | 114.101 | . 61 | 20.50 | 113.983 | 1.43 | 20.38 | 150.440 | . 65 | 20.70 | 170.488 | 1.00 |
| 5687.95 | 21.42 | 386.456 |  | 20.70 | 132.759 |  | 20.42 | 131.457 |  | 20.24 | 175.040 |  | 20.70 | 198.368 |  |
| 689.92 | 21.45 | . 907 |  | 20.65 | . 914 |  | . 10 | . 610 |  | . 20 | . 245 |  | . 83 | . 600 |  |
| 690.90 | 20.78 | 387.131 | . 45 | 19.85 | . 991 | . 52 | . 06 | . 687 | . 98 | . 24 | . 346 | . 73 | . 72 | . 715 | . 98 |
| 691.88 | 21.29 | . 356 |  | 20.06 | 133.068 |  | . 32 | . 764 |  | . 36 | . 448 |  | . 70 | . 830 |  |
| 692.91 | . 36 | . 592 | . 71 | . 15 | . 150 | . 60 | . 30 | . 844 | . 96 | . 46 | . 553 | . 89 | . 45 | . 951 | . 40 |
| 693.91 | . 45 | . 821 | . 71 | . 15 | . 228 | . 85 | . 25 | . 922 | 1.22 | . 56 | . 658 | . 94 | . 30 | 199.068 | . 70 |
| 715.81 | 21.48 | 392.835 | . 76 | 20.15 | 134.950 | . 65 | . 06 | 133.627 | . 69 | . 41 | 177.929 | . 99 | . 83 | 201.641 | 1.02 |
| 716.84 | 20.94 | 393.071 | . 44 | 19.95 | 135.031 | . 60 | . 15 | . 708 | . 89 | . 03 | 178.036 | . 72 | . 76 | . 764 | . 76 |
| 717.81 | 21.23 | . 293 | . 41 | 20.15 | . 107 | . 48 | . 32 | . 783 | . 90 | . 03 | . 137 | . 77 | . 53 | . 877 | . 54 |
| 718.85 | . 41 | . 531 | . 54 : | . 25 | . 189 | . 75 | . 40 | . 864 | . 92 | . 07 | . 242 | . 58 | . 31 | 202.000 | . 49 |
| 719.76 | . 29 | . 739 | . 66 | . 25 | . 261 | . 80 | . 47 | . 935 | 1.07 | . 24 | . 339 | . 81 | . 42 | . 107 | . 68 |
| 755.74 | 21.41 | 401.977 |  | . 20 | 138.091 |  | . 16 | 136.737 |  | . 20 : | 181.070 |  | . 30 : | 206.334 |  |
| 808.75 | 20.65 | 419.113 | . 44 | . 35 | 142.260 | . 65 | . 35 | 140.865 | 1. 12 | . 56 | 187.567 | . 94 | . 70 : | . 564 | 1.20 |
| 809.76 | 21.06 | . 344 |  | . 10: | . 340 |  | . 40 | . 943 |  | . 72 | . 672 |  | . 83 | . 683 |  |
| 837.70 | . 48 | 420.741 |  | . 70 | 144.537 |  | . 69 | 143. 120 |  | . 56 | 190.569 |  | . 15 | 215.967 |  |
| 838.65 | 21.54 | . 959 |  | 20.73 | . 611 |  | 20.60 | . 194 |  | 20.90 | . 668 |  | 20.45 | 216.078 |  |
| 6048.95 | 20.83 | 469.107 |  | 20.15 | 161.152 |  | 19.88 | 159.579 |  | 20.46 | 212.476 |  | 20.62 | 240.793 |  |
| 073.85 | 21.54 | 474.808 |  | - | - |  | 20.15 | 161.511 |  | . 20 | 214.058 |  | 21.00 | 243.719 |  |
| . 94 | . 27 | . 829 |  | . 15 | 163.117 |  | . 12 | . 518 |  | . 22 | . 068 |  | 20.89 | . 729 |  |
| 075.90 | . 00 | 475.277 |  | . 50 | . 272 |  | . 10 | . 671 |  | . 20 | . 271 |  | . 40 | . 960 |  |
| . 93 | - | - |  | - | - |  | . 08 | . 673 |  | - | - |  | - | - |  |
| 077.93 | . 41 | . 742 |  | . 50 | . 431 |  | . 34 | . 829 |  | . 28 | . 481 |  | . 45 | 244.198 |  |
| 078.83 | . 29 | . 948 |  | . 60 | . 502 |  | . 40 | . 899 |  | . 36 | . 575 |  | . 50 | . 300 |  |
| 102.90 | . 23 | 481.459 |  | . 47 | 165.395 |  | . 25 | 163.774 |  | . 24 | 218.071 |  | . 35 | 247.133 |  |
| 103.96 | . 36 | . 701 |  | . 52 | . 478 |  | . 32 | . 856 |  | . 16 | . 181 |  | . 43 | . 257 |  |
| 193.75 | 21.06 | 502.259 |  | 20.55 | 172.541 |  | 20.35 | 170.849 |  | 20.41: | 227.492 |  | 20.55: | 257.810 |  |

Table B (continued)

| $\begin{aligned} & \text { JD } \\ & 2,430,000- \end{aligned}$ | $\checkmark 10$ |  |  | V I i |  |  | V13 |  |  | $\vee 15$ |  |  | $\vee 17$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4596.95 | 22.00 | 196.164 | $+0.55$ | 2 i. 25 | 200.479 | +0.55 | 21.64 | 156.968 | +0.43 | 19.75 | 28.075 | +1.05 | 20.57 | 88.677 | +0.66 |
| 4932.92 | 21.75 | 306.567 | . 58 | 21.23 | 313.311 | . 53 | 21.73 | 245.311 | . 85 | 19.40 | 43.875 | . 54 | 20.86 | 138.585 | . 92 |
| 5009.78 | . 88 | 331.824 | . 60 | . 17 | 339.123 | . 33 | . 71 | 265.522 | 1.13 | 20.33 | 47.490 | 1. 09 | 20.86 | 150.003 | 1.05 |
| 011.75 | . 36 | 332.471 | . 61 | . 13 | . 785 | . 69 | . 46 | 266.040 | . 78 | 20.11 | . 583 | 1. 14 | 21.00 | . 292 | 1.27 |
| 035.78 | . 37 | 340.368 | . 58 | 21.06 | 347.855 | . 72 | . 73 | 272.359 | 1.12 | 19.46 | 48.713 | . 43 | 20.53 | 153.865 | 1.02 |
| 036.90 | - | - | - | 20.94 | 348.231 | . 55 | . 75 | . 653 | 1.14 | . 31 | . 765 | . 52 | . 90 | 154.031 | 1.12 |
| 037.66 | 21.65 | . 985 | . 89 | 21.30 | . 487 | . 60 | . 48 | . 853 | . 82 | . 51 | . 801 | . 40 | 20.93 | . 144 | 1.20 |
| 065.67 | 22.10 | 350.190 | - | . 00 | 357.893 | . 78 | . 69 | 280.218 | . 94 | . 80 | 50.118 | 1.16 | 21.05 | 158.305 | 1.20 |
| 066.68 | 21.43 | . 521 | . 69 | . 00 | 358.232 | . 58 | . 81 | . 483 | 1.04 | 19.92 | . 166 | 1.27 | 21.20 | . 455 | 1.25 |
| 068.67 | . 81 | 351.175 | . 74 | 21.00: | . 901 | . 70 | . 34 | 281.007 | . 78 | 20.20 | . 260 | 1.07 | 20.66 | . 750 | . 64 |
| 069.67 | . 60 | . 504 | . 45 | 20.90 | 359.236 | . 69 | . 84 | . 270 | . 81 | . 02 | . 307 | 1.24 | . 65 | . 900 | . 92 |
| 097.68 | . 72 | 360.708 | . 65 | 21.19 | 368.644 | . 72 | . 94 | 288.635 | . 89 | 20.25 | 51.624 | 1.11 | . 96 | 162.060 | 1.16 |
| 098.68 | . 90 | 361.037 | . 64 | . 08 | . 979 | . 43 | . 38 | . 898 | . 74 | 19.84 | . 671 | . 80 | 20.99 | . 209 | 1.18 |
| 099.71 | 21.23 | . 376 | . 59 | 21.06 | 369.326 | . 53 | 21.49 | 289.169 | . 91 | 19.35 | . 720 | . 45 | 21.06 | . 361 | 1.23 |
| 5370.93 | 21.59 | 450.501 | . 46 | 21.05 | 460.411 | . 66 | 21.90 | 360.486 | . 87 | 20.25 | 64.475 | 1.17 | 20.60 | 203.652 | . 75 |
| 371.91 | . 87 | . 823 | . 62 | . 15: | .741 | . 75 | 22.05 | . 744 | . 79 | . 25 | . 521 | 1.05 | . 60 | . 797 | . 80 |
| 394.75 | . 47 | 458.329 | . 53 | . 00 | 468.411 | . 70 | 21.82 | 366.750 | . 74 | . 33 | 65.595 | 1.17 | 20.80 | 207.190 | 1.36 |
| 395.74 | . 65 | . 654 | . 75 | . 16 | . 744 | . 83 | . 45 | 367.010 | . 81 | 20.38 | . 642 | 1.02 | 21.04 | . 337 | 1. 18 |
| 396.71 | . 82 | . 973 | . 88 | . 05 | 469.070 | . 35 | 21.76 | . 265 | . 97 | 19.67 | . 687 | . 78 | 21.19 | . 480 | 1.31 |
| 397.87 | . 47 | 459.354 | . 43 | . 29 | . 459 | . 56 | 22.05 | . 570 | . 95 | . 40 | . 742 | . 30 | 20.60 | . 654 | . 60 |
| 450.72 | 21.71 | 476.721 | . 74 | 21.00 | 487.208 | . 57 | 21.59 | 381.467 | 1.21 | 19.98 | 68.227 | 1.24 | 21.10 | 215.504 | 1.03 |
| 5687.95 | 21.65 | 554.677 |  | 21.00 | 566.879 |  | 21.37 | 443.846 |  | 20.33 | 79.384 |  | 20.48 | 250.745 |  |
| 689.92 | . 65 | 555.325 |  | . 16 | 567.541 |  | . 65 | 444.364 |  | . 40 | . 477 |  | . 82 | 251.037 |  |
| 690.90 | . 65 | . 647 | . 75 | . 15 | . 870 | . 55 | . 95 | . 622 | . 85 | . 20 | . 523 | 1. 25 | 20.85 | . 183 | 1. 15 |
| 691.88 | . 65 | . 969 |  | . 11 | 568.199 |  | . 49 | . 880 |  | . 20 | . 569 |  | 21.25 | . 329 |  |
| 692.91 | . 59 | 556.307 | . 61 | . 23 | . 545 | . 69 | . 76 | 445.151 | . 64 | . 20 | . 618 | 1.27 | 21.12 | . 481 | 1.05 |
| 693.91 | 21.56 | . 636 | . 64 | 21.15 | . 88 i | . 65 | 21.92 | . 414 | . 83 | 20.00 | . 665 | 1.00 | 20.53 | . 630 | . 97 |
| 715.81 | 22.00: | 563.832 | . 65 | 20.90 | 576.236 | . 71 | 22.00 | 451.172 | . 61 | 19.44 | 80.695 | . 71 | . 80 | 254.883 | . 70 |
| 716.84 | 21.93 | 564.171 | . 62 | 21.16 | . 582 | . 78 | 21.80 | . 443 | . 96 | . 23 | . 743 | . 52 | . 78 | 255.036 | 1. 12 |
| 717.81 | . 41 | . 490 | . 64 | 21.10 | . 908 | . 50 | . 73 | . 698 | . 98 | . 28 | . 789 | . 54 | 20.82 | . 180 | 1.23 |
| 718.85 | . 76 | . 831 | . 74 | 20.87 | 577.257 | . 69 | . 66 | . 972 | . 37 | . 40 | . 838 | . 47 | 21.02 | . 335 | 1.03 |
| 719.76 | . 87 | 565. 130 | . 88 | 21.34 | . 562 | . 57 | 21.92 | 452.211 | . 63 | 19.44 | . 880 | . 71 | 21.01 | . 470 | 1.19 |
| 755.74 | . 77 | 576.954 |  | . 31 | 589.646 |  | 22.02 | 461.672 |  | 20.20 | 82.572 |  | 20.57 | 260.815 |  |
| 808.75 | . 20 | 594.373 | . 60 | 21.06 | 607.449 | . 79 | 22.10 | 475.611 | - | 19.75 | 85.066 | . 87 | . 45 | 268.690 | . 72 |
| 809.76 | . 78 | . 705 |  | 20.96 | . 788 |  | 21.41 | . 876 |  | 19.80 | . 113 |  | . 70 | . 840 |  |
| 837.70 | . 77 | 603.887 |  | 20.93 | 617.171 |  | . 49 | 483.223 |  | 20.25 | 86.427 |  | 20.87 | 272.990 |  |
| 838.65 | 21.76 | 604.199 |  | 21.10 | . 490 |  | 21.71 | . 473 |  | 20.16 | . 472 |  | 21.05 | 273.131 |  |
| 6048.95 | 22.00 | 673.305 |  | 20.92 | 688.117 |  | 21.69 | 538.771 |  | 20.07 | 96.362 |  | 21.12 | 304.371 |  |
| 073.85 | 21.48 | 681.488 |  | 21.22 | 696.480 |  | . 70 | 545.319 |  | - | - |  | 20.96 | 308.070 |  |
| . 94 | . 59 | . 517 |  | 21.18 | . 510 |  | . 87 | . 343 |  | . 02 | 97.537 |  | 21.08 | . 084 |  |
| 075.90 | . 82 | 682.161 |  | 20.94 | 697.168 |  | - | - |  | 20.16 | . 630 |  | . 15 | . 375 |  |
| . 93 | - | - |  | 21.00 | . 178 |  | . 59 | . 866 |  | - | - |  | 21.12 | . 379 |  |
| 077.93 | . 59 | . 828 |  | . 11 | . 850 |  | . 79 | 546.392 |  | 19.32 | . 725 |  | 20.57 | . 676 |  |
| 078.83 | - | - |  | . 07 | 698.152 |  | - | - |  | . 40 | . 767 |  | 20.73 | . 810 |  |
| 102.90 | . 94 | 691.034 |  | . 01 | 706.236 |  | . 56 | 552.957 |  | . 53 | 98.899 |  | 21.08 | 312.386 |  |
| 103.96 | . 39 | . 382 |  | 21.17 | . 592 |  | . 69 | 553.236 |  | . 44 | . 949 |  | 21.06 | . 453 |  |
| 193.75 | 21.90 | 720.888 |  | - | - |  | 21.44 | 576.846 |  | 19.84 | 103.172 |  | 20.62 | 325.882 |  |
|  | $\vee 21$ |  |  | $\vee 27$ |  |  | $\vee 30$ |  |  | $\vee 31$ |  |  | $\vee 36$ |  |  |
| 4596.95 | 21.75 | 178.315 | +0.55 | 21.68 | 230.232 | +0.58 | 20.37 | 46.353 | +1.03 | 19.60 | 44.762 | +0.59 | 21.94 | 166.125 | +0.70 |
| 4932.92 | 21.97 | 278.673 | . 76 | 21.95 | 359.808 | . 73 | 20.20 | 72.445 | . 90 | 19.91 | 69.955 | . 64 | 21.76 | 259.622 | . 72 |
| 5009.78 | . 98 | 301.631 | . 83 | . 60 | 389.452 | . 56 | 20.50 | 78.409 | . 80 | . 58 | 75.718 | . 52 | . 94 | 281.011 | . 85 |
| 011.75 | . 55 | 302.220 | . 70 | . 58 | 390.212 | . 58 | 19.95 | . 562 | . 95 | . 75 | . 866 | . 70 | . 81 | . 560 | . 69 |
| 035.78 | . 76 | 309.398 | . 56 | . 64 | 399.480 | . 52 | 20.45 | 80.427 | . 75 | . 58 | 77.668 | . 58 | . 45 | 288.247 | . 66 |
| 036.90 | - | - | - | . 72 | . 912 | . 89 | . 00 | . 514 | . 80 | . 70 | . 752 | . 46 | - | - | - |
| 037.66 | . 36 | . 959 | . 28 | . 71 | 400.205 | . 49 | . 25 | . 573 | . 60 | . 68 | . 809 | . 67 | . 82 | . 770 | . 80 |
| 065.67 | . 78 | 318.326 | . 56 | . 68 | 411.008 | 1.05 | . 30 | 82.749 | 1.15 | . 85 | 79.909 | . 69 | . 62 | 296.565 | . 88 |
| 066.68 | . 82 | . 628 | . 81 | . 36 | . 398 | . 60 | . 25 | . 827 | 1.39 | . 85 | . 985 | . 81 | . 67 | . 846 | 1. 10 |
| 068.67 | . 53 | 319.222 | . 63 | . 94 | 412.165 | . 74 | . 50 | . 982 | 1.32 | 19.95 | 80.134 | . 89 | . 77 | 297.400 | . 42 |
| 069.67 | . 86 | . 521 | . 62 | . 65 | . 551 | . 78 | . 55 | 83.059 | 1.45 | 20.07 | . 209 | . 81 | . 71 | . 678 | . 92 |
| 097.68 | . 53 | 327.888 | . 70 | . 45 | 423.354 | . 55 | . 47 | 85.235 | 1.23 | 19.97 | 82.310 | . 81 | . 60 | 305.473 | . 71 |
| 098.68 | . 47 | 328.187 | . 55 | . 74 | . 739 | . 85 | . 35 | . 312 | 1.20 | . 83 | . 385 | . 74 | . 77 | . 752 | . 95 |
| 099.71 | 21.70 | . 494 | . 74 | 21.87 | 424.137 | . 70 | 20.38 | . 393 | 1.09 | 19.80 | . 462 | . 66 | 21.82 | 306.038 | . 98 |
| 5370.93 | 21.82 | 409.510 | . 62 | 21.76 | 528.741 | . 74 | 20.15 | 106.452 | . 85 | 19.75 | 102.799 | . 52 | 21.71 | 381.516 | . 71 |
| 371.91 | 22. 10 | . 803 | - | . 82 | 529.119 | . 78 | . 10 | . 530 | . 73 | . 73 | . 872 | . 64 | . 87 | . 788 | 1.02 |
| 394.75 | 21.71 | 416.626 | . 74 | . 88 | 537.927 | 1.00 | . 42 | 108.303 | . 98 | . 70 | 104.585 | . 50 | . 95 | 388.145 | . 80 |
| 395.74 | . 26 | . 921 | . 59 | . 44 | 538.309 | . 56 | . 47 | . 379 | . 95 | . 60 | . 660 | . 51 | . 65 | . 420 | . 59 |
| 396.71 | 21.82 | 417.211 | . 41 | . 76 | . 684 | . 89 | 20.05 | . 454 | . 85 | . 58 | . 732 | . 57 | . 88 | . 690 | . 84 |
| 397.87 | 22.05 | . 558 | . 65 | . 92 | 539.130 | . 83 | 19.93 | . 545 | . 87 | . 68 | . 819 | . 68 | . 95 | 389.013 | . 75 |
| 450.72 | 21.70 | 433.345 | . 77 | 21.67 | 559.514 | . 68 | 20.10 | 112.649 | . 99 | 19.62 | 108.782 | . 62 | 21.76 | 403.720 | . 84 |

Table B（continued）


Table B (continued)

| $\begin{aligned} & \text { JD } \\ & 2,43 C, 000+ \end{aligned}$ | $\checkmark 22$ |  |  | $\vee 24$ |  |  | $\checkmark 34$ |  |  | $\vee 55$ |  |  | $\checkmark 57$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\checkmark$ | Pnase | B-V | V | Phase | $B-V$ | V | Phase | B-V | V | Phase | B-V | v | Fnase | o- ${ }^{-}$ |
| 5687.95 | 21.00 | 45.254 |  | 20.75 | 36.493 |  | 20.55 | 27.227 |  |  |  |  | 21.39 | 31.565 |  |
| 689.92 | . 06 | . 307 |  | . 85 | . 535 |  | . 45 | . 258 |  | 22.00 | 87.757 |  | . 50 | . 602 |  |
| 690.90 | . 14 | . 333 | $+0.41$ | . 75 | . 557 | +0.83 | . 45 | . 274 | +0.62 | . 26 | . 808 | - | . 42 | . 620 | $+0.88$ |
| 691.88 | . 02 | . 359 |  | . 75 | . 579 |  | . 50 | . 290 |  | . 05 | . 859 |  | . 64 | . 638 |  |
| 692.91 | . 06 | . 387 | . 59 | . 55 | . 601 | . 75 | . 52 | . 307 | . 61 | (22.0 | . 912 | - | . 52 | . 658 | . 68 |
| 693.91 | . 08 | . 414 | . 52 | . 56 | . 623 | . 77 | . 53 | . 324 | . 61 | 22.10 | . 964 | - | . 50 | . 676 | . 72 |
| 715.81 | 21.17 | 46.001 | . 46 | . 52 | 37.096 | . 68 | . 88 | . 676 | . 76 | 21.59 | 89.001 | +0.81 | . 35 | 32.086 | . 50 |
| 716.84 | 20.89 | . 028 | . 51 | . 60 | . 118 | . 60 | 20.83 | . 692 | . 88 | . 65 | . 156 | . 72 | . 30 | . 105 | . 55 |
| 717.81 | 21.00 | . 054 | . 40 | . 60 | . 140 | . 50 | 21.07 | . 709 | . 83 | . 65 | . 205 | . 80 | . 42 | . 123 | . 45 |
| 718.85 | 20.89 | . 082 | . 44 | . 50 | . 161 | . 75 | 20.73 | . 725 | 1.11 | . 54 | . 260 | . 98 | . 27 | . 143 | . 60 |
| 719.76 | 20.94 | . 107 | . 46 | . 50 | . 182 | . 75 | . 91 | . 740 | . 77 | . 40 | . 307 | 1.18 | . 29 | . 160 | . 68 |
| 755.74 | 21.06 | 47.071 |  | . 35 | . 960 |  | . 22 | 28.320 |  | 21.41 | 91.176 |  | . 60 | . 832 |  |
| 808.75 | . 17 | 48.493 | . 95 | . 80 : | 39.106 | . 55 | . 34 | 29.175 | . 70 | 22.16 | 93.928 | - | . 42 | 33.824 | . 68 |
| 809.76 | . 13 | . 520 |  | . 50 | . 127 |  | . 37 | . 191 |  | 21.82 | . 981 |  | . 48 | . 843 |  |
| 837.70 | . 11 | 49.269 |  | . 35 | . 731 |  | . 70 | . 642 |  | . 65 | 95.432 |  | . 42 | 34.365 |  |
| 838.65 | 21.00 | . 294 |  | 20.55 | . 753 |  | 20.58 | . 657 |  | 21.65 | . 481 |  | 21.28 | . 383 |  |
| 6048.95 | 21.06 | 54.932 |  | 20.60 | 44.298 |  | 20.50 | 33.050 |  | 21.82 | 106.402 |  | 21.21 | 38.315 |  |
| 073.85 | . 66 | 55.600 |  | . 98 | . 837 |  | . 79 | . 451 |  | - | - |  | . 35 | . 781 |  |
| . 94 | . 66 | . 602 |  | . 85 | . 839 |  | . 81 | . 454 |  | 22.23 | 107.700 |  | . 35 | . 783 |  |
| 075.90 | . 76 | . 655 |  | - | - |  | . 70 | . 484 |  | - | - |  | - | - |  |
| . 93 | . 65 | . 656 |  | . 70 | . 878 |  | - | - |  | - | - |  | . 40 | . 820 |  |
| 077.53 | . 29 | . 709 |  | . 65 : | . 925 |  | . 76 | . 514 |  | 22.23 | . 907 |  | - | - |  |
| 078.83 | . 29 | . 733 |  | . 80 | . 944 |  | . 83 | . 532 |  | - | - |  | - | - |  |
| 102.90 | . 48 | 36.379 |  | . 50 | 45.465 |  | . 53 | . 920 |  | 21.53 | 109.204 |  | . 34 | 39.324 |  |
| 103.96 | . 36 | . 407 |  | . 53 | . 487 |  | . 53 | . 937 |  | 21.64 | . 259 |  | . 33 | . 344 |  |
| 193.75 | 21.36 | 58.814 |  | 20.25: | 47.429 |  | 20.35 | 35.385 |  | 22.35 | 113.92 \| |  | 21.13 | 41.023 |  |

Table C. Photographic observations and phases for ten eclipsing binaries.

| JD | $\vee 1 *$ |  | $\checkmark 12$ |  | $\checkmark 23^{*}$ |  | $\vee 29$ |  | $\vee 35$ |  | $\vee 60$ |  | $\begin{gathered} \vee 7^{*} \\ B \end{gathered}$ | $\begin{aligned} & V 40^{\star} \\ & B \end{aligned}$ | $\begin{gathered} V^{44} \\ B \end{gathered}$ | $\begin{gathered} V 45^{*} \\ B \\ \hline \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2,430,000+ | B | Phase | B | Phase | B | Phase | B | Phase | $B$ | Phase | B | Phase |  |  |  |  |
| 4184.951 | 21.39 | 0.360 | 21.67 | 0.578 | 20.73 | 0.249 | 21.94 | 0.536 | 22.01 | 0.811 | 19.07 | 0.231 | 20.90 | 21.08 | 21.67 | 22.04 |
| 224.892 | . 10 | . 438 | . 60 | . 763 | . 88 | . 564 | . 64 | . 891 | 22.04 | . 966 | . 00 | . 680 | . 75 | . 25 | . 84 | 21.92 |
| 243.835 |  |  | . 62 | . 913 | . 86 | . 560 | 21.94 | . 482 | 21.79 | . 629 | . 15 | . 264 | . 72 | . 30 | . 88 | 22.38 |
| 244.833 |  |  | . 65 | . 343 | . 63 | . 718 | 22.18 | . 566 | 21.79 | . 033 | . 38 | . 400 | . 91 | . 35 | . 94 | . 18 |
| 245.842 | . 18 | . 480 | . 67 | . 777 | . 84 | . 877 | 21.65 | . 651 | 22.06 | . 441 | 19.04 | . 536 | 20.84 | . 10 | . 74 | . 24 |
| . 896 | - | - | . 54 | . 800 | . 84 | . 886 | . 56 | . 655 | 21.94 | . 463 | 18.98 | . 545 | 21.30 | . 29 | . 62 | 22.36 |
| 246.807 |  |  | . 60 | . 192 | . 98 | . 030 | . 69 | . 732 | 22.12 | . 831 | 19.00 | . 669 | 20.83 | . 10 | . 73 | 21.96 |
| 277.749 | . 19 | . 542 | . 88 | . 505 | . 90 | . 923 | . 72 | . 331 | 22.80 | . 347 | 19.14 | . 850 | . 83 | . 17 | . 69 | 22.73 |
| 304.597 |  |  | 21.75 | . 099 | . 81 | . 185 | . 84 | . 594 | 21.82 | . 247 | 18.91 | . 567 | . 87 | . 13 | . 86 | 21.94 |
| 305.659 | . 48 | . 597 | 22.10 | . 514 | . 90 | . 337 | . 54 | . 675 | . 76 | . 636 | . 94 | . 698 | . 84 | . 17 | . 76 | 22.28 |
| 330.699* | - | - | 21.57 | . 287 | . 78 | . 297 | . 60 | . 779 | 21.85 | . 765 | . 90 | . 114 | . 74 | . 12 | - | $\underline{21.98}$ |
| 334.638 | . 65 | . 654 | 22.06 | . 982 | . 84 | . 920 | . 48 | . 110 | 22.79 | . 358 | 18.92 | . 651 | 20.80 | 21.13 | . 67 | 22.38 |
| 360.615 |  |  | 21.45 | . 159 | . 75 | . 028 | 21.57 | . 292 | . 00 | . 865 | 19.02 | . 195 | 21.01 | 20.98 | . 58 | . 04 |
| 361.607 | 21.55 | . 706 | . 52 | . 586 | . 73 | . 184 | 22.00 | . 375 | . 01 | . 267 | . 34 | . 330 | 20.77 | 20.95 | . 77 | . 18 |
| 362.673 | - | - | 21.88 | . 045 | 20.88 | . 353 | 22. 18 | . 465 | 22.03 | . 698 | 19.02 | . 476 | 20.81 | 21.45 | 21.72 | 22.08 |
| 4596.913 | (22.5 | . 166 | 21.60 | . 831 | 20.91 | . 396 | 21.55 |  | 21.97 | . 445 | 19.38 | . 431 | 20.72 | 21.00 | 21.74 | 22.17 |
| 597.877 | " |  | . 53 | . 219 | . 78 | . 548 | . 54 | . 222 | 22.16 | . 835 | . 00 | . 562 | 20.71 | 20.88 | . 72 | 21.92 |
| 598.878 | " |  | . 63 | . 250 | . 86 | . 707 | . 33 | . 306 | 21.90 | . 240 | . 02 | . 699 | 21.39 | . 91 | . 60 | . 84 |
| 599.875 | " |  | . 66 | . 105 | . 88 | . 864 | 21.60 | . 390 | . 98 | . 643 | . 43 | . 835 | 20.78 | . 72 | . 69 | 21.84 |
| 600.880 | " | . 174 | 21.78 | . 539 | . 91 | . 023 | 22.00 | . 474 | . 97 | . 050 | 19.18 | . 972 | . 68 | . 94 | . 72 | 22.75 |
| 601.956 | " |  | 22.01 | . 000 | . 80 | . 193 | 21.70 | . 564 | 21.91 | . 485 | 18.97 | . 119 | . 72 | . 84 | . 80 | . 16 |
| 602.878* | " |  | 21.57 | . 397 | 20.84 | . 339 | . 50 | . 642 | 22. 10 | . 858 | 19.05 | . 245 | . 85 | . 91 | - | . 18 |
| $625.772 *$ | " | . 223 | I. | - | 21.11 | . 960 | . 75 | . 565 | 21.80 | . 118 | . 40 | . 368 | . 95 | - | - | . 8 |
| . 889 | " |  | . 61 | . 298 | 21.15 | . 978 | . 77 | . 575 | . 84 | . 165 | . 51 | . 384 | . 77 | . 86 | . 80 | . 20 |
| 626.769 | ' |  | . 63 | . 650 | 20.80 | . 117 | . 65 | . 648 | . 95 | . 521 | . 02 | . 504 | . 87 | . 88 | . 74 | . 28 |
| . $875{ }^{\text {* }}$ | " |  | . 50 | . 696 | . 80 | . 134 | . 50 | . 658 | 21.90 | . 564 | 19.00 | . 518 | . 92 | - | - | - |
| 627.763 | " | . 227 | . 60 | . 104 | . 81 | . 274 | . 67 | . 732 | 22.07 | . 923 | 18.90 | . 639 | . 76 | . 97 | . 89 | - |
| 628.910 | " |  | 21.65 | . 598 | . 97 | . 456 | . 60 | . 828 | 22.34 | . 388 | 19.27 | . 796 | . 74 | . 97 | . 67 | . 78 |
| 629.764 | " |  | 22.16 | . 965 | . 72 | . 591 | . 88 | . 900 | 21.94 | . 733 | . 33 | . 912 | . 70 | . 94 | . 67 | . 14 |
| 630.783 | " | . 233 | 21.64 | . 404 | . 76 | . 752 | . 76 | . 986 | 21.78 | . 145 | . 02 | . 051 | . 89 | . 92 | . 78 | 22.08 |
| 633.761 | " |  | . 60 | . 685 | . 81 | . 223 | . 52 | . 236 | 22.80 | . 350 | 19.15 | . 458 | . 68 | . 92 | . 56 | 21.80 |
| 634.845 | (22.5 | . 241 | . 57 | . 151 | . 88 | . 394 | . 58 | . 327 | 22.01 | . 788 | 18.93 | . 606 | . 68 | . 90 | . 70 | 21.86 |
| 660.749 | 21.31 | . 292 | . 62 | . 271 | 20.92 | . 491 | . 98 | . 503 | 21.98 | . 266 | 19.02 | . 139 | . 70 | . 95 | . 74 | 22.04 |
| 663.795 | . 50 | . 297 | . 54 | . 608 | 21.06 | . 973 | . 50 | . 759 | 21.93 | . 498 | 18.90 | . 555 | . 88 | . 92 | . 70 | . 08 |
| 680.640 | . 23 | . 331 | . 56 | . 856 | 20.69 | . 636 | . 62 | . 174 | 22.44: | . 312 | 19.40 | . 853 | . 91 | . 94 | . 64 | . 36 |
| 681.690 |  |  | . 52 | . 308 | 20.69 | . 802 | . 52 | . 262 | 21.98 | . 737 | 19.02 | . 996 | . 85 | . 83 | . 48 | . 53 |
| 682.659 |  |  | 21.48 | . 726 | 21.05 | . 956 | . 90 | . 343 | 21.84 | . 128 | 18.90 | . 128 | . 81 | . 87 | . 58 | . 02 |
| 714.625* |  |  | 22.00 | . 478 | - | - | . 60 | . 029 | . | . | 19.00 | . 489 | . 8 | . 87 | . | . 02 |
| 717.609 |  |  | 21.65 | . 563 | 20.92 | . 483 | 21.69 | . 279 | 22.02 | . 266 | . 32 | . 896 | . 75 | . 82 | . 61 | . 02 |
| 718.625 | 21.15 | . 405 | 21.64 | . 199 | 20.76 | . 643 | 22.06 | . 365 | 22.06 | . 677 | 19.07 | . 035 | 20.79 | 20.90 | 21.50 | 22.06 |

Table C (continued)

| JD | $\vee 1 *$ |  | $\checkmark 12$ |  | $\vee 23$ * |  | $\vee 29$ |  | $\vee 35$ |  | $\vee 60$ |  | $\begin{gathered} V^{7 *} \\ B \end{gathered}$ | $\begin{aligned} & V 40^{*} \\ & B \end{aligned}$ | $\begin{gathered} V 44 \\ B \end{gathered}$ | $\begin{aligned} & \vee 45^{\star} \\ & B \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2,430,000+ | B | Phase | B | Phase | B | Phase | B | Phase | B | Phase | B | Phase |  |  |  |  |
| 4923.949 |  |  | 21.73 | 0.543 | 20.90 | 0.113 | 21.60 | 0.612 | 21.95 | 0.728 | 18.90 | 0.045 | 20.88 | 20.97 | 21.52 | 22.32 |
| 924.953 |  |  | 22.04 | . 975 | . 70 | . 272 | . 52 | . 696 | . 86 | . 134 | 18.97 | . 182 | . 87 | 21.06 | . 52 | 21.98 |
| 925.952 | 21.37 | 0.810 | 21.70 | . 405 | . 92 | . 430 | . 56 | . 780 | . 98 | . 538 | 19.28 | . 318 | . 73 | 20.92 | . 52 | 22.36 |
| 926.947 |  |  | . 52 | . 833 | . 81 | . 587 | . 92 | . 863 | 21.88 | . 941 | 19.15 | . 454 | . 80 | 20.95 | . 82 | 22.38 |
| 927.950* | - | - | . 45 | . 265 | . 78 | . 746 | . 80 | . 948 | 22.60: | . 346 | 18.90 | . 591 | . 77 | 21.00 | - | - |
| 928.945 |  |  | . 60 | . 793 | . 82 | . 903 | . 72 | . 031 | 22.00 | . 748 | 19. 10 | . 727 | . 85 | . 11 | . 65 | 21.94 |
| 929.952 | . 27 | . 818 | . 60 | . 126 | . 85 | . 063 | . 72 | . 116 | 21.83 | . 155 | . 38 | . 864 | . 90 | 21.00 | . 58 | . 90 |
| 930.955 |  |  | 21.67 | . 558 | . 91 | . 221 | . 50 | . 200 | . 96 | . 561 | 19.09 | . 001 | . 87 | 20.81 | . 72 | . 92 |
| 931.945 |  |  | 22.04 | . 984 | . 72 | . 378 | . 57 | . 283 | 21.80 | . 962 | 18.94 | . 136 | . 84 | 21.00 | . 80 | . 98 |
| 932.955 | . 33 | . 824 | 21.71 | . 418 | 20.88 | . 537 | . 62 | . 368 | 22.44 | . 371 | 19. 15 | . 274 | . 85 | 20.94 | . 64 | 21.90 |
| 954.969 | . 69 | . 867 | . 60 | . 890 | 21.00 | . 019 | . 80 | . 217 | 22.14 | . 275 | . 24 | . 277 | . 84 | 20.98 | . 58 | 22.20 |
| 981.876 | . 20 | . 920 | . 92 | . 467 | 20.78 | . 274 | . 82 | . 478 | 21.90 | . 158 | . 07 | . 948 | . 87 | . 95 | . 69 | . 08 |
| 983.862 |  |  | . 50 | . 321 | . 88 | . 588 | . 67 | . 644 | 21.92 | . 961 | . 15 | . 218 | . 77 | . 92 | . 69 | . 16 |
| 984.917 |  |  | . 49 | . 775 | . 76 | . 755 | . 56 | . 733 | 22.20 | . 389 | . 61 | . 362 | . 74 | . 95 | . 70 | . 02 |
| 985.865 | . 22 | . 928 | . 62 | . 183 | . 84 | . 905 | . 62 | . 813 | . 00 | . 772 | . 06 | . 492 | 20.97 | . 85 | . 67 | . 24 |
| . 977 |  |  | . 47 | . 231 | . 82 | . 922 | . 46 | . 822 | 22.08 | . 818 | . 03 | . 507 | 21.19 | - | . 78 | 22.16 |
| 5006.785 |  |  | . 60 | . 184 | . 81 | . 213 | . 69 | . 570 | 21.96 | . 235 | . 49 | . 346 | 20.69 | 20.87 | . 78 | 21.88 |
| 007.805 | . 11 | . 971 | . 52 | . 623 | . 90 | . 358 | . 50 | . 656 | . 86 | . 647 | 19.20 | . 485 | . 97 | 21.00 | . 85 | 22.28 |
| 008.789 |  |  | 21.70 | . 046 | . 83 | . 530 | . 49 | . 738 | . 96 | . 045 | 18.90 | . 619 | . 85 | 20.90 | . 64 | . 04 |
| 009.819 | . 17 | . 974 | 22.12 | . 490 | . 76 | . 693 | . 62 | . 825 | 21.98 | . 462 | 19.12 | . 760 | . 81 | . 80 | . 64 | . 10 |
| 010.764 |  |  | 21.54 | . 896 | . 78 | . 842 | 21.82 | . 904 | 22.11 | . 844 | . 32 | . 888 | . 70 | - | . 64 | . 06 |
| 011.794 |  |  | . 64 | . 339 | . 98 | . 005 | 22.00 | . 991 | . 00 | . 261 | . 10 | . 029 | 20.81 | . 92 | . 69 | . 36 |
| 035.735 |  |  | . 58 | . 640 | 20.74 | . 791 | 21.76 | . 002 | 22.01 | . 944 | . 24 | . 295 | 21.35 | . 85 | . 64 | . 32 |
| 036.868 | . 15 | . 027 | 21.60 | . 128 | 21.32 | . 965 | . 69 | . 097 | 21.96 | . 403 | 19.21 | . 450 | 21.26 | 20.98 | . 76 | . 48 |
| 037.702 |  |  | 22.12 | . 487 | 20.81 | . 102 | . 54 | . 167 | 21.90 | . 740 | 18.88 | . 563 | 20.87 | 21.01 | . 67 | . 18 |
| . 838 |  |  | 21.80 | . 545 | . 80 | . 124 | . 43 | . 178 | 22.16 | . 794 | . 82 | . 582 | . 78 |  | . 67 | . 20 |
| 038.702 | . 33 | . 031 | . 58 | . 917 | . 74 | . 260 | . 62 | . 251 | 21.88 | . 144 | 18.93 | . 700 | . 73 | 20.92 | . 65 | . 73 |
| 064.633 |  |  | 21.65 | . 074 | . 81 | . 361 | . 72 | . 429 | . 94 | . 632 | 19.11 | . 237 | . 75 | 21.17 | . 56 | . 16. |
| 065.628 | . 45 | . 084 | 22.03 | . 502 | . 76 | . 518 | . 92 | . 513 | 21.86 | . 035 | . 40 | . 373 | . 69 | 20.94 | . 77 | . 14 |
| 066.632 |  |  | 21.76 | . 934 | . 72 | . 677 | . 58 | . 597 | 22.00 | . 442 | 19.07 | . 510 | 20.72 | 21.11 | . 80 | . 06 |
| 067.624 |  |  | . 49 | . 361 | 20.73 | . 834 | . 65 | . 680 | 22.10 | . 843 | 18.86 | . 645 | 21.02 | . 04 | . 64 | . 16 |
| 068.623 | . 50 | . 090 | . 64 | .791 | 21.00 | . 992 | 21.64 | . 764 | 21.96 | . 247 | 19.15 | . 782 | 20.76 | . 04 | . 70 | . 32 |
| 069.626 |  |  | . 50 | . 222 | 20.76 | . 150 | 22.00 | . 848 | . 82 | . 653 | . 20 | . 918 | 20.83 | 21.06 | . 79 | 22.48 |
| . 814 |  |  | . 54 | . 303 | . 77 | . 180 | 21.84 | . 864 | . 93 | . 729 | . 12 | . 944 | 21.06 | 20.87 | . 82 | 21.92 |
| 097.625 | . 67 | . 147 | . 57 | . 269 | . 81 | . 578 | . 45 | . 200 | . 90 | . 978 | . 07 | . 738 | 20.78 | 21.10 | . 64 | 22.28 |
| . 760 |  |  | . 50 | . 327 | . 90 | . 600 | . 52 | . 212 | 21.86 | . 032 | . 10 | . 756 | 21.06 | - | . 64 | . 14 |
| 098.639 |  |  | . 50 | . 705 | . 81 | . 739 | . 72 | . 294 | 22.36 | . 388 | . 43 | . 876 | 20.77 | 20.97 | . 70 | . 06 |
| 099.661 | 21.70 | . 151 | . 54 | . 145 | . 82 | . 900 | . 82 | . 372 | 22.10 | . 802 | 19.03 | . 016 | . 70 | 21.11 | . 76 | . 02 |
| 100.685 |  |  | 21.63 | . 586 | 20.86 | . 062 | 21.96 | . 458 | 21.99 | . 216 | 18.90 | . 155 | 20.81 | 20.98 | 21.83 | 22.40 |
| 5342.822 | 21.30 | . 626 | 21.65 | . 769 | 20.81 | . 354 | 21.67 | . 797 | 22.00 | . 158 | 19.06 | . 188 | 21.01 | 21.11 | 21.72 | 22.28 |
| 370.886 |  |  | . 56 | . 844 | 20.84 | . 792 | . 64 | . 154 | . 02 | . 510 | 19.02 | . 016 | 20.84 | . 11 | . 78 | . 04 |
| 371.738 | . 38 | . 683 | . 64 | . 211 | 21.00 | . 927 | . 40 | . 226 | 22.10 | . 854 | 18.85 | . 132 | . 74 | - | . 70 | - |
| . 810 |  |  | . 57 | . 242 | . 05 | . 938 | - | - | 21.98 | . 884 | 18.93 | . 142 | 20.77 | . 04 | . 73 | - |
| . 876 |  |  | . 63 | . 270 | 21.11 | . 948 | . 48 | . 238 | 21.89 | . 911 | 19.03 | . 151 | 21.10 | - | - | . 00 |
| 372.760 | . 49 | . 685 | . 46 | . 651 | 20.78 | . 088 | . 60 | . 312 | 22.12 | . 268 | . 11 | . 272 | 20.72 | . 21 | . 64 | 22.73 |
| . 914 |  |  | - | - | . 78 | . 113 | . 50 | . 325 | 22.63 | . 330 | . 30 | . 293 | . 74 | - | - | 21.96 |
| 373.936 |  |  | . 60 | . 157 | . 84 | . 274 | . 90 : | . 411 | 21.92 | . 744 | . 35 | . 432 | . 98 | . 65 | - | 22.63 |
| 394.687 | . 35 | . 728 | . 55 | . 085 | . 75 | . 556 | . 55 | . 154 | . 90 | . 137 | . 05 | . 263 | . 78 | . 11 | - | . 63 |
| 395.766 |  |  | . 81 | . 549 | . 82 | . 726 | . 45 | . 244 | . 85 | . 573 | . 30 | . 410 | . 74 | - | - | . 73 |
| . 866 |  |  | . 50 | . 592 | - | - | . 57 | . 253 | . 87 | . 614 | . 24 | . 424 | 20.99 | - | . 76 | - |
| . 937 |  |  | . 55 | . 623 | . 76 | . 753 | . 55 | . 259 | . 85 | . 643 | 19.25 | . 434 | 21.31 | 21.31 | . 73 | . 36 |
| 396.679 |  |  | 21.85 | . 942 | . 88 | . 871 | . 80 | . 321 | . 96 | . 943 | 18.90 | . 535 | 20.80 | - | - | - |
| . 843 | . 25 | . 732 | 22.20 | . 013 | - | - | . 62 | . 335 | 21.88 | . 009 | 18.82 | . 557 | . 74 | - | . 65 | - |
| 397.704 |  |  | 22.25 | . 469 | . 80 | . 064 | 21.90 | . 424 | 22.00 | . 438 | 19.00 | . 702 | 20.80 | 20.97 | - | - |
| 403.839* | . 38 | . 746 | 21.90 | . 023 | . 88 | . 003 | 22.00 | . 923 | - | - | 19.00 | . 512 | 21.40 | 21.11 | - | - |
| 426.834* | . 20 | . 791 | . 60 | . 916 | . 72 | . 639 | 21.80 | . 854 | 21.80 | . 140 | 18.90 | . 648 | . 20 | 21.04 | - | - |
| 450.686 | 21.48 | . 838 | 21.50: | . 179 | 20.86 | . 412 | 21.75 | . 858 | 22.10 | . 788 | 19.20 | . 903 | 21.30 | 20.97 | - | 22.08 |
| 5690.944 | 21.65 | . 307 | 21.65 | . 555 | 20.88 | . 406 | 21.85 | . 039 | 21.90 | . 970 | 19.00 | . 678 | 20.80 |  | 21.80 | 22.34 |
| 692.881 |  |  | . 60 | . 388 | . 75 | . 712 | . 63 | . 202 | 22.01 | . 754 | 19.16 | . 943 | . 75 |  | . 63 | . 04 |
| 693.877 | . 54 | . 313 | . 66 : | . 816 | . 85 | . 870 | . 55 | . 286 | 21.83 | . 156 | 18.97 | . 078 | . 72 |  | 21.78 | 22.21 |
| 715.782 |  |  | . 50 | . 241 | . 75 | . 333 | . 40 | . 125 | . 80 | . 017 | 19.00 | . 067 | . 80 |  |  |  |
| 716.771 | . 63 | . 358 | . 50 | . 667 | . 90 | . 490 | . 70 | . 209 | . 90 | . 417 | . 00 | . 201 | . 70 |  |  |  |
| 717.787 |  |  | 21.60 | . 104 | . 70 | . 650 | 21.60 | . 294 | . 95 | . 828 | . 30 | . 340 | 20.75 |  |  |  |
| 718.772 |  |  | 22.10 | . 528 | 20.90 | . 806 | 22.00 | . 377 | . 85 | . 226 | 19.20 | . 474 | 21.00 |  |  |  |
| 719.802 | . 45 | . 364 | 22.00 | . 971 | 21.20 | . 969 | 21.85 | . 463 | . 90 | . 643 | 18.90 | . 615 | . 20 |  |  |  |
| 808.782 | 21.45 | . 538 | 21.60 | . 256 | 20.85 | . 040 | 21.80 | . 937 | 21.80 | . 634 | 19.05 | . 753 | 21.06 |  |  |  |
| 6103.915 | 21.30 | .116 | 21.45 | . 241 | 20.90 | . 713 | 21.45 | . 729 | 21.80 | . 012 | 19.00 | . 016 | 20.75 |  |  |  |
| 104.959 |  |  | . 50 | . 690 | . 80 | . 878 | . 70 | . 817 | . 90 | . 434 | 18.90 | . 159 | 21.75 |  |  |  |
| 128.720 |  |  | 21.55 | . 914 | 20.80 | . 636 | 21.70 | . 812 | 21.90 | . 045 | 19.26 | . 400 | 21.40 |  |  |  |
| Photovisual Observations |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | V |  | V |  | $\checkmark$ |  | $\checkmark$ |  | $\checkmark$ |  | $\checkmark$ |  | V | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| 4596.949 | (22.0 | . 166 | 21.48 | . 846 | 21.00 | . 402 | 21.72 | . 144 | 21.90 | . 460 | 19.52 | . 436 |  | 21.0 | 21.57 | 21.75 |
| 097.677 | 22.0 | . 147 | . 45 | . 292 | 20.82 | . 587 | . 66 | . 205 | . 79 | . 999 | . 36 | . 745 |  |  | . 80 | - |
| 5690.899 | 21.5 | . 307 | . 75 | . 535 | . 97 | . 399 | . 67 | . 036 | . 84 | . 952 | . 22 | . 672 |  |  | . 73 | 22.09 |
| 716.844 | . 55 | . 358 | 21.61 | . 698 | 20.98 | . 502 | 21.78 | . 215 | 21.99 | . 446 | 19.25 | . 212 |  |  | 21.90 | - |
| 6103.915 | 21.6 | . 116 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 128.720 | (22.0 | . 164 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 193.751 | ${ }^{2} 1.7$ | . 292 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

Table D. Magnitudes and colors of 546 stars in Field IV, M31.

| $\begin{gathered} \text { Star } \\ \text { A } \end{gathered}$ | V | B-V | $\begin{gathered} \text { Star } \\ \text { A } \end{gathered}$ | V | B-V | Star A | V | B-V | $\begin{gathered} \text { Star } \\ \text { A } \end{gathered}$ | V | B-V | Star A | V | B-V | $\begin{gathered} \text { Star } \\ \text { A } \end{gathered}$ | V | B-V | $\begin{gathered} \text { Star } \\ \text { A } \end{gathered}$ | $\checkmark$ | B-V |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 20.41 | 1.57 | 48 | 21.93 | -. 09 | 86 | 20.63 | -. 09 | 137 | 19.54 | -. 01 | 178 | 20.56 | . 87 | 240 | 18.50 | . 02 | 280 | 21.61 | . 14 |
| 2 | 21.91 | . 04 | 49 | 21.19 | . 09 | 87 | 20.84 | -. 21 | 138 | 21.43 | . 77 | 179 | 15.62 | . 51 | 241 | 18.18 | . 82 | 281 | 21.30 | . 82 |
| 3 | 21.94 | . 99 | 50 | 20.71 | 1.57 | 88 | 20.13 | 1.69 | 139 | 20.09 | 1.57 | 180 | 20.74 | 1.60 | 242 | 21.23 | -. 06 | 282 | 21. 18 | -. 04 |
| 4 | 21.52 | . 69 | 51 | 21.64 | . 10 | 89 | 21.26 | . 65 | 140 | 18.06 | . 53 | 181 | 20.07 | . 40 | 243 | 19.26 | 2.20 | 284 | 18.82 | 1.86 |
| 5 | 19.58 | 1.23 | 52 | 20.79 | . 03 | 90 | 21.53 | . 01 | 141 | 18.95 | 1.47 | 182 | Galax | y | 244 | 19.76 | . 77 | 285 | 21.65 | . 11 |
| 7 | 21.71 | . 17 | 53 | 20.88 | . 18 | 91 | 21.70 | . $25^{\text {s }}$ | 142 | 21.68 | -. 09 | 183 | 19.03 | . 68 | 245 | 20.95 | . 28 | 287 | 21.72 | . 00 |
| 9 | 22.15 | -. 04 | 54 | 21.50 | -. 06 | 92 | 18.75 | 1.72 | 143 | 16.21 | 1.39 | 184 | 20.78 | . 10 | 246 | 20.54 | . 19 | 288 | 21.32 | -. 11 |
| 10 | 19.18 | . 03 | 54a | 21.85 | . 00 | 93 | 21.65 | . 07 | 144 | 21.34 | -. 08 | 185 | 18.86 | . 45 | 247 | 21.02 | -. 01 | 289 | 20.23 | 1.63 |
| 11 | 22.16 | -. 01 | 55 | 20.35 | . 17 | 94 | 21.27 | -. 15 | 145 | 20.78 | -. 09 | 186 | 20.89 | . 07 | 248 | 21.89 | -. 06 | 290 | 21.09 | -. 09 |
| 12 | 21.59 | 1.13 | 56 | 19.90 | -. 06 | 96 | 21.76 | . 47 | 146 | 20.24 | 1.54 | 200 | 19.68 | . 02 | 249 | 21.55 | -. 08 | 291 | 20.92 | 1.47 |
| 13 | 20.97 | 1.51 | 57 | 19.98 | 1.23 | 97 | 20.23 | . 27 | 147 | 21.88 | . 02 | 201 | 21.17 | . 12 | 250 | 21.54 | . 00 | 292 | 21.86 | . 06 |
| 14 | 21.72 | -. 11 | 58 | 19.44 | . 03 | 98 | 20.14 | . 82 | 148 | 21.16 | 1.35 | 203 | 19.50 | -. 20 | 250a | 21.83 | . 28 | 293 | 21.37 | . 32 |
| 15 | 19.01 | . 81 | 59 | 21.16 | 1.36 | 99 | 21.05 | 1.48 | 149 | 21.51 | 1.49 | 205 | 21.78 | -. 04 | 250b | 21.37 | . 02 | 294 | 21.90 | . 01 |
| 16 | 20.88 | 1.60 | 60 | 21.95 | . 39 | 100 | 21.02 | . 96 | 150 | 21.84 | -. 03 | 206 | 20.06 | -. 05 | 251 | 21.41 | 1.22 | 295 | 19.36 | -. 03 |
| 17 | 21.67 | 1.05 | 61 | 21.46 | . 03 | 101 | 21.21 | 1.37 | 151 | 20.30 | . 41 | 207 | 17.25 | . 50 | 252 | 20.04 | . 02 | 296 | 21.24 | . 06 |
| 19 | 20.83 | 1.37 | óla | 21.79 | . 12 | 102 | 20.90 | 1.67 | 152 | 20.89 | 1.30 | 208 | 21.42 | -. 04 | 253 | 21.33 | . 02 | 297 | 21.15 | . 06 |
| 22 | 20.24 | . 27 | 616 | 20.87 | . 25 | 105 | 18.45 | 1.28 | 153 | 20.11 | 1.65 | 209 | 20.71 | -. 02 | 254 | 20.64 | -. 05 | 298 | 21.50 | -. 04 |
| 23 | 20.33 | 1.51 | 61 c | 21.24 | 1.41 | 106 | 21.09 | 1.27 | 154 | 20.40 | . 79 | 210 | 21.92 | -. 05 | 255 | 21.44 | -. 06 | 300 | 20.29 | 1.42 |
| 25 | 20.94 | . 32 | 62 | 19.63 | 1.72 | 107 | 21.47 | 1.13 | 155 | 18.84 | 1.65 | 211 | 20.46 | -. 12 | 256 | 20.97 | -. 11 | 301 | 19.61 | 1.70 |
| 26 | 18.20 | 1.60 | 63 | 20.33 | 1.73 | 108 | 21.74 | 1.08 | 156 | 20.70 | 1. 49 | 212 | 21.12 | 1.57 | 257 | 20.94 | -. 05 | 302 | 19.75 | -. 05 |
| 27 | 20.75 | . 01 | 64 | 21.14 | 1.31 | 109 | 21.65 | 1.28 | 157 | 18.08 | 1.62 | 213 | 21.87 | . 01 | 258 | 19.73 | . 75 | 303 | 21.50 | . 42 |
| 28 | 20.13 | -. 05 | 65 | 21.58 | -. 07 | 110 | 21.16 | 1.17 | 158 | 20.60 | 1.54 | 214 | 19.92 | 1.72 | 259 | 20.91 | -. 17 | 304 | 21.51 | 1.04 |
| 29 | 17.75 | . 95 | 66 | 20.98 | 1.62 | 111 | 16.45 | . 73 | 159 | 22.06 | -. 10 | 215 | 21.73 | . 07 | 260 | 21.23 | -. 06 | 305 | 20.64 | -. 09 |
| 30 | 21.34 | -. 05 | 67 | 20.81 | 1.63 | 112 | 20.58 | 1.64 | 160 | 20.94 | 1.50 | 216 | 19.61 | 1.83 | 261 | 21.89 | -. 13 | 306 | 15.38 | . 67 |
| 31 | 21.52 | . 29 | 68 | 21.83 | . 64 | 113 | 21.23 | 1.28 | 161 | 20.43 | . 39 | 217 | 20.66 | 1.58 | 262 | 20.53 | -. 10 | 307 | 19.42 | . 78 |
| 32 | 21.20 | 1.17 | 69 | 20.33 | 1.82 | 120 | 21.35 | 1.19 | 162 | 20.69 | 1.01 | 219 | 21.60 | . 00 | 263 | 20.11 | -. 12 |  |  |  |
| 33 | 21.46 | -. 15 | 70 | 21.88 | . 39 | 121 | 20.51 | 1.70 | 163 | 19.94 | . 30 | 222 | 19.32 | 1.61 | 265 | 20.91 | -. 04 |  |  |  |
| 34 | 21.94 | -. 08 | 71 | 19.46 | . 94 | 123 | 19.90 | 1.66 | 164 | 21.03 | -. 04 | 223 | 19.28 | -. 04 | 267 | 21.03 | 1. 44 |  |  |  |
| 35 | 21.37 | -. 19 | 73 | 21.34 | . 04 | 124 | 20.94 | . 71 | 166 | 20.81 | 1.36 | 225 | 21.39 | . 61 | 268 | 21.53 | 1.22 |  |  |  |
| 36 | 20.11 | 1.28 | 74 | 18.89 | 1.50 | 125 | 18.37 | 1.63 | 167 | 21.52 | -. 18 | 226 | 21.23 | . 34 | 269 | 21.73 | -. 06 |  |  |  |
| 37 | 21.09 | -. 05 | 75 | 18.47 | . 39 | 126 | 21.58 | 1. 10 | 168 | 21.69 | -. 06 | 227 | 21.91 | . 62 | 270 | 19.99 | 1.62 |  |  |  |
| 38 | 21.38 | . 10 | 76 | 16.58 | . 59 | 127 | 21.87 | -. 07 | 169 | 20.98 | . 29 | 228 | 21.47 | 1.21 | 271 | 20.86 | . 34 |  |  |  |
| 39 | 20.39 | . 02 | 77 | 21.27 | -. 13 | 128 | 20.48 | 1.59 | 170 | 17.90 | . 73 | 230 | 20.92 | 1.77 | 272 | 20.76 | -. 02 |  |  |  |
| 40 | 21.07 | . 02 | 78 | 19.05 | . 86 | 129 | 18.60 | 1.53 | 171 | 20.11 | -. 06 | 232 | 19.14 | -. 18 | 273 | 21.81 | . 11 |  |  |  |
| 41 | 21.02 | 1.54 | 79 | 18.61 | . 93 | 130 | 21.70 | . 05 | 172 | 19.88 | -. 23 | 233 | 18.42 | . 84 | 274 | 20.81 | 1.58 |  |  |  |
| 42 | 21.95 | -. 11 | 80 | 21.79 | -. 15 | 131 | 19.46 | . 73 | 173 | 21.13 | 1.48 | 234 | 21.04 | -. 08 | 275 | 21.18 | 1.44 |  |  |  |
| 43 | 21.51 | . 06 | 81 | 19.28 | . 61 | 132 | 20.61 | 1.56 | 174 | 21.45 | -. 04 | 236 | 21.97 | . 01 | 276 | 21.82 | . 06 |  |  |  |
| 45 | 21.70 | -. 03 | 82 | 20.75 | 1.63 | 134 | 21.48 | -. 19 | 175 | 19.23 | . 81 | 237 | 21.23 | . 03 | 277 | 21.77 | -. 14 |  |  |  |
| 46 | 21.11 | -. 09 | 83 | 20.63 | 1.42 | 135 | 18.87 | 1. 15 | 176 | 21.45 | -. 17 | 238 | 21.40 | 1.31 | 278 | 21.81 | -. 13 |  |  |  |
| 47 | 20.69 | . 19 | 85 | 21.89 | . 06 | 136 | 21.31 | -. 08 | 177 | 20.68 | -. 04 | 239 | 20.66 | -. 16 | 279 | 21.67 | . 01 |  |  |  |
| B |  |  | B |  |  | B |  |  | B |  |  | B |  |  | B |  |  | B |  |  |
| 1 | 21.37 | -. 17 | 41 | 19.05 | -. 29 | 76 | 21.81 | . 07 | 117 | 17.22 | 1.51 | 156 | 21.02 | 1.27 | 202 | 20.71 | 1.68 | 244 | 21.15 | . 38 |
| 2 | 17.03 | . 80 | 42 | 21.19 | -. 01 | 77 | 21.64 | -. 11 | 118 | 17.51 | . 54 | 159 | 20.35 | 1.74 | 203 | 21.12 | . 09 | 245 | 20.64 | 1.42 |
| 3 | 21.73 | . 71 | 43 | 21.39 | -. 11 | 78 | 21.41 | . 08 | 119 | 21.31 | 1.32 | 160 | 17.49 | . 98 | 204 | 21.16 | 1. 48 | 246 | 21.58 | . 71 |
| 4 | 19.41 | 1.81 | 44 | 21.06 | -. 05 | 79 | 17.43 | . 65 | 120 | 21.29 | 1.47 | 162 | 20.97 | 1.55 | 205 | 21.61 | . 83 | 247 | 19.06 | . 93 |
| 5 | 21.87 | -. 05 | 45 | 21.76 | -. 13 | 80 | 19.09 | 1.61 | 121 | 21.40 | . 19 | 163 | 21.43 | -. 23 | 206 | 20.51 | . 69 | 248 | 21.74 | . 00 |
| 6 | 21.24 | 1.42 | 46 | 20.04 | -. 15 | 81 | 16.65 | . 65 | 122 | 21.10 | 1.46 | 165 | 21.85 | -. 08 | 207 | 21.71 | 1. 16 | 249 | 19.60 | . 70 |
| 7 | 18.07 | . 59 | 47 | 21.85 | 1.01 | 82 | 21.92 | -. 01 | 123 | 21.46 | 1.44 | 166 | 20.88 | 1.51 | 208 | 21.70 | 1.22 | 250 | 18.56 | . 82 |
| 8 | 21.66 | -. 12 | 48 | 20.41 | -. 11 | 83 | 21.66 | -. 10 | 124 | 17.11 | . 55 | 167 | 20.81 | . 45 | 209 | 17.41 | 1.05 | 252 | 19.10 | 1.65 |
| 9 | 21.79 | -. 11 | 49 | 17.65 | . 87 | 84 | 21.75 | -. 03 | 125 | 17.61 | . 70 | 168 | 20.22 | 1.77 | 210 | 21.40 | . 19 | 253 | 21.92 | 1. 18 |
| 10 | 20.61 | . 22 | 50 | 21.84 | . 23 | 85 | 20.14 | 1.25 | 126 | 16.93 | . 44 | 169 | 20.31 | 1.72 | 211 | 21.90 | . 14 | 254 | 21.55 | 1.29 |
|  | 21.29 | -. 07 | 51 | 18.99 | 2.13 | 86 | 21.69 | . 00 | 127 | 21.43 | 1.25 | 170 | 20.84 | . 46 | 212 | 21.41 | . 26 | 255 | 20.56 | 1.57 |
| 12 | 21.85 | . 12 | 52 | 20.53 | -. 09 | 87 | 20.17 | . 02 | 128 | 17.86 | 1.58 | 171 | 20.66 | . 16 | 213 | 20.52 | 1.52 | 256 | 20.65 | . 20 |
| 13 | 21.46 | -. 02 | 53 | 21.76 | . 11 | 88 | 21.36 | . 11 | 129 | 20.61 | 1.58 | 172 | 21.00 | 1.44 | 214 | 21.93 | . 29 | 257 | 19.74 | 1.76 |
| 14 | 20.59 | -. 16 | 54 | 20.67 | -. 08 | 89 | 21.45 | . 12 | 130 | 18.20 | . 54 | 173 | 20.43 | -. 12 | 215 | 21.22 | 1.17 | 258 | 19.14 | 1.45 |
| 15 | 21.42 | . 08 | 55 | 21.29 | . 11 | 90 | 21.57 | . 13 | 131 | 16.93 | . 63 | 174 | 19.98 | . 56 | 216 | 18.99 | . 52 | 259 | 18.46 | 1.69 |
| 16 | 19.90 | -. 15 | 56 | 20.42 | -. 03 | 91 | 20.24 | . 73 | 132 | 19.74 | 1.50 | 176 | 21.09 | 1.34 | 217 | 17.07 | . 68 | 260 | 20.10 | 1.65 |
| 17 | 21.79 | -. 05 | 57 | 20.16 | -. 14 | 92 | 21.87 | -. 06 | 133 | 15.41 | . 94 | 177 | 21.69 | -. 02 | 218 | 20.22 | -. 02 | 261 | 21.90 | . 84 |
| 18 | 19.27 | -. 10 | 58 | 21.84 | -. 11 | 93 | 20.78 | -. 25 | 134 | 21.55 | 1.36 | 178 | 18.44 | . 58 | 219 | 20.76 | . 53 | 262 | 21.16 | 1.24 |
| 19 | 19.19 | -. 19 | 59 | 17.84 | -. 15 | 94 | 19.08 | 1.77 | 135 | 21.48 | 1.51 | 179 | 18.84 | . 60 | 220 | 16.28 | . 97 | 263 | 17.02 | . 64 |
| 20 | 20.73 | -. 22 | 60 | 21.54 | -. 07 | 95 | 19.40 | 1.06 | 136 | 21.23 | . 72 | 180 | 21.41 | -. 14 | 221 | 21.72 | . 57 | 264 | 19.97 | 1.43 |
| 21 | 21.61 | -. 01 | 60 a | 20.08 | -. 09 | 96 | 19.33 | 1.80 | 137 | 20.94 | 1.62 | 182 | 20.79 | 1.63 | 222 | 20.72 | 1.53 | 265 | 21.85 | . 02 |
| 22 | 20.01 | . 97 | 60b | 21.81 | . 09 | 97 | 21.88 | . 15 | 138 | 19.18 | 1.77 | 183 | 20.52 | . 13 | 223 | 21.34 | 1.38 | 266 | 20.37 | -. 24 |
| 23 | 21.58 | -. 09 | 61 | 20.09 | 1.72 | 98 | 21.75 | . 91 | 139 | 21.60 | 1.13 | 184 | 17.60 | . 64 | 224 | 21.06 | 1.51 | 267 | 20.62 | . 62 |
| 24 | 18.63 | -. 19 | 62 | 21.10 | -. 04 | 99 | 18.88 | 2.04 | 140 | 20.92 | . 60 | 185 | 21.70 | -. 08 | 225 | 20.93 | 1.50 | 268 | 21.71 | -. 11 |
| 25 | 21.96 | . 10 | 63 | 20.57 | -. 22 | 100 | 21.94 | -. 12 | 141 | 21.55 | 1.25 | 186 | 21.89 | . 99 | 226 | 20.27 | -. 02 | 269 | 21.27 | 1.49 |
| 26 | 19.80 | -. 21 | 64 | 19.61 | -. 29 | 101 | 21.65 | . 27 | 142 | 19.04 | 1.56 | 187 | 21.01 | 1.58 | 227 | 21.27 | 1.06 | 270 | 17.08 | . 99 |
| 27 | 21.91 | -. 11 | 65 | 21.94 | -. 08 | 102 | 20.37 | 1.18 | 143 | 18.03 | . 58 | 188 | 21.86 | . 39 | 228 | 18.31 | 1.15 | 271 | 18.39 | 1.58 |
| 28 | 21.17 | -. 03 | 66 | 21.93 | -. 12 | 103 | 17.90 | 1.08 | 143 a | 21.74 | 1.21 | 189 | 19.87 | . 56 | 229 | 21.95 | . 67 | 272 | 21.15 | 1.45 |
| 29 | 20.56 | 1.60 | 67 | 21.41 | -. 07 | 104 | 21.66 | . 02 | 144 | 21.17 | 1.51 | 190 | 19.36 | 1.85 | 230 | 18.58 | 1.77 | 273 | 21.04 | 1.73 |
| 30 | 21.00 | . 16 | 68 | 21.84 | . 08 | 106 | 21.65 | -. 14 | 145 | 20.01 | 1.65 | 191 | 18.81 | 1.43 | 231 | 21.21 | . 57 | 274 | 21.59 | 1.11 |
| 31 | 21.97 | . 00 | 68a | 21.85 | . 03 | 107 | 21.09 | -. 07 | 146 | 21.77 | . 73 | 192 | 21.61 | . 03 | 232 | 21.52 | . 76 | 275 | 21.52 | 1.30 |
| 32 | 21.76 | . 27 | 69 | 20.90 | -. 20 | 108 | 16.72 | . 43 | 147 | 21.32 | 1.52 | 193 | 21.44 | . 55 | 234 | 20.35 | 1.07 | 276 | 21.99 | . 59 |
| 33 | 19.08 | -. 19 | 69a | 16. 19 | . 80 | 109 | 19.88 | . 86 | 148 | 20.46 | . 93 | 194 | 21.12 | . 38 | 236 | 21.95 | . 01 | 277 | 21.54 | 1.43 |
| 34 | 19.96 | 1.51 | 69b | 20.63 | . 04 | 110 | 17.39 | . 88 | 149 | 20.62 | . 01 | 195 | 21.85 | . 31 | 237 | 21.17 | . 36 | 278 | 21.95 | . 05 |
| 35 | 21.45 | -. 19 | 70 | 20.95 | -. 01 | 111 | 21.20 | 1. 40 | 150 | 21.03 | -. 19 | 196 | 21.34 | 1. 17 | 238 | 21.85 | -. 15 | 279 | 21.70 | . 67 |
| 36 | 21.85 | . 15 | 71 | 19.42 | -. 26 | 112 | 20.02 | 1.66 | 151 | 20.04 | -. 17 | 197 | 21.63 | . 13 | 239 | 21.41 | -. 04 | 280 | 20.87 | -. 01 |
| 37 | 21.67 | -. 12 | 72 | 20.58 | -. 04 | 113 | 19.86 | 1.69 | 152 | 21.73 | 1.28 | 198 | 18.22 | . 34 | 240 | 20.18 | 1.56 | 281 | 19.66 | 1.70 |
| 38 | 17.47 | . 91 | 73 | 19.94 | 1.79 | 114 | 19.42 | 1.62 | 153 | 21.57 | -. 14 | 199 | 18.89 | . 76 | 241 | 21.21 | 1.51 | 282 | 21.22 | . 20 |
| 39 | 20.06 | -. 20 | 74 | 19.78 | -. 29 | 115 | 21.36 | 1.54 | 154 | 21.63 | 1.15 | 200 | 18.53 | 1.34 | 242 | 21.91 | . 85 | 283 | 20.32 | 1.07 |
| 40 | 21.30 | -. 06 | 75 | 21.07 | . 31 | 116 | 20.88 | 1.62 | 155 | 21.61 | -. 18 | 201 | 21.18 | 1.51 | 243 | 16.71 | . 62 | 284 | 20.87 | 1.70 |

## Note on Planetary Nebulae in M 31

LITTLE can be added to Baade's report (1955) on five planetary nebulae that he found in Field IV in M31. They have been marked on the chart (Plate I of the preceding paper) and are numbered using a prefix PL. Table I lists new magnitudes for them based on

Table I.

|  |  |  |  |  |
| ---: | :---: | :---: | :---: | :---: |
|  | $B$ | $V$ | $B-V$ | $M_{B}$ |
| PL 1 | $22.2:$ | $\ldots$ | $\ldots$ | -2.65 |
| 2 | 22.2 | 21.5 | +0.7 | 2.65 |
| 4 | 22.4 | 21.3 | +1.1 | 2.35 |
| 5 | 22.3 | 21.7 | +0.6 | 2.55 |
| 6 | 22.3 | 21.0 | +1.3 | -2.55 |
| Mean | 22.3 | 21.4 | +0.9 | -2.55 |

Arp's photoelectric sequence and measured in the same way as the variables. The apparent magnitudes are uncorrected for reddening.
Both the $B$ and $V$ magnitudes are very sensitive to whether the emission lines are included or cut off by the combination of plate and filter used. The conversion of these $B$ magnitudes to the International system used in planetary nebulae catalogues has not been attempted as the measured magnitudes are excitation dependent.

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Baade, W. 1955 . Astron J. 60, 151.

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# Distribution of Stars in the Leo I Dwarf Galaxy 

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#### Abstract

The distribution of resolved stellar images in the dwarf galaxy Leo I has been determined from star counts on seven plates. The galaxy is elliptical in outline and perfectly symmetrical within the observational uncertainties. The ellipticity is approximately uniform from the center outwards with a value of $\epsilon$ of $0.31 \pm 0.07$. The star density profile of the Leo I system resembles those of other dwarf elliptical galaxies, and is unlike those for giant ellipticals. If the distance to the system is 230 kpc , then the observed sharp cutoff in radius at $14.3 \mathrm{~min} \pm 1.0 \mathrm{~min}$, along the major axis, corresponds to a linear cutoff radius of $0.95 \pm 0.07$ kpc . This is somewhat smaller than the computed present tidal radius.


## I. INTRODUCTION

THE Leo I galaxy (Fig. 1) is the fourth object to be studied in an attempt to determine and understand the structure of dwarf elliptical galaxies. The three previous galaxies studied (Hodge 1961a, 1961b, 1962) were found to be remarkably similar in their structural properties. All showed a steeper profile than predicted by a Hubble luminosity law and all had a distinct cutoff at a distance near to, but somewhat smaller than what one predicts from tidal considerations. In the local group of galaxies the two most distant known dwarf ellipticals are the Leo I and Leo II systems discovered in 1950 (Harrington and Wilson 1950). Leo I, although brighter than Leo II, has not been extensively studied because of its proximity to the star Regulus, which makes photography of the system difficult for large telescopes with correcting lenses. Baade (1950) obtained a few plates of it with the 200inch telescope, using diaphragms in the optics to cut down reflections from Regulus. He estimated that the distance to the galaxy is about the same as that of the

Leo II system, for which Sandage (1961) quotes a distance modulus of $m-M=21.8$, corresponding to 230 kpc . Baade found a few RR Lyrae variables, and no evidence for globular clusters or dust or gas. Many RR Lyrae variables have been found at Berkeley using 120 -inch plates and these are presently being studied ; periods and light curves are not yet available. There is a diffuse object near the major axis of Leo I, but this is apparently unrelated to the system; on the best 120 -inch plates it has the appearance of a distant spiral galaxy. The total apparent magnitude of Leo I has been measured by Holmberg (1958), who finds $m_{\mathrm{v}}=10.40$ and $C I=+0.87$. The dimensions from Holmberg's data are 12.0 min by 9.5 min ; these compare with Harrington and Wilson's estimate of a diameter of 17 min . Accepting a distance of 230 kpc leads to a value for the absolute visual magnitude of the system of $M_{\mathrm{v}}=-11 \cdot 4$, and the linear dimensions determined by Holmberg become 830 by 650 pc . Intrinsically Leo I is an exceedingly small, very faint object, though brighter by 1.5 mag. than Leo II.

